



Technical University  
of Moldova

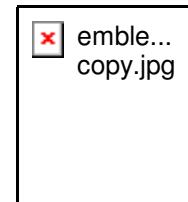
University of  
Applied Science



# Development of new geodetic infrastructure in Republic of Moldova

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- **Introduction**

Preconditions for new geodetic infrastructure development. Development of GNSS Permanent Network and MODPOS services

- **Geodetic databases development**

RTCM-based Positioning GNSS-Services. MOLDPOS architecture and communication configuration. Reference Datum Transformation. Height Reference Transformation. Testing out of geodetic databases

- **Generation of RTCM 3.1 Transformation messages**

Gridding for transformation messages. Structure of RTCM 3.1 messages

- **GNSS-Positioning Services Applications**

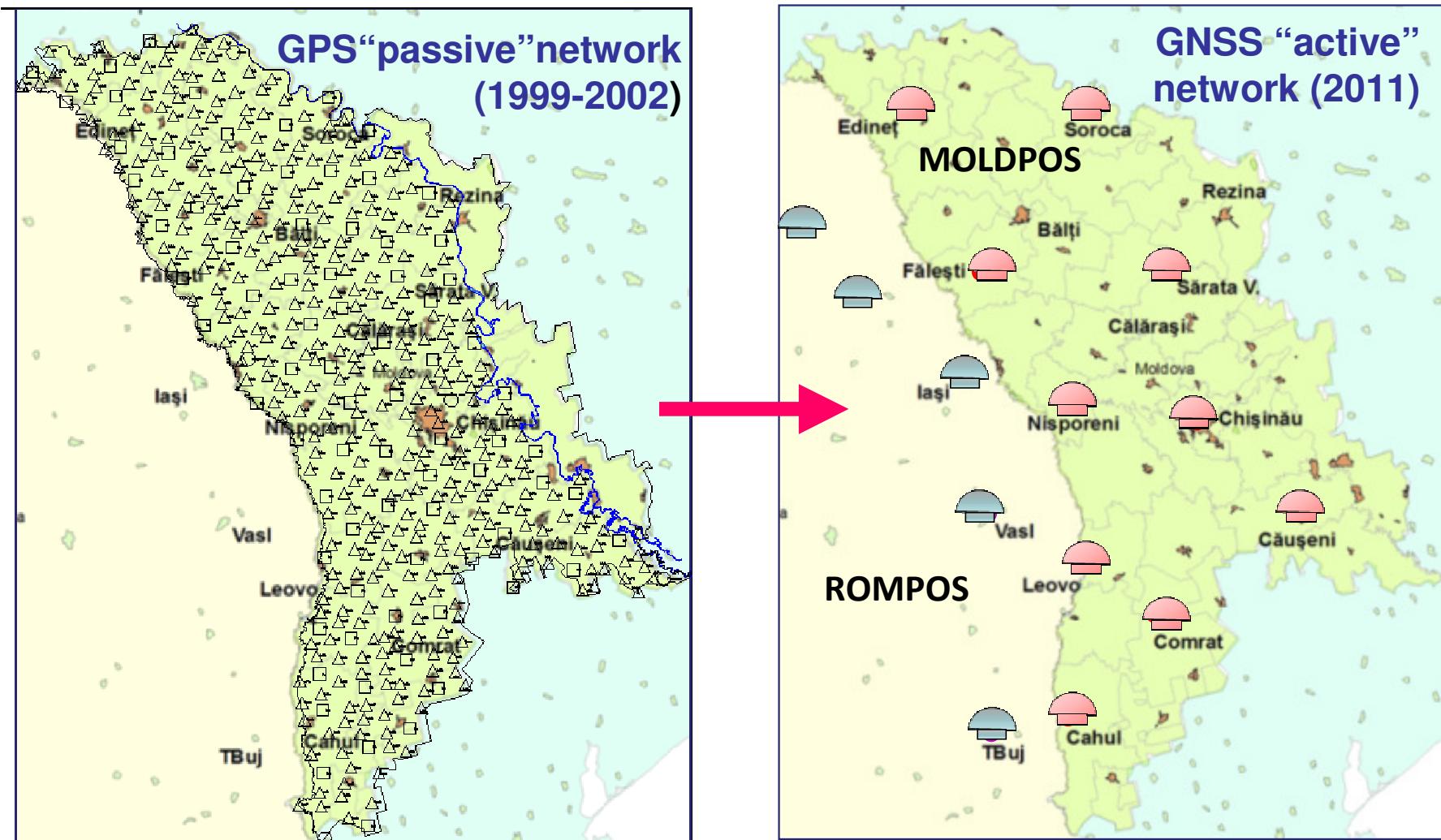
GNSS-Positioning Services – User-Groups. GNSS-based and Multisensor Low-Cost Platforms for Navigation and Object-Georeferencing. Growth of GNSS-Positioning Services User-Groups

