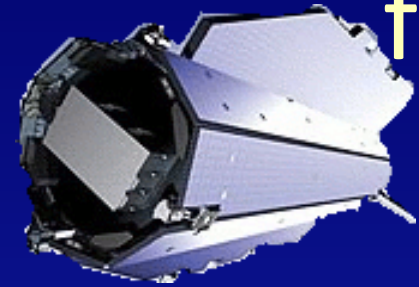


Multi-scale gravity field modeling from GOCE & surface data



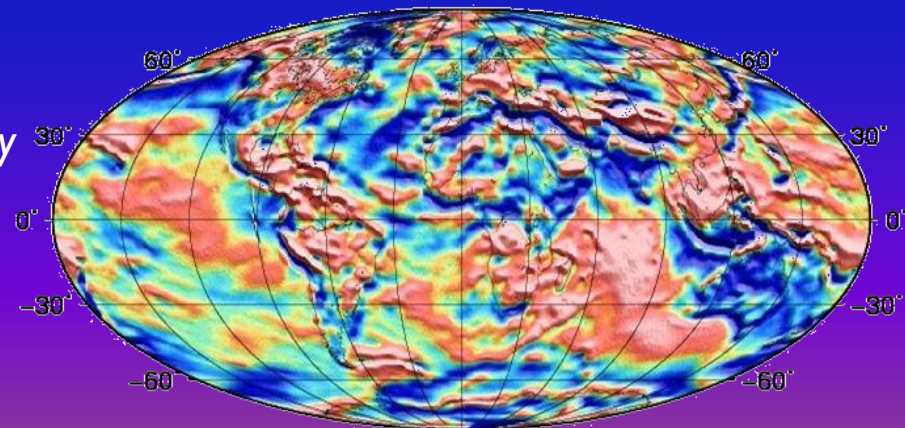
*I. Panet^{1,2}, G. Pajot-Métivier¹, O. Jamet¹,
M. Holschneider³, L. Métivier^{1,2}*



1 – Institut National de l'Information Géographique & Forestière, GRGS, France

2 - Institut de Physique du Globe de Paris, Sorbonne Paris-Cité, Université Paris-Diderot, UMR CNRS 7154, France

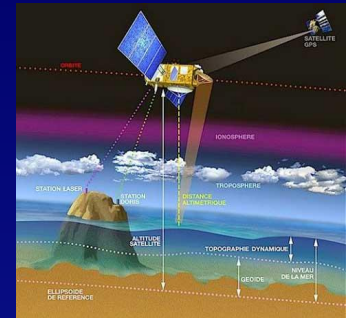
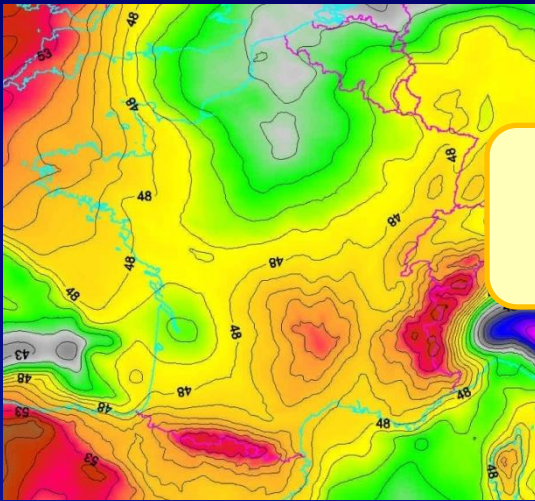
*3 – University of Potsdam, Department of
Applied Mathematics, Germany*



Motivations

Geopotential modeling

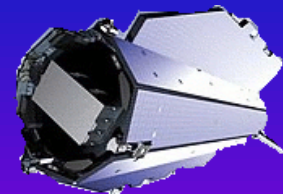
Geoid

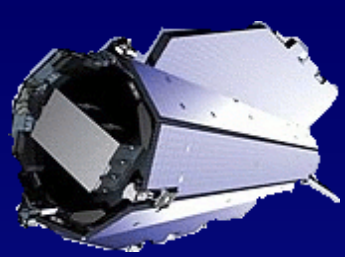


- Local zoom
- *Best possible precision at all spatial scales from large, heterogeneous datasets*

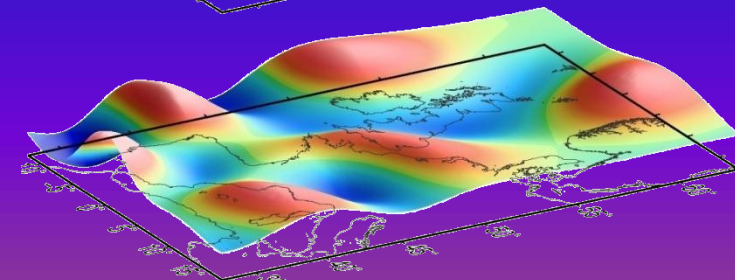
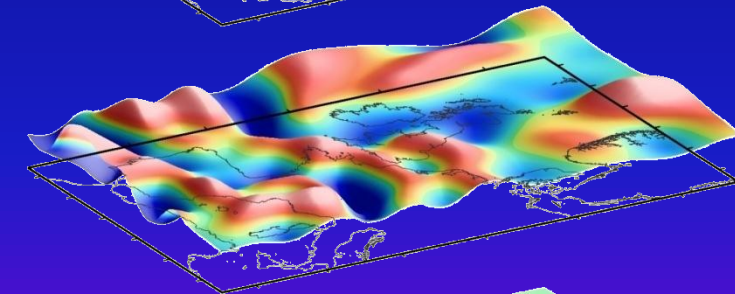
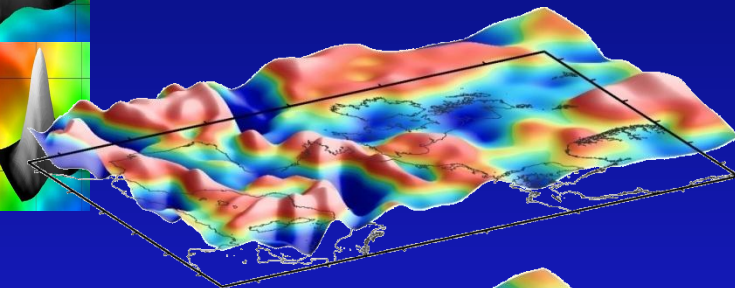
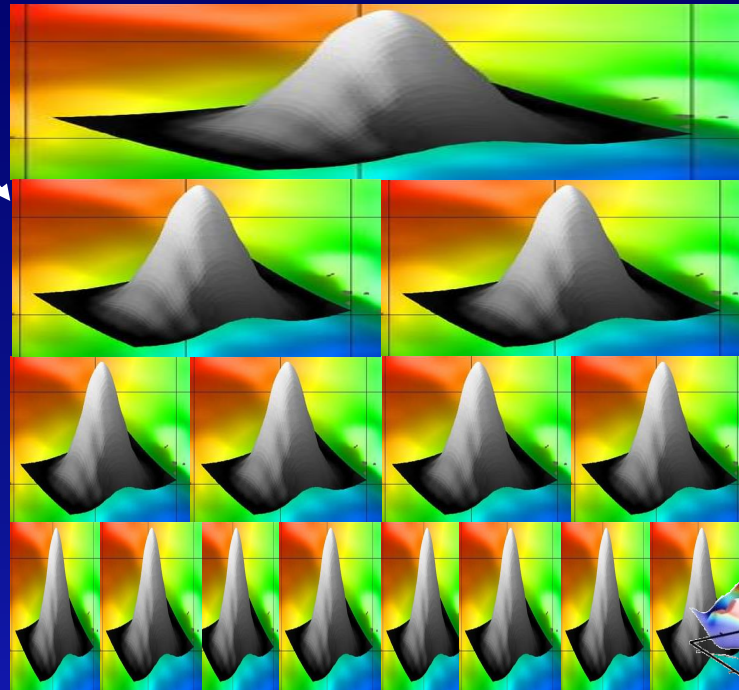
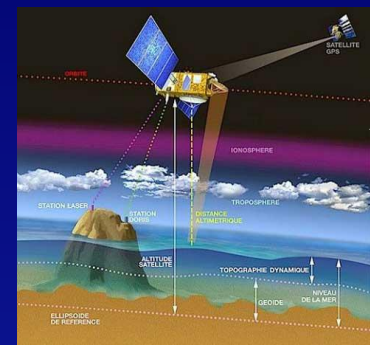
Use of the GOCE gradients