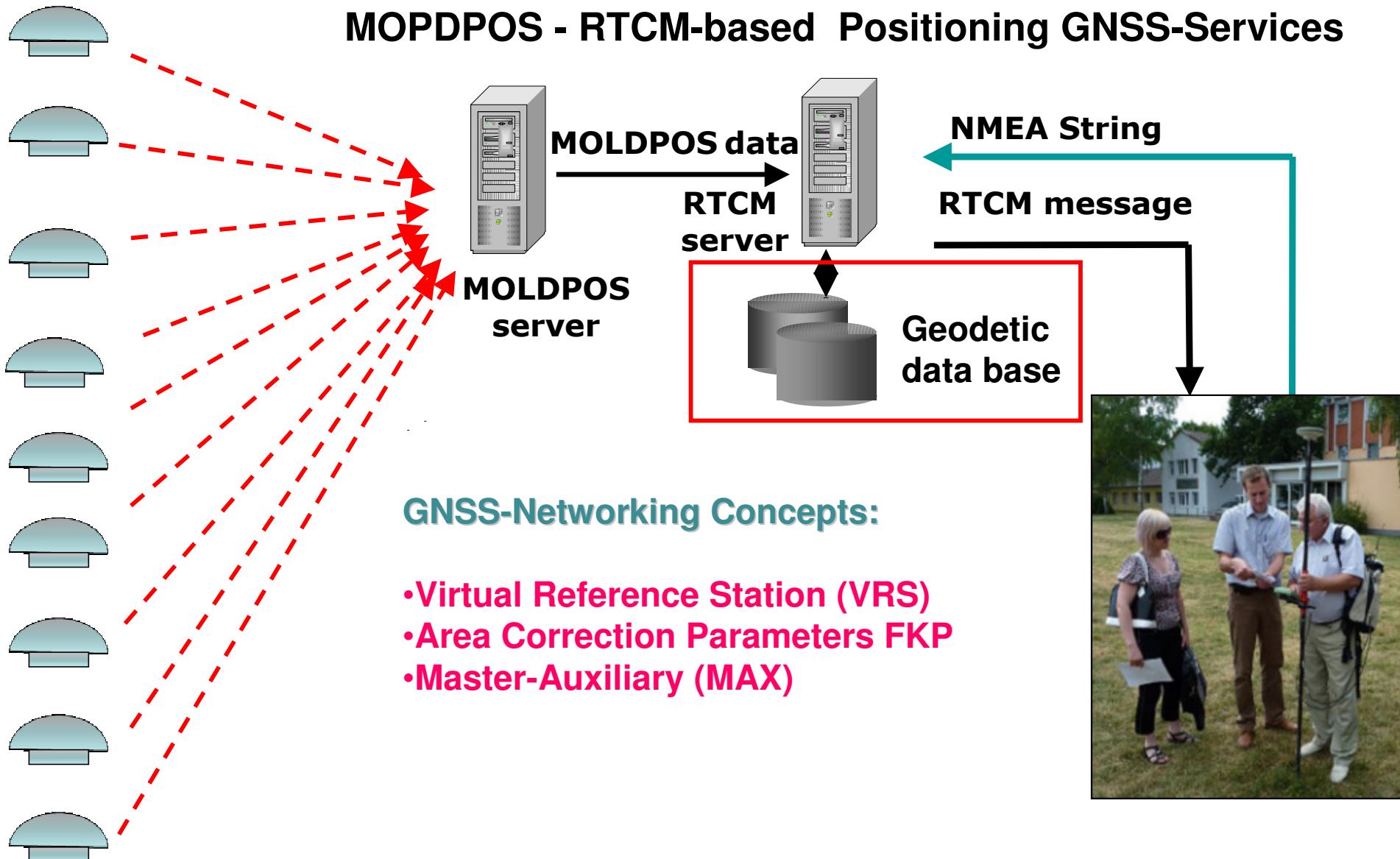
- **Conclusions**

## Preconditions for new geodetic infrastructure development

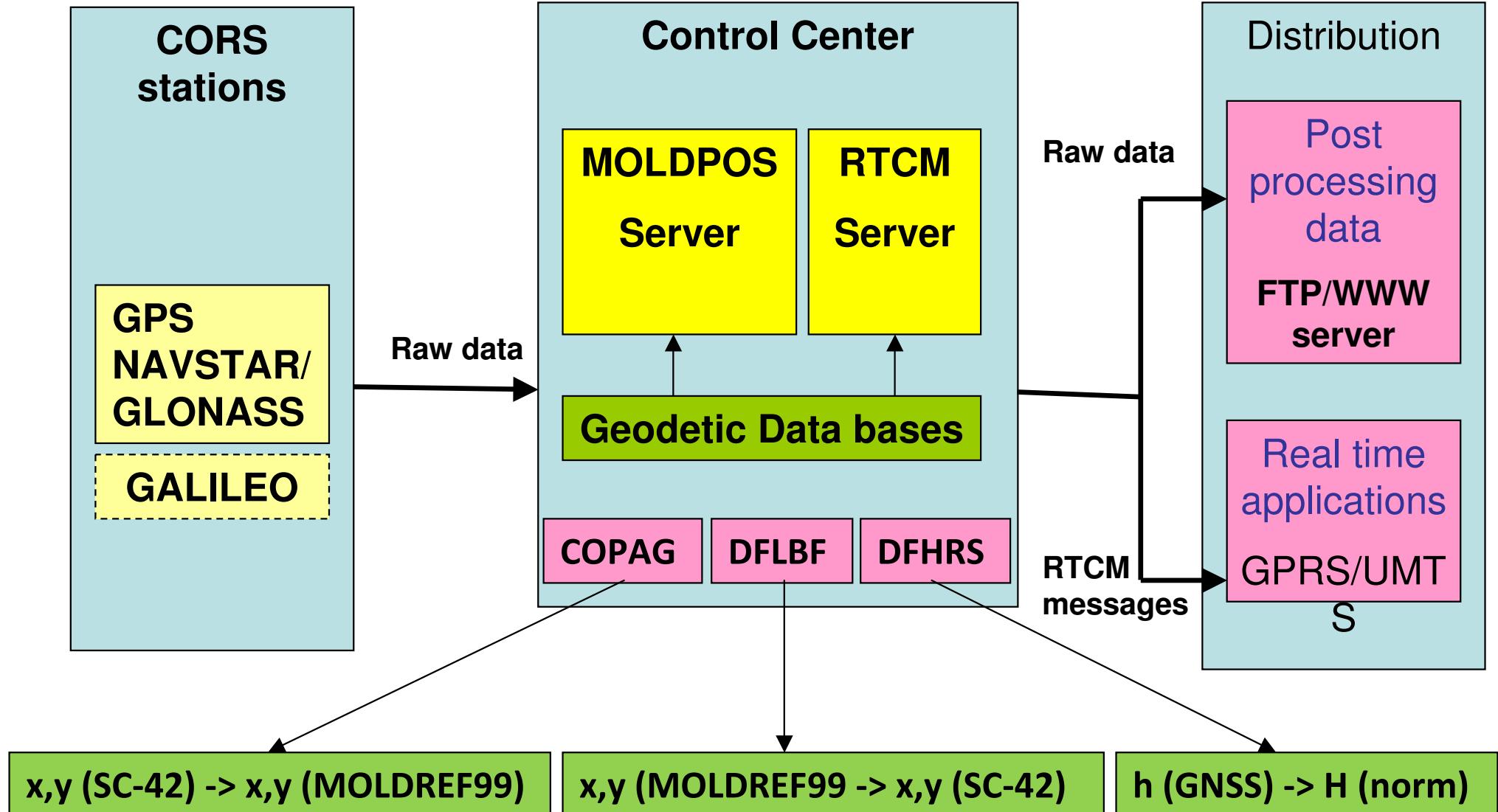
- Development of new Moldavian Reference System MOLDREF99 and Transversal Mercator for Moldova (TMM) Map Projection (1999)
- Creation of the National Geodetic Network (1999-2002) and National Gravity Network (2006-)
- Reconstruction of National Leveling Network and future integration in ULEN (2002-)
- Installation of first permanent GNSS reference station at Technical University of Moldova in the frame of educational project JEP-24243-2003, TACIS-TEMPUS (2006)
- Installation and maintenance of IGEO (Chisinau) EPN permanent GNSS reference station by the Agency of Land Relations and Cadastre in collaboration with BKG (2007)

# **Development of GNSS Permanent Network and MOLDPOS service (Government decision Nr. 307 from 28.04.2011)**

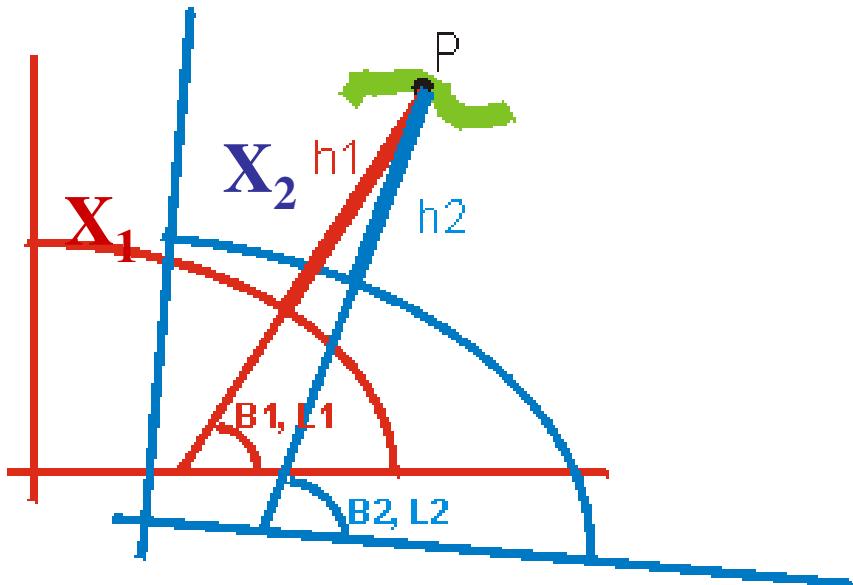




## MOLDPOS architecture and communication configuration



## Reference Datum Transformation



$$X = (N + h) \cdot \cos B \cdot \cos L$$

$$Y = (N + h) \cdot \sin B \cdot \sin L$$

$$Z = (N - Ne^2 + h) \cdot \sin B$$

**3D Transformation**

$$\begin{bmatrix} X_2(B_2, L_2, h_2) \\ Y_2(B_2, L_2, h_2) \\ Z_2(B_2, L_2, h_2) \end{bmatrix} = s \cdot R \cdot \begin{bmatrix} X_1(B_1, L_1, h_1) \\ Y_1(B_1, L_1, h_1) \\ Z_1(B_1, L_1, h_1) \end{bmatrix} + t$$