- Curvature of the equipotential surfaces
- Redundancy → local signal/noise optimization





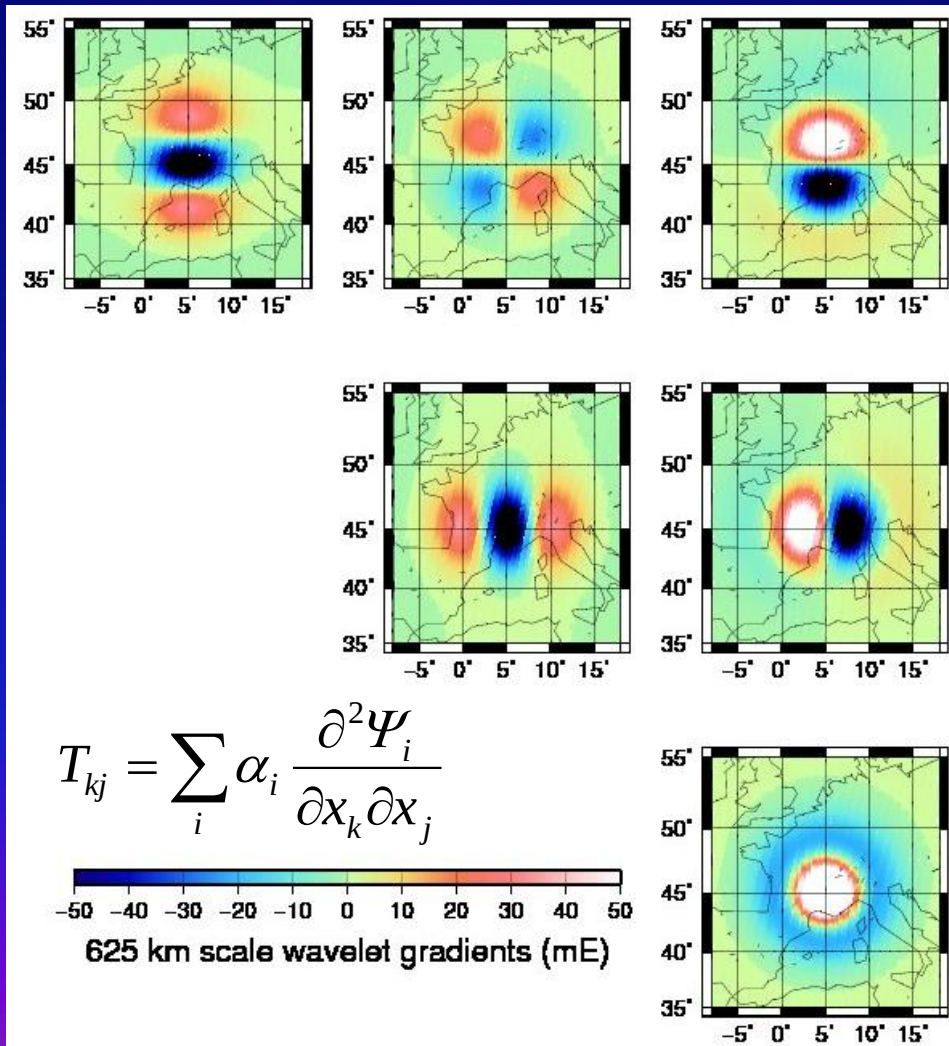
Regional multi-scale models



• Local densification **embedded in regional** and global models ?

• How to build a model over a wide area **block by block** ? How to « patch » local densifications ?

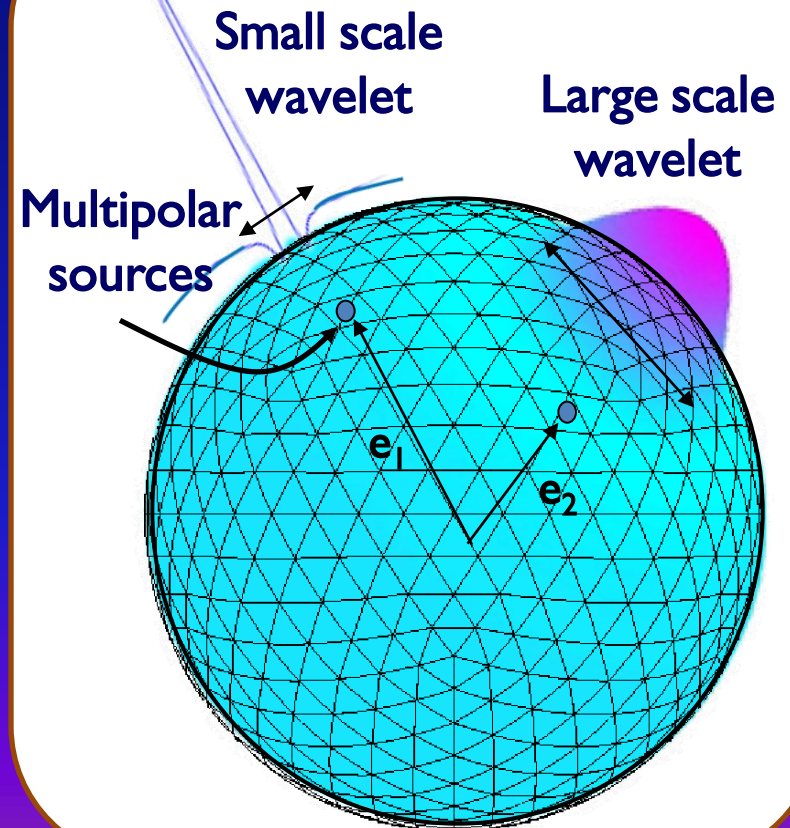
The wavelets and their gradients



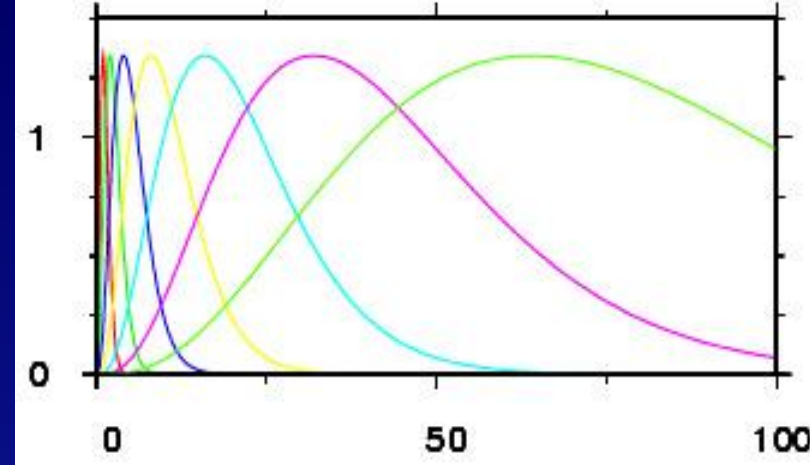
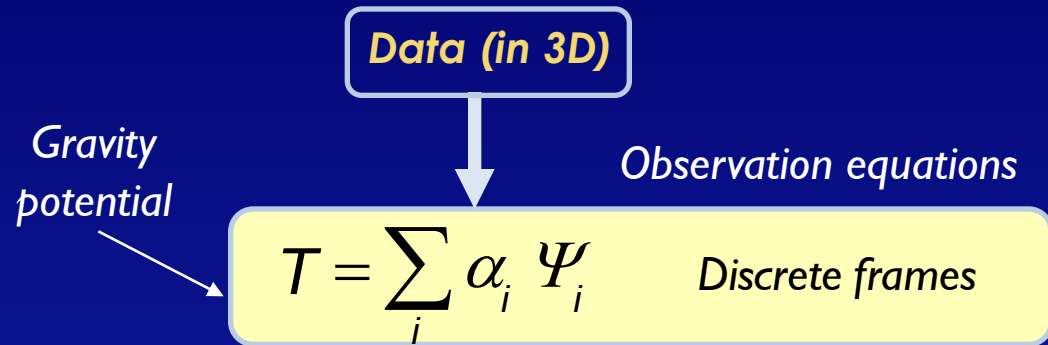
Analytical computation of the derivatives