## Reference Datum Transformation

### Karlsruhe Solution

$$\begin{bmatrix} B \\ L \\ h \end{bmatrix}_2 - \begin{bmatrix} \Delta B_{(a,b)_1,(a,b)_2} \\ \Delta L_{(a,b)_1,(a,b)_2} \\ \Delta h_{(a,b)_1,(a,b)_2} \end{bmatrix} - \begin{bmatrix} B \\ L \\ h \end{bmatrix}_1 + \begin{bmatrix} v_B \\ v_L \\ v_h \end{bmatrix}_i = [Molodensky]_{(B,L,h)_1,i} .$$

were ellipsoid transition corrections are:

$$\begin{bmatrix} \Delta B_{(a,b)_1,(a,b)_2} = B(a,b)_2 |(X,Y,Z)_1) - B(a,b)_1 |(X,Y,Z)_1) \\ \Delta L_{(a,b)_1,(a,b)_2} = 0 \\ \Delta h_{(a,b)_1,(a,b)_2} = h(a,b)_2 |(X,Y,Z)_1) - h(a,b)_1 |(X,Y,Z)_1) \end{bmatrix}$$

$$\begin{bmatrix} \varepsilon_x \\ \varepsilon_y \\ \varepsilon_z \\ \Delta s \\ t_x \\ t_y \\ t_z \end{bmatrix}$$



Wtrans.lnk

1D-,2D-,3D-

Identical Points

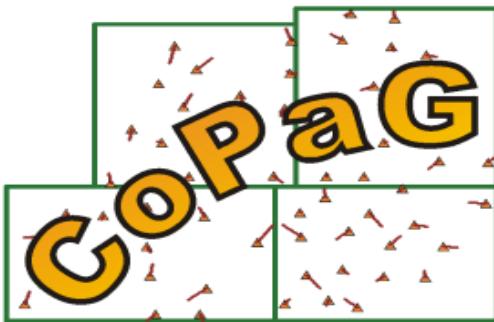
**WTRANS**

[www.geozilla.de](http://www.geozilla.de)



$-\sin(L) \cdot \frac{a \cdot W + h}{M + h}$	$\cos(L) \cdot \frac{a \cdot W + h}{M + h}$	0	$-\sin(B) \cdot \cos(B) \cdot N \cdot e^2$	$-\sin(B) \cdot \cos(L)$	$-\sin(B) \cdot \sin(L)$	$\cos(B)$
$\sin(B) \cdot \cos(L) \cdot (N \cdot (1 - e^2) + h)$	$\sin(B) \cdot \sin(L) \cdot (N \cdot (1 - e^2) + h)$	-1	0	$-\sin(L)$	$\cos(L)$	0
$(N + h) \cdot \cos(B)$	$(N + h) \cdot \cos(B)$	0	$h + a \cdot W$	$\cos(B) \cdot \cos(L)$	$\cos(B) \cdot \sin(L)$	$\sin(B)$

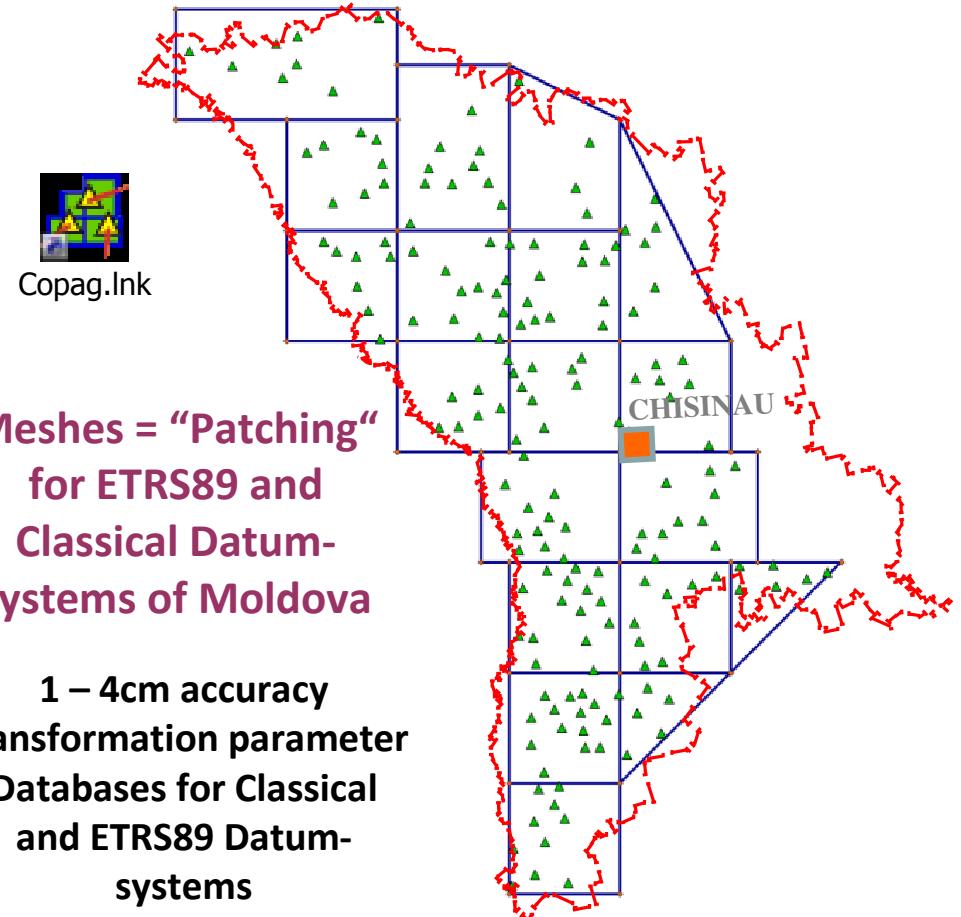
## Reference Datum Transformation



COPAG =  
Continuously  
Patched  
Georeferencing  
**Continuity along the  
Mesh Borders!**

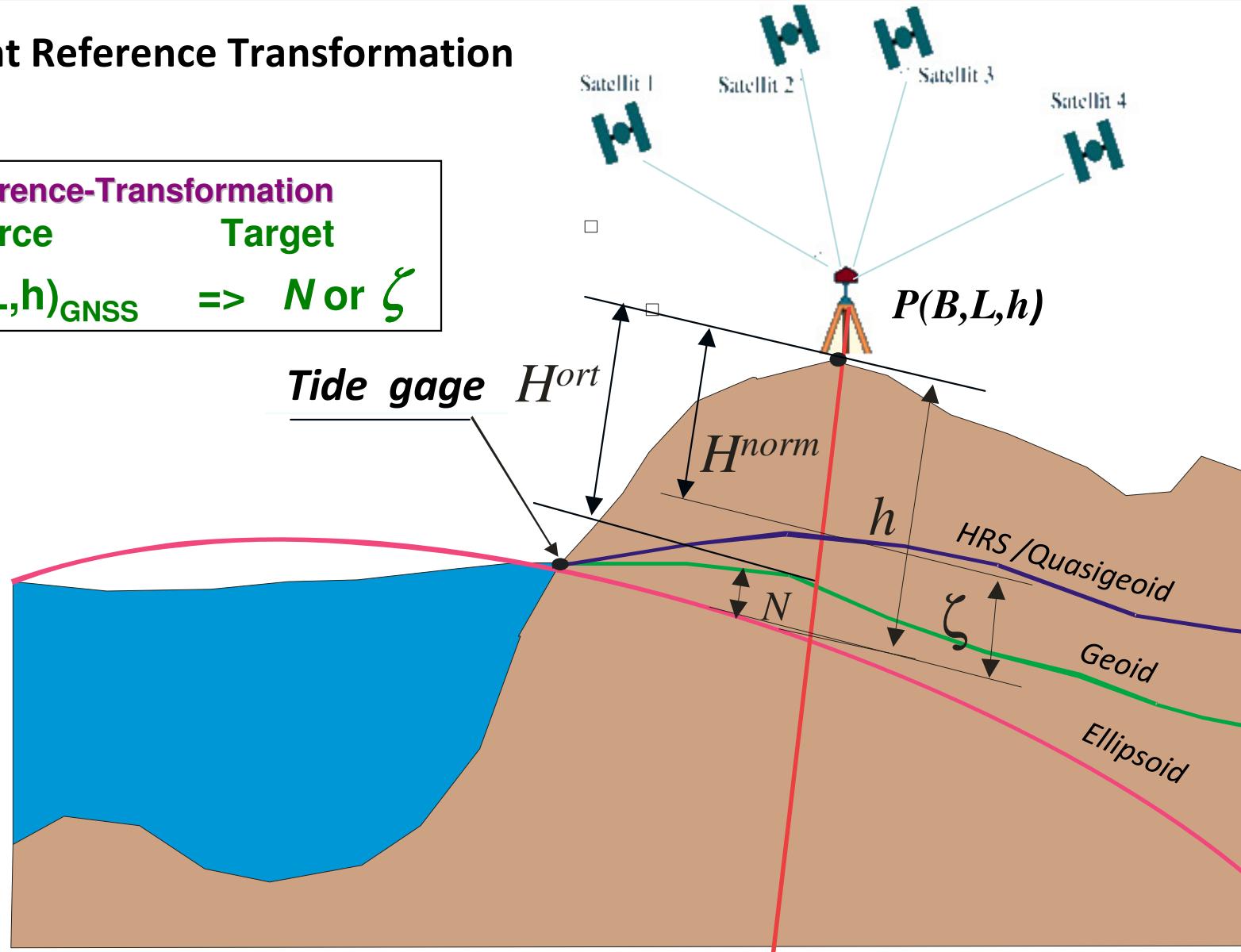


Combined Old Classical Triangulation and ETRS89  
Control Points from GNSS measurements



## Height Reference Transformation

Reference-Transformation	
Source	Target
$(B, L, h)_{GNSS}$	$\Rightarrow N \text{ or } \zeta$



## Height Reference Transformation

GNSS-heights and levelling heights

$$h_{\text{GNSS}} + v = H + \mathbf{f}^T \cdot \mathbf{p} - h_{\text{GNSS}} \Delta m$$

Existing Geoid Grids or Grids from GPM

$$N_G^j + v^j = \mathbf{f}^T \cdot \mathbf{p} + \partial N_G(\mathbf{d}^j)$$

Vertical Deflection components

$$\xi^j + v = -\mathbf{f}_B^T / M(B) \cdot \mathbf{p} + \partial \xi(\mathbf{d}_{\xi,\eta})^j$$

$$\eta^j + v = -\mathbf{f}_L^T / (N(B) \cdot \cos(B)) \cdot \mathbf{p} + \partial \eta(\mathbf{d}_{\xi,\eta})^j$$