Equivalent sources

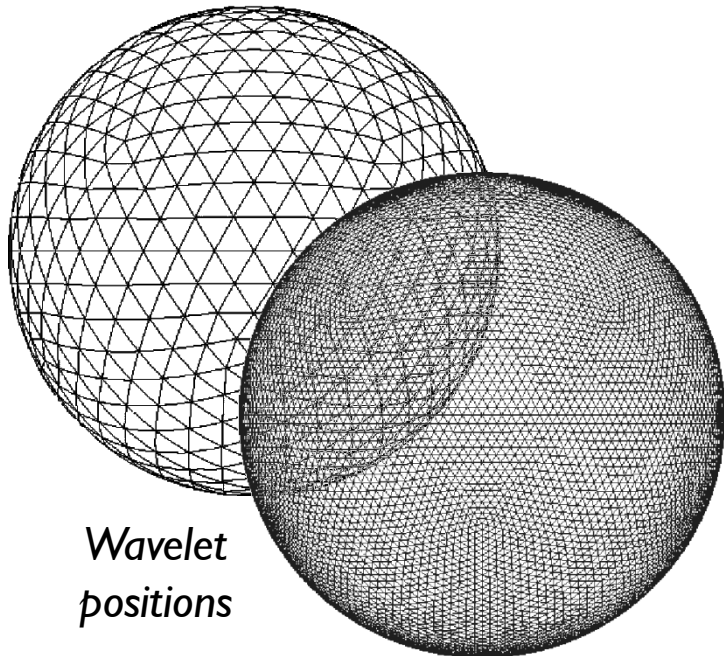
(Poisson multipoles)



Building the model



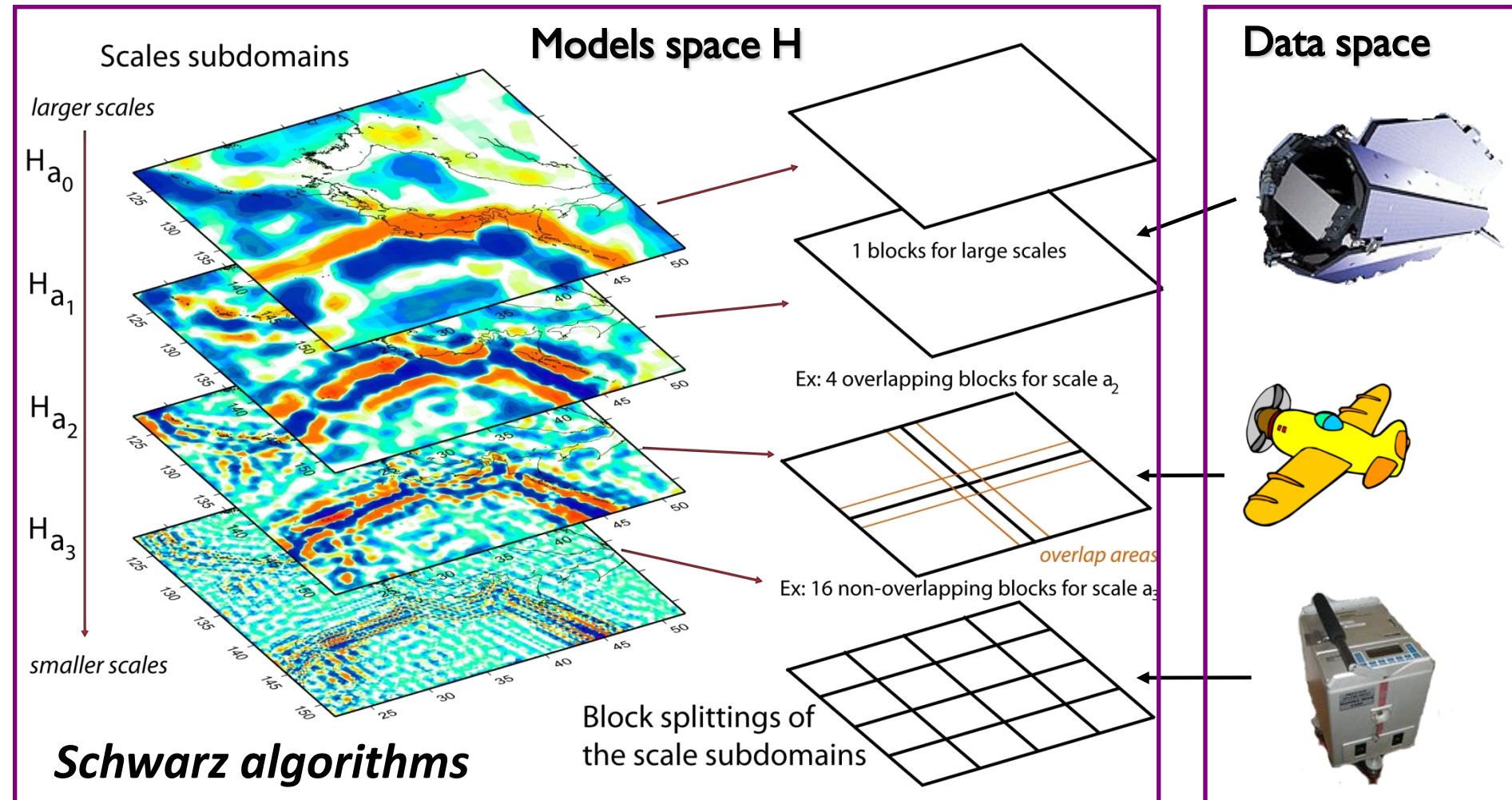
Wavelet spectra as a function of S.H. degree, for different scales.



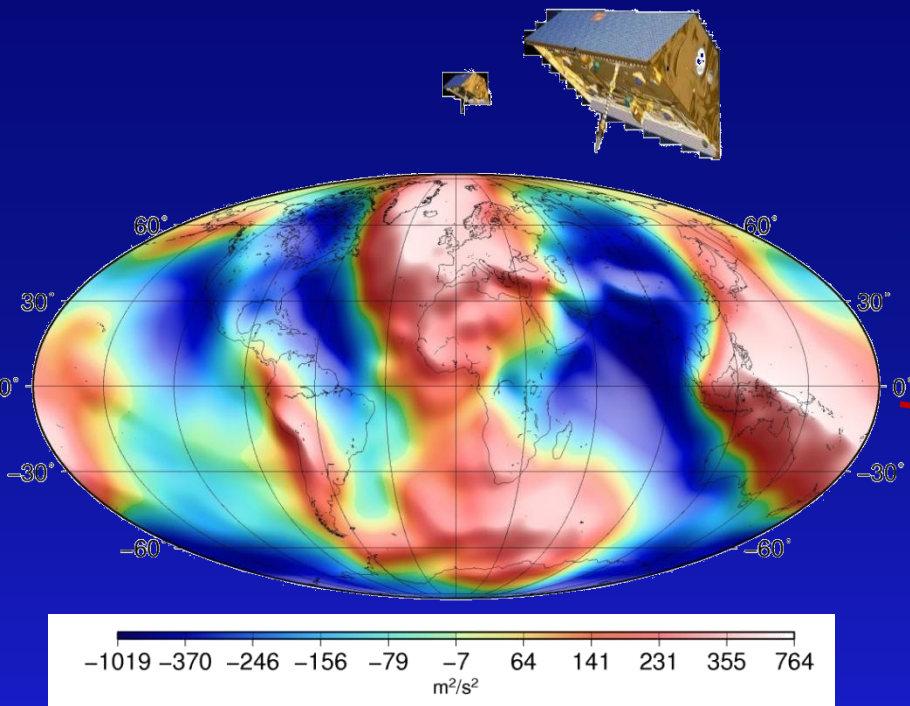
- A discrete wavelet frame representation of T is built by an appropriate discretisation of a continuous wavelet transform (CWT) in scale and space.
- The least-squares adjustment of the data allows to get the wavelet coefficients α .

Domain decomposition method

- Sequential scale iterations & for a given scale: parallel block iterations.
- Larger number of blocks at smaller scales.