Continuity Equations along the mesh borders

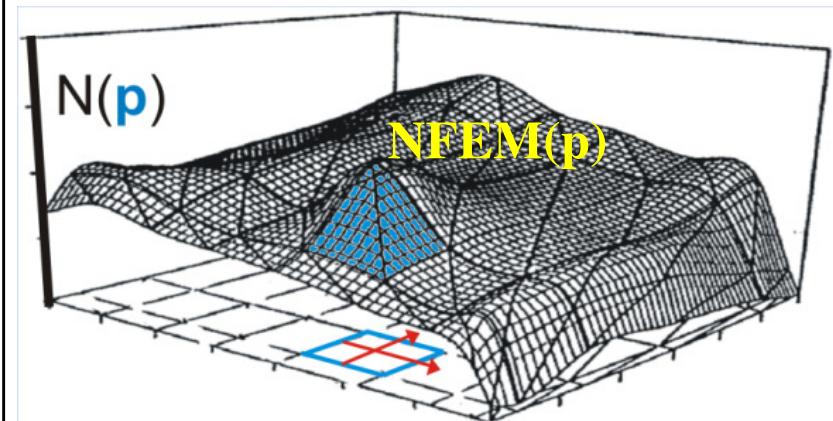
$$C + v = C(\mathbf{p})$$

Observation Equations for the mapping of the coefficients of Global Geopotential Models (e.g. EGM2008, EIGEN)

$$g_{\text{grav}} + v = \sum_{k=0}^{\infty} \left( \frac{a}{r} \right)^{n(k)+1} \frac{(n(k)+1)}{r} \sum_{m=0}^k (\bar{C}'_{n(k),m} \cdot \cos m\lambda' + \bar{S}'_{n(k),m} \cdot \sin m\lambda') \cdot P_{n(k),m}(\cos \theta') + dg(\mathbf{d})$$

$$N_{\text{GPM}}^j + v = \frac{1}{\gamma_Q} \left( \sum_{k=0}^{\infty} \left( \frac{a}{r} \right)^{n(k)+1} \sum_{m=0}^k (\bar{C}'_{n(k),m} \cdot \cos m\lambda' + \bar{S}'_{n(k),m} \cdot \sin m\lambda') \cdot P_{n(k),m}(\cos \theta') - V_{\text{ref}} \right) + \partial N(\mathbf{d}^j)$$

Karlsruhe Solution for Digital Finite Element Height reference surface representation as polynomial



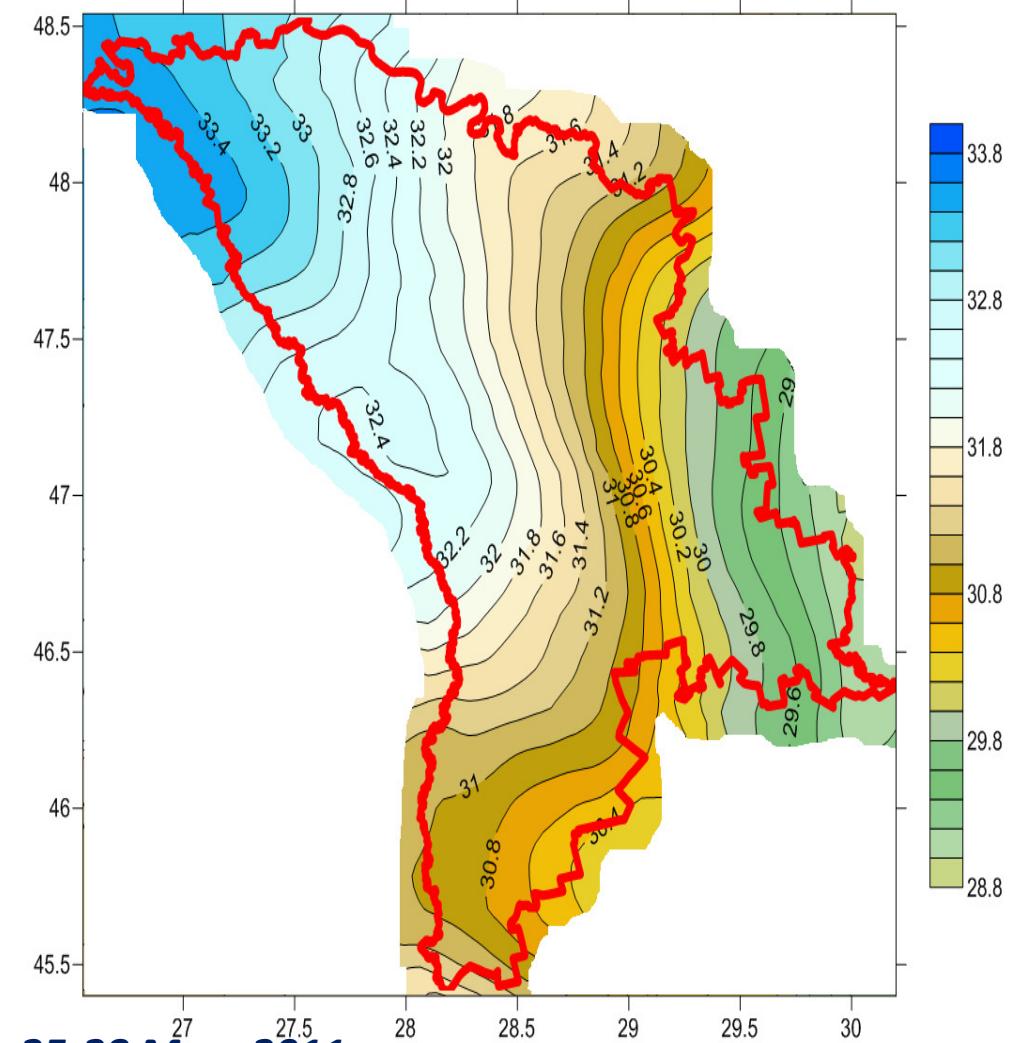
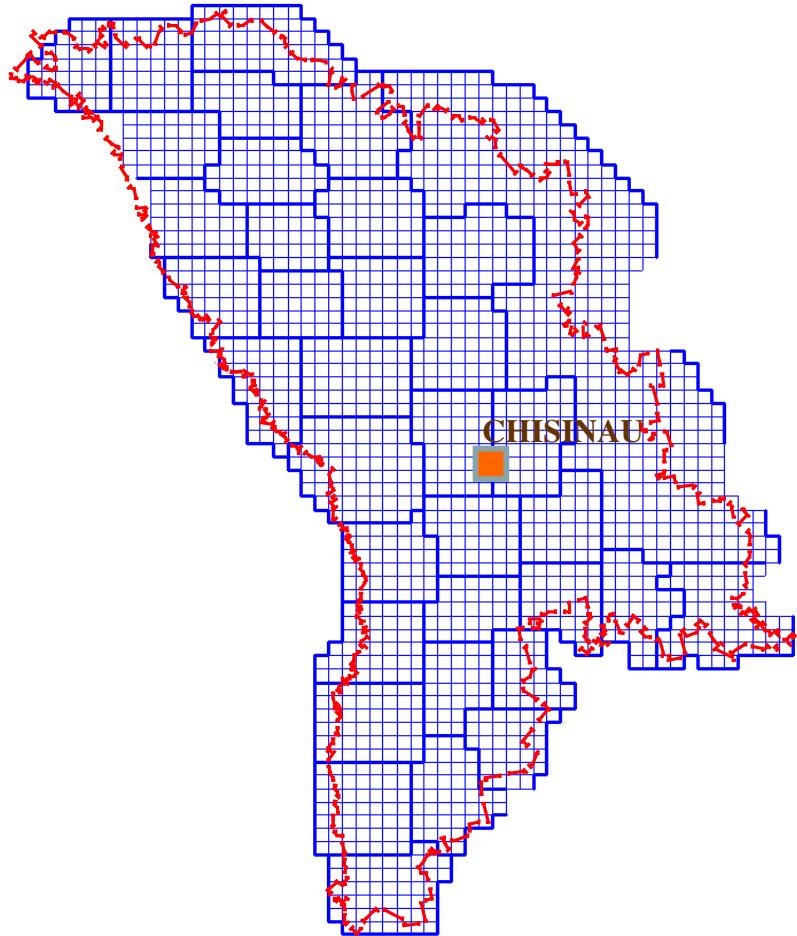
$$\text{NFEM}(\hat{\mathbf{p}} | B, L) = \mathbf{f}^T \cdot \hat{\mathbf{p}}$$