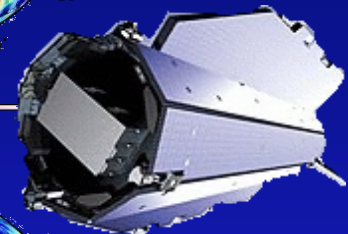
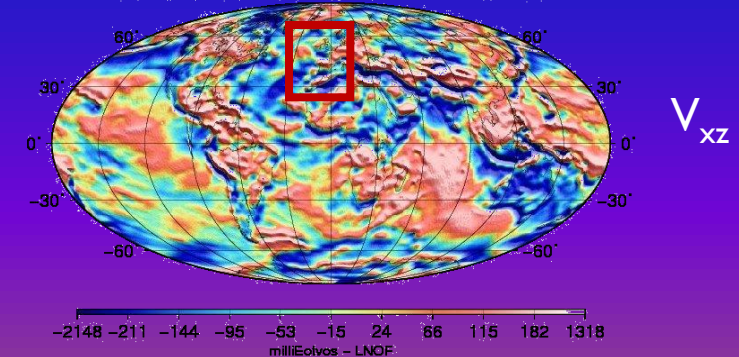
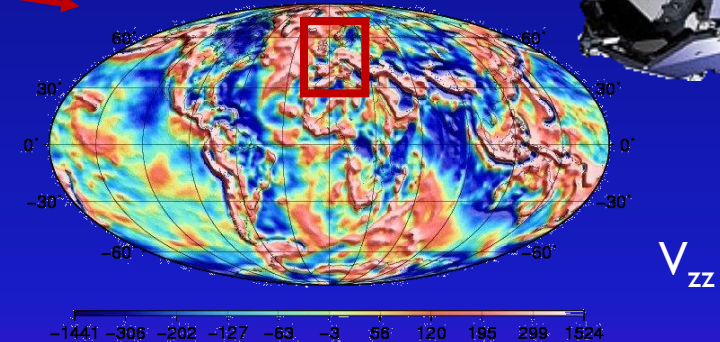
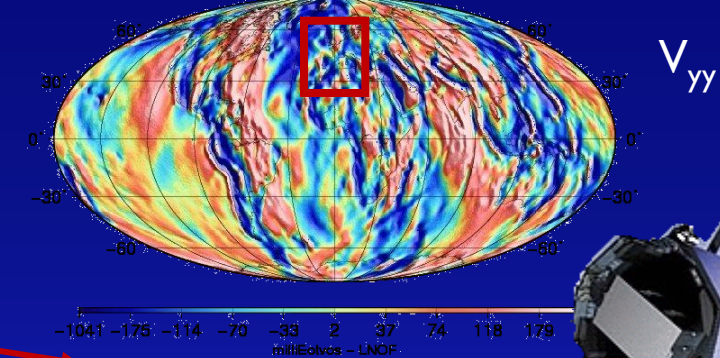
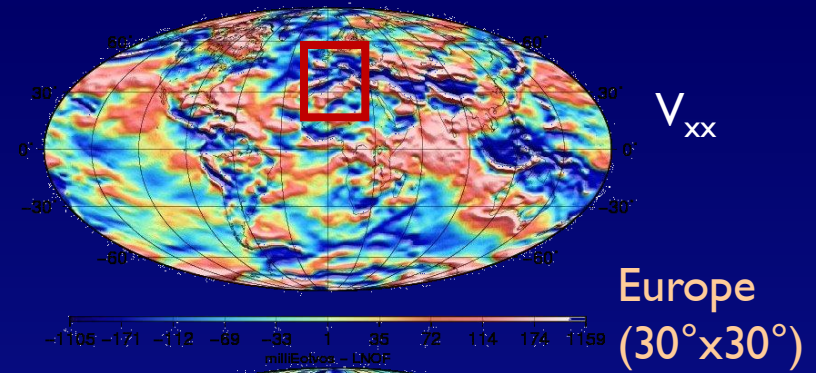


Data & models

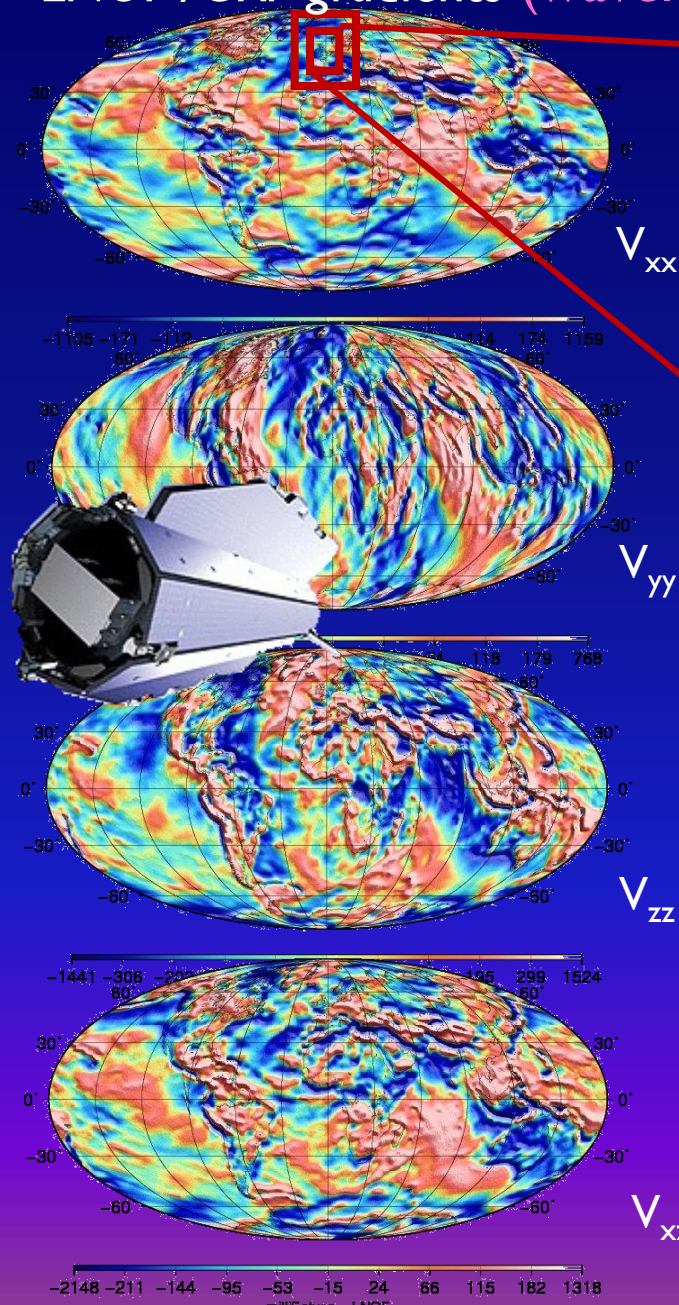


Global scale (down to 1250 km) - *GRACE*
model (SH)