$$\mathbf{f}(B, L) = [1 | B, L | B^2, B \cdot L, L^2 | \dots]^T$$

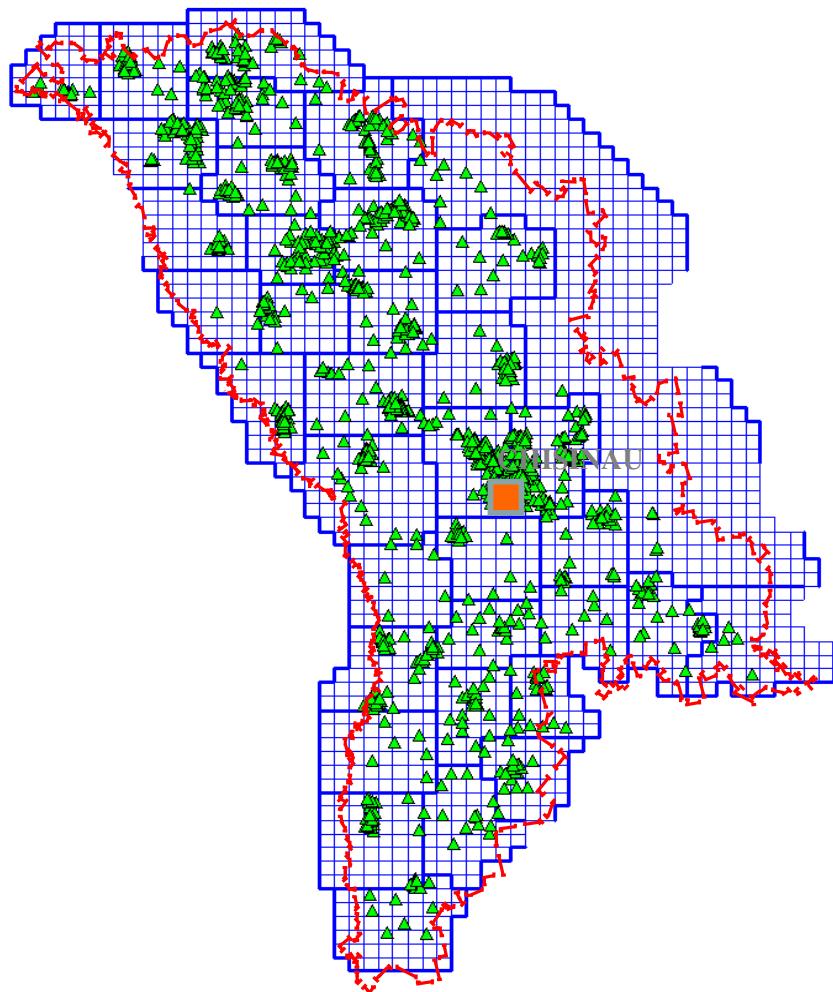
$$\hat{\mathbf{p}} = [\hat{p}_{00} | \hat{p}_{10}, \hat{p}_{01} | \hat{p}_{20}, \hat{p}_{11}, \hat{p}_{02} | \dots]^T$$

## Testing out of geodetic databases

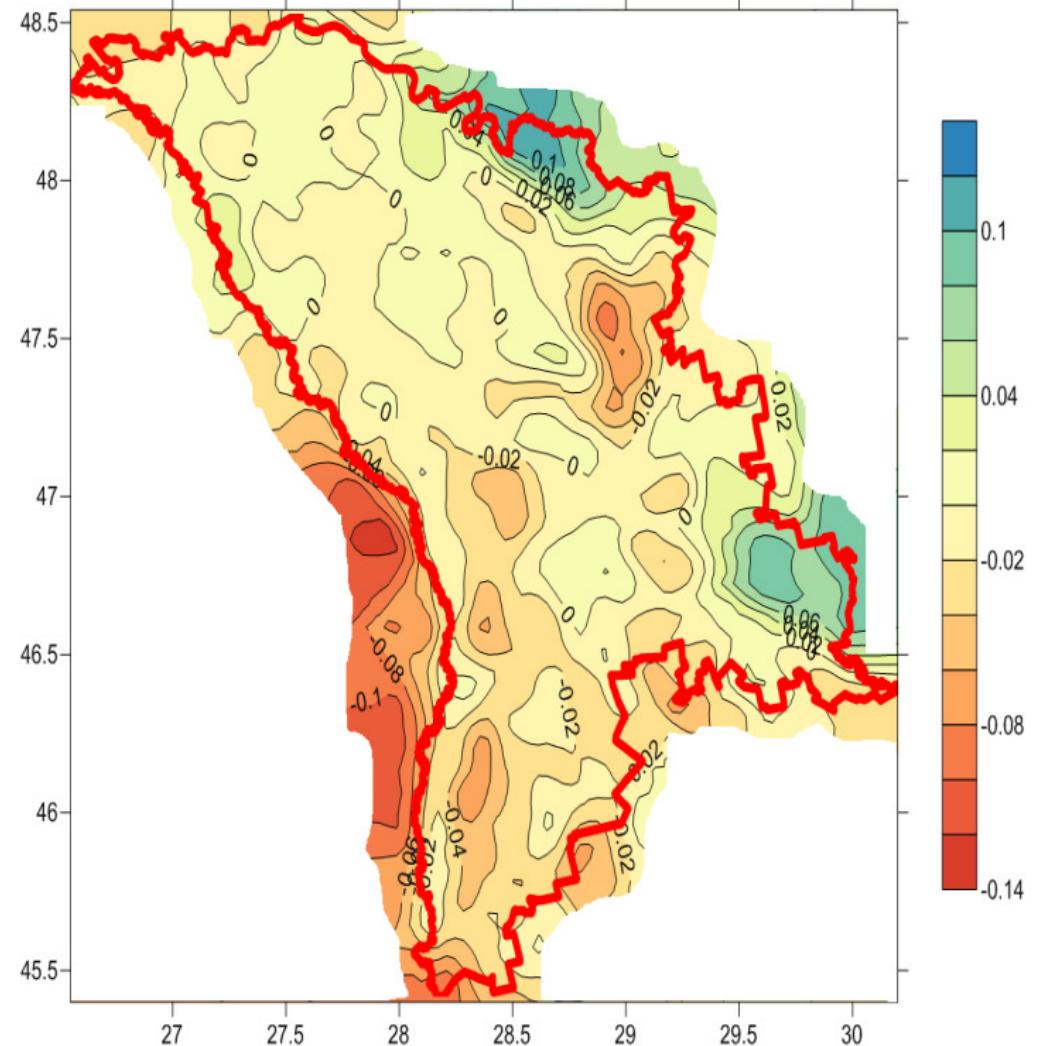
Modeling HRS/Quasigeoid for Moldova using EIGEN-GL04C  
EGG97 and GNSS/leveling measurements



## Testing out of geodetic databases



## Accuracy of HRS/Quasigeoid for Moldova



## Testing out of geodetic databases



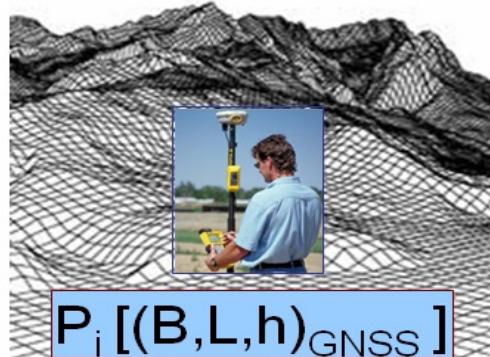
Second order leveling Benchmarks	MOLDREF99 Horizontal coordinates (m) X (N) Y (E)		Leveling normal heights (m)	Calculated from GNSS measurements normal heights (m)	Heights difference (m)
Ratus	225920,222	230467,989	58,414	58,407	-0,007
Roman	232181,483	227567,418	128,279	128,256	-0,023
Ivancea