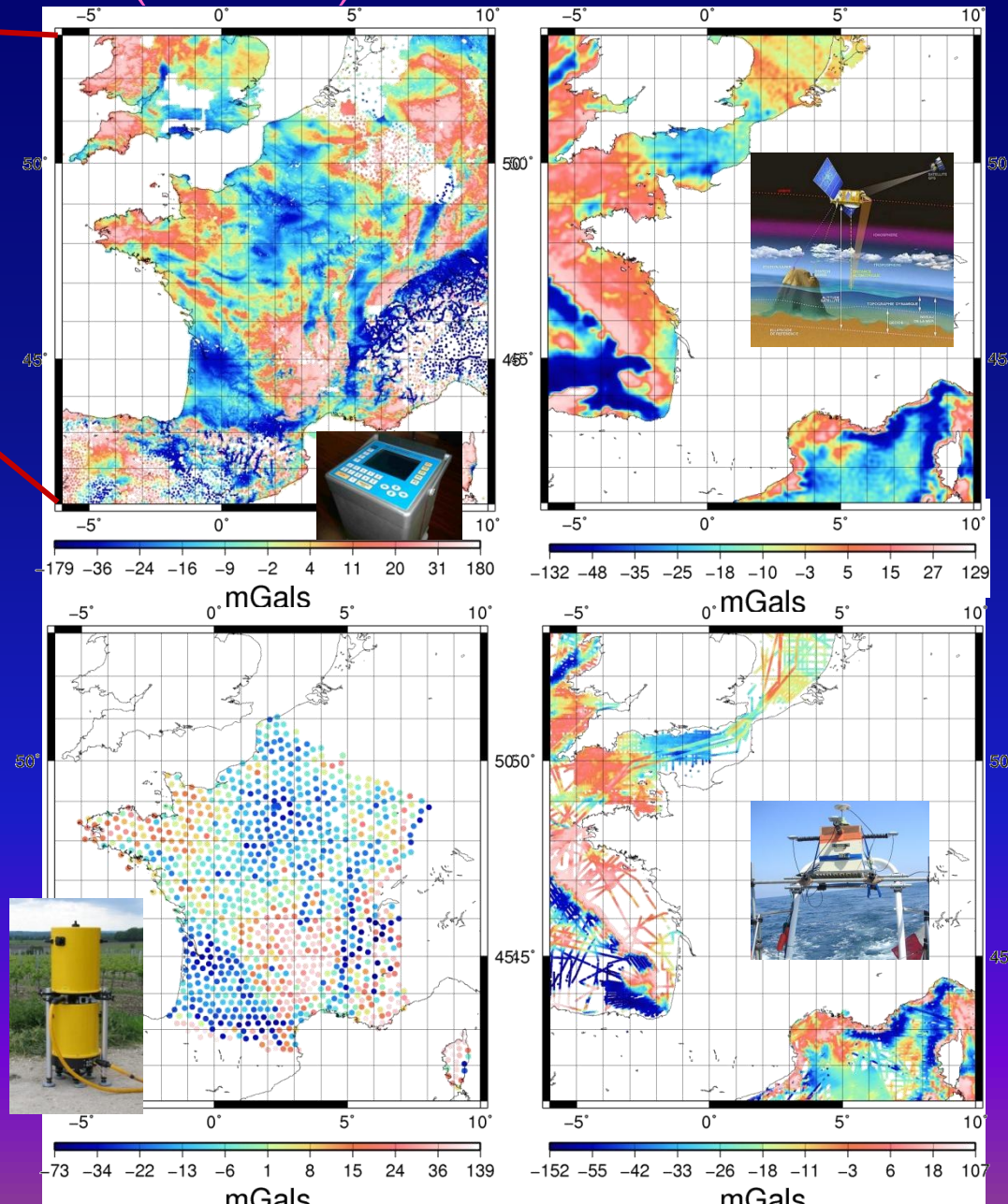
Medium scale (625 – 80 km) - *GOCE*
LNOF/GRF gradients (wavelets)



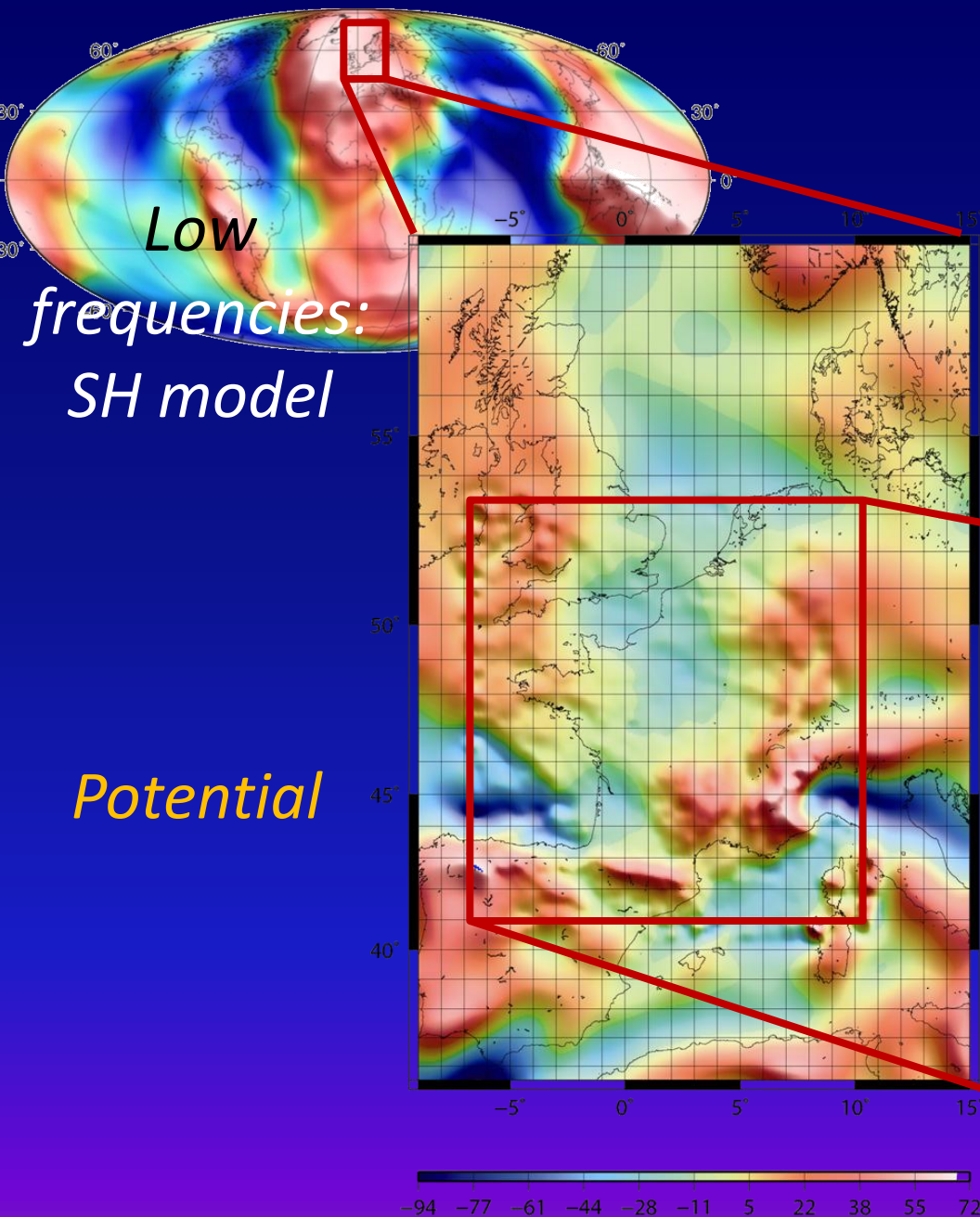
Medium scale (625 – 80 km) - GOCE
LNOF /GRF gradients (wavelets)



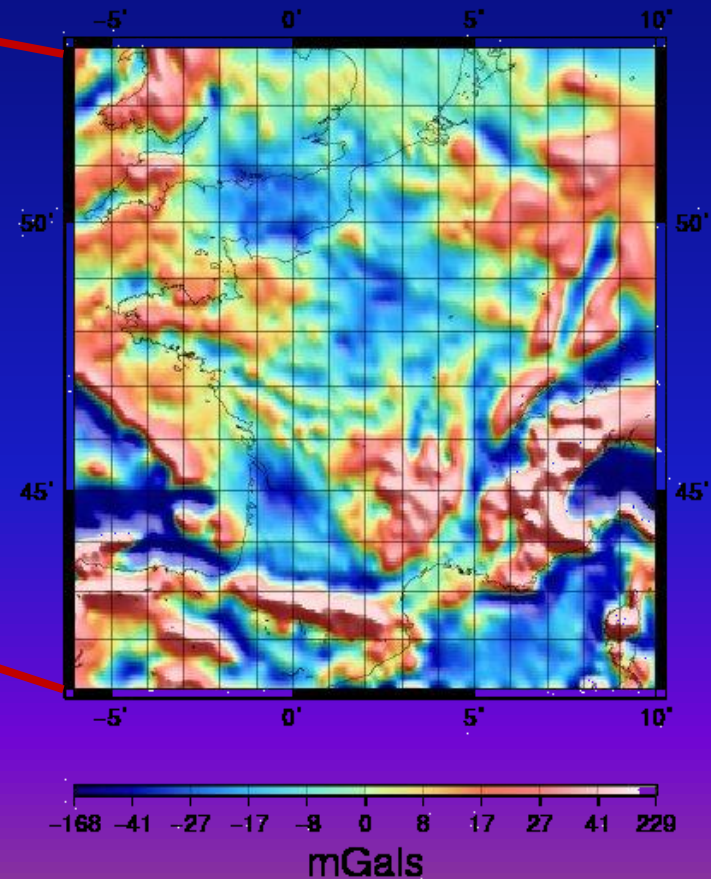
Small scales (200 – 20 km) – Surface data
(wavelets)



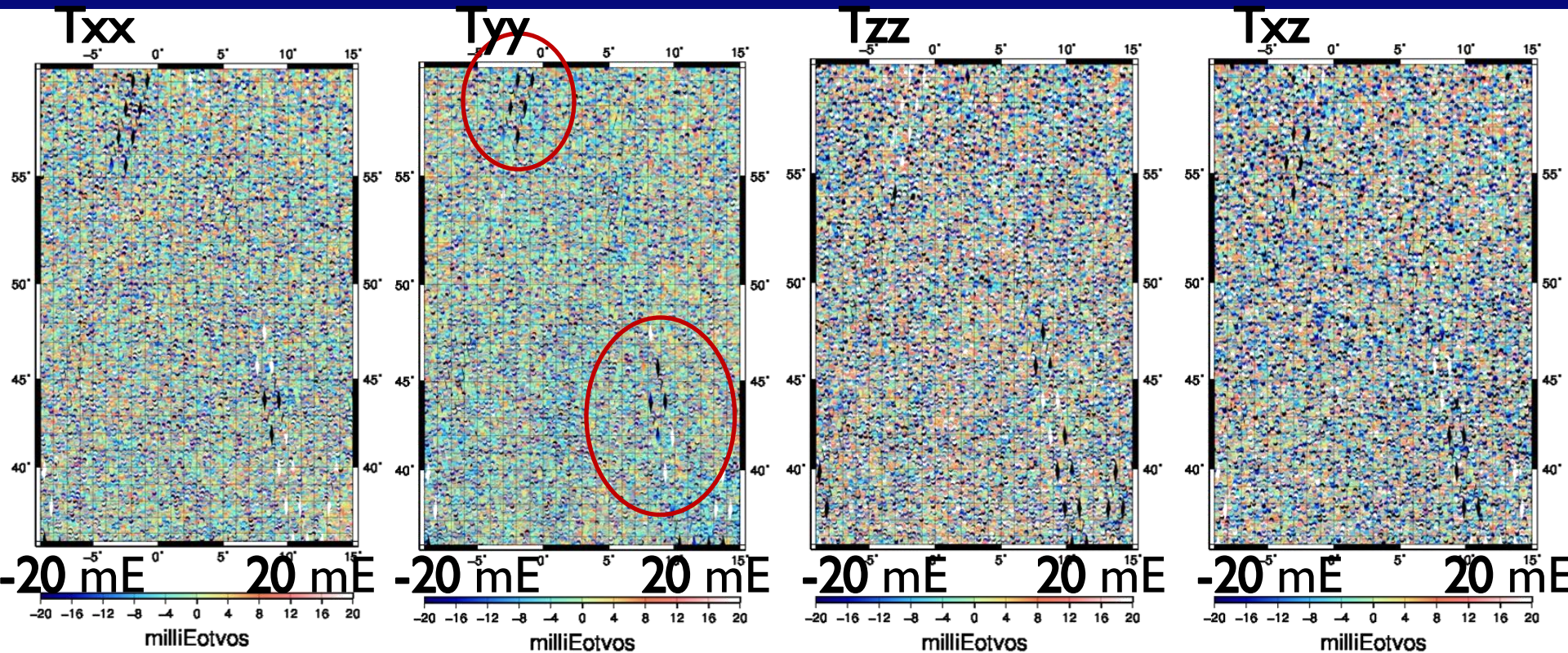
The model



Free-air anomalies
35 km resolution



Residuals to the LNOF gradients



rms: 11.6 mE

12.2 mE

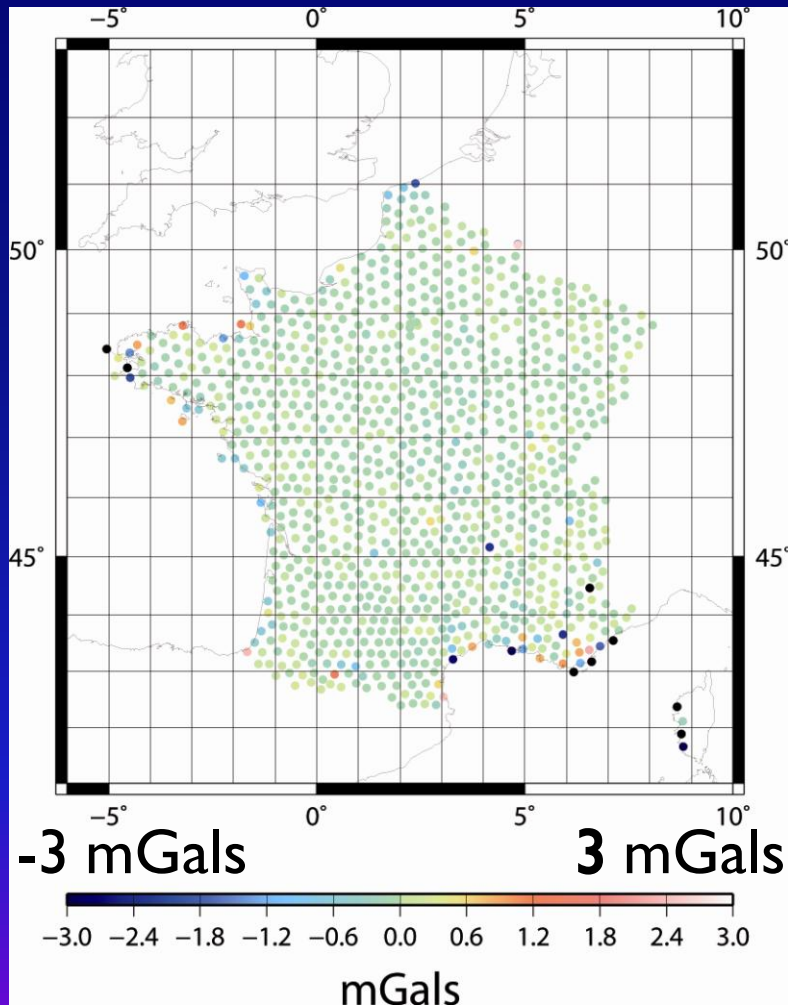
15.2 mE

13.9 mE

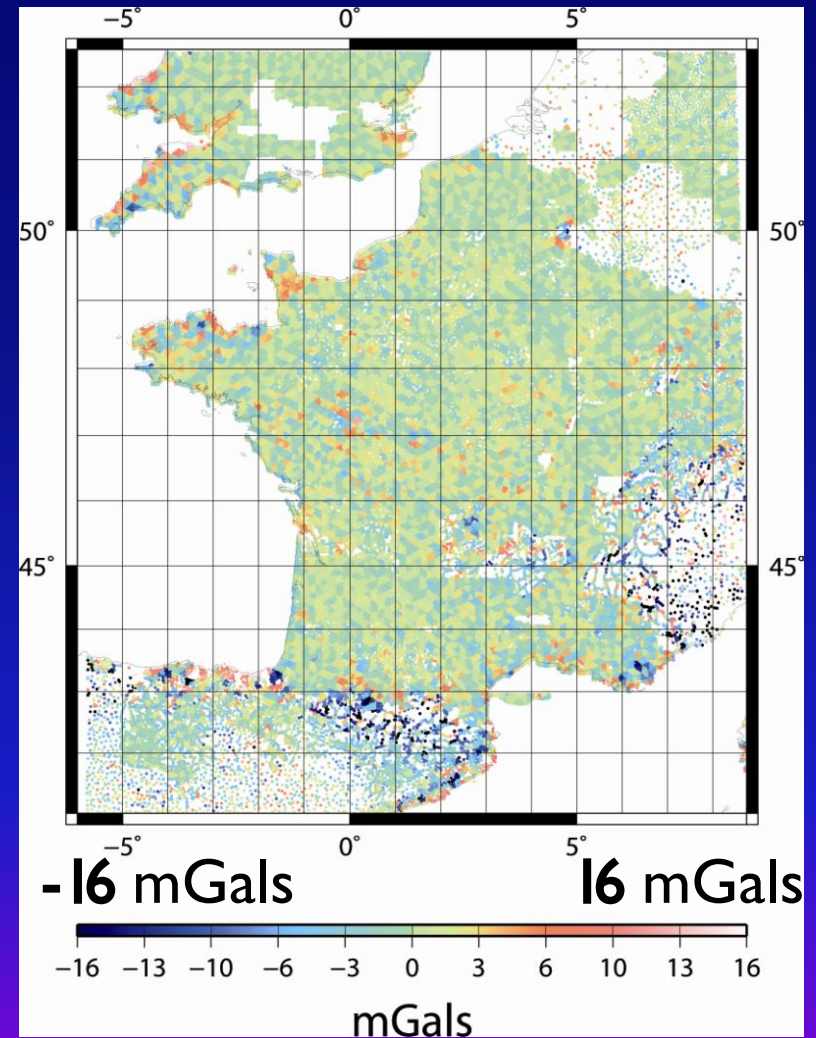
LNOF gradients from November 2009 to December 2010

Residuals to terrestrial gravity

35 km resolution



rms: 0.8 mGal

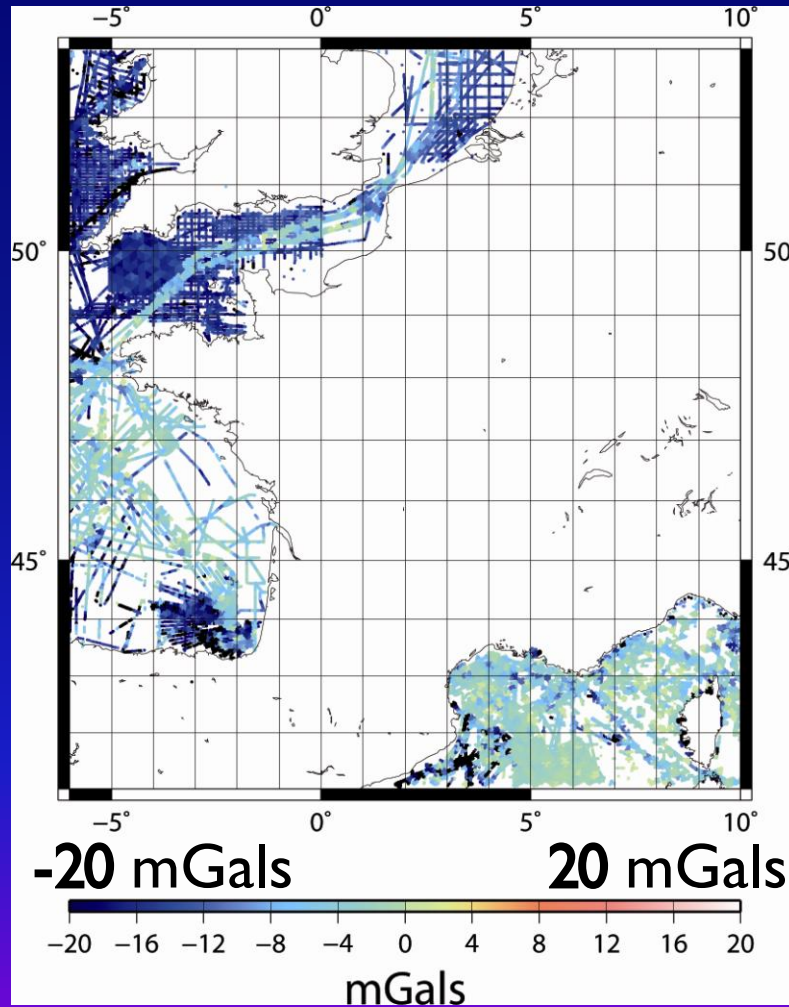


rms: 2,4 mGal

Residual terrain corrections applied for scales < 35 km.

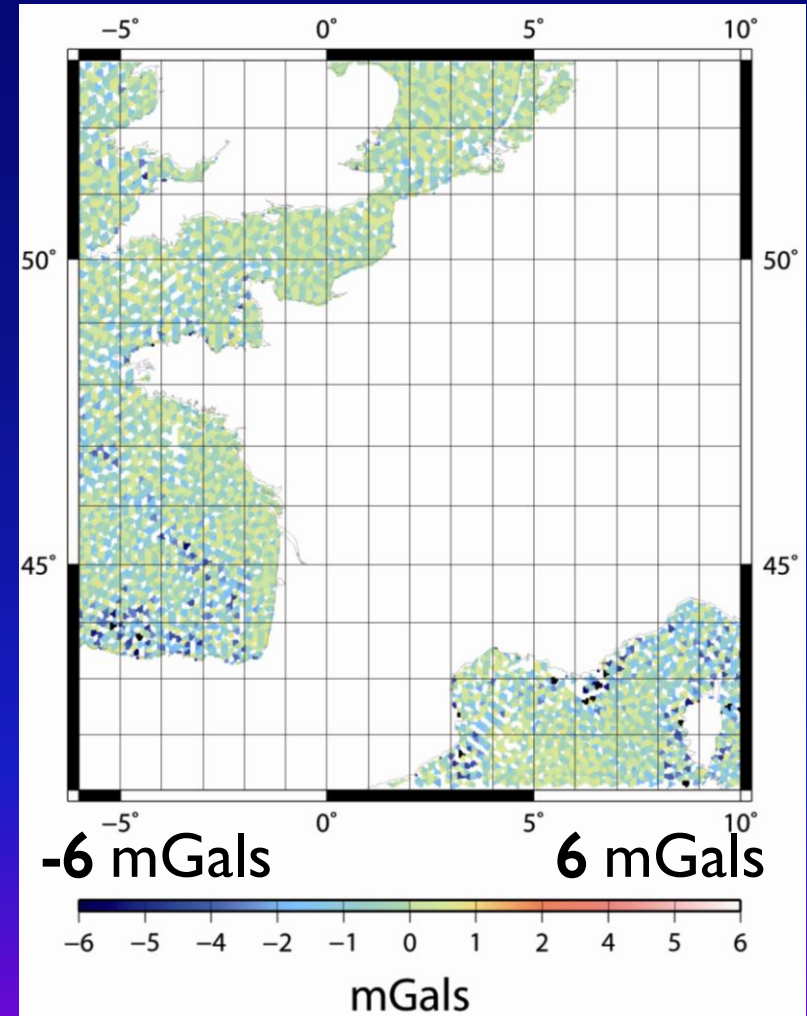
Residuals to ship & altimetry data

35 km resolution



rms: 6 mGal

bias: -2,4 mGal



rms : 1,5 mGal

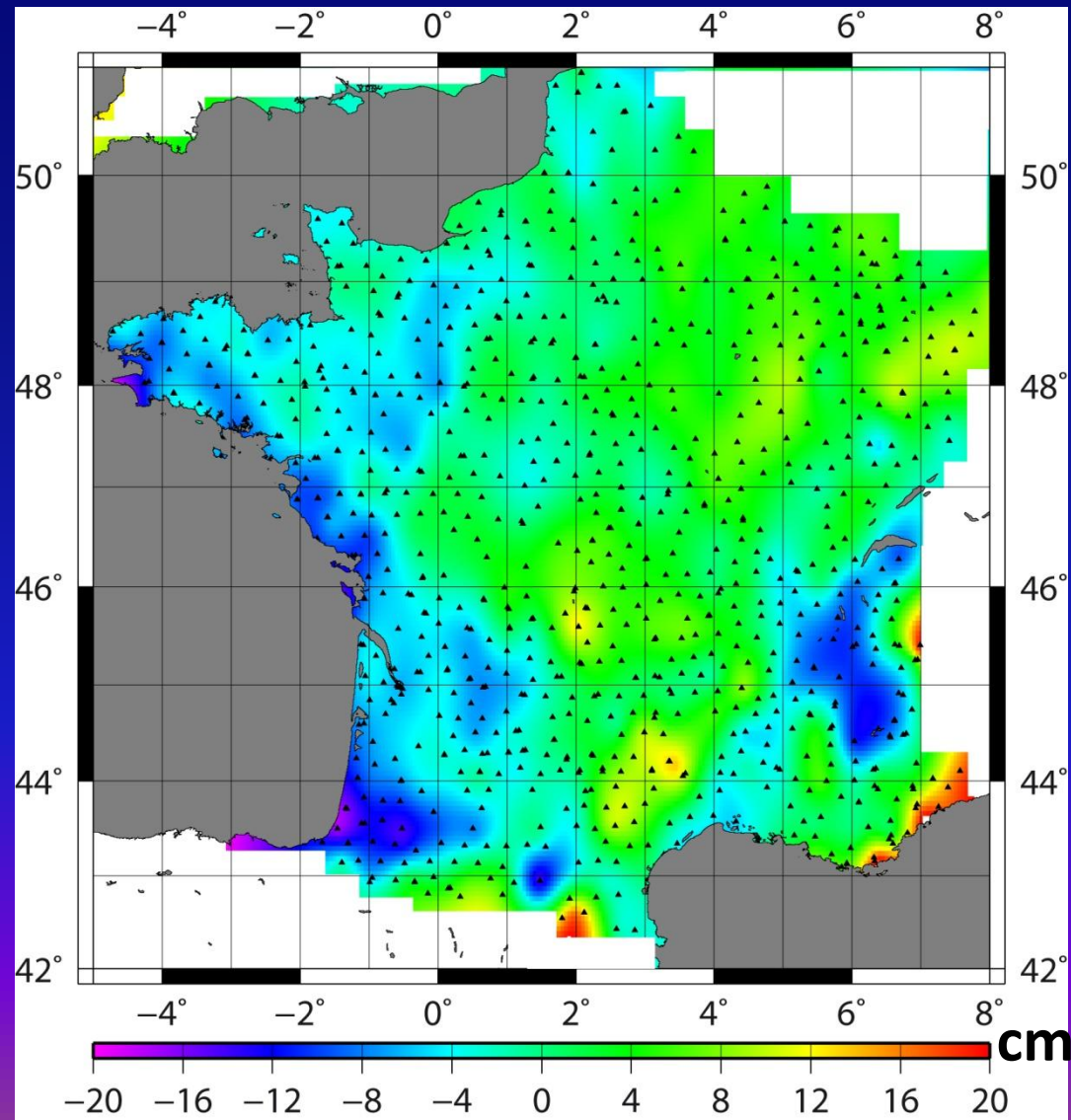
Comparison with GPS/levelling height anomalies

Differences on height anomalies:

- From the wavelet / SH model,
- From GPS & levelling.

Omission error reduced
in the 35-9 km scale band
using EGM2008.

rms = 7.3 cm

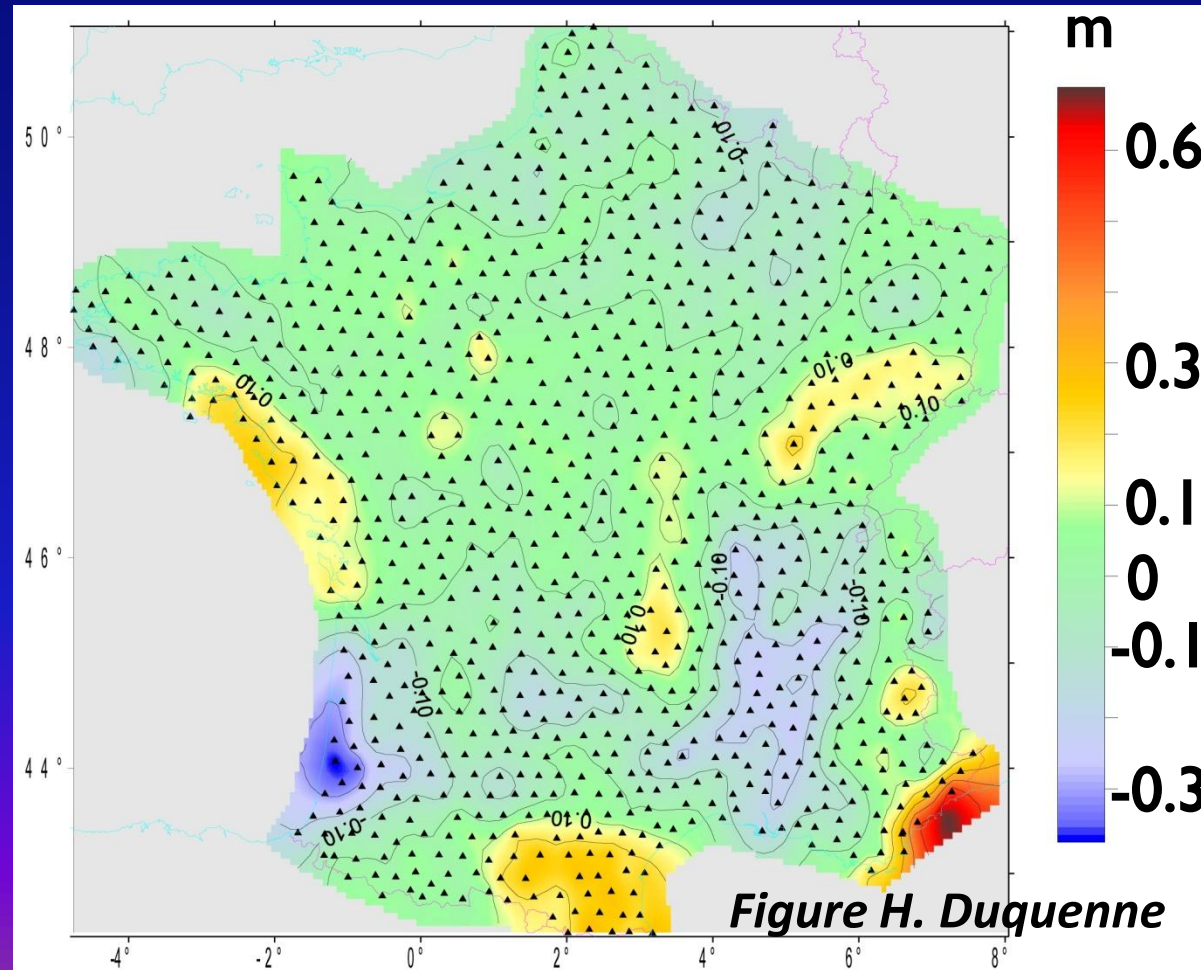


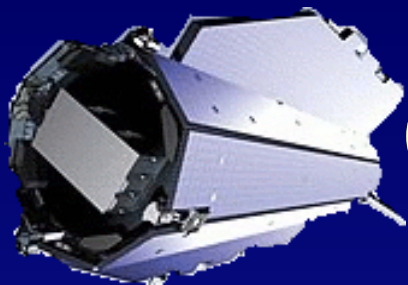
Comparison with GPS/levelling height anomalies

Case of the previous
quasi-geoid model
computed over France,
QGF98 (Duquenne, 1998):

rms = 10.9 cm

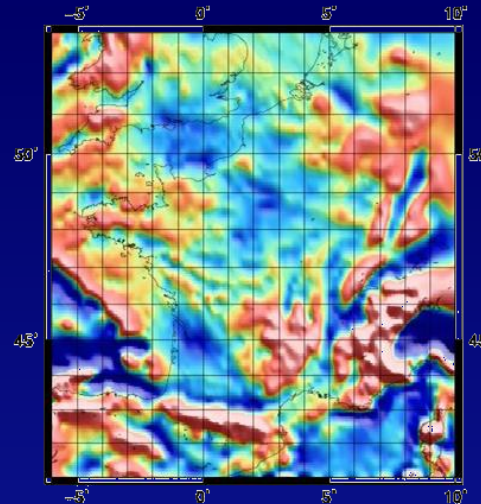
- Improvement of the
available gravity data
- Validation of the
results





Conclusion & outlook

→ A flexible method to combine the GOCE gradients with surface data.



Local models embedded in regional ones

→ The domain decomposition approach allows to handle wide areas by blocks. The block size is related to the scale.

→ We obtain a 35 km resolution model around France.

→ *Understand discrepancies to GPS/levelling on the Atlantic coast*

→ *Increase spatial resolution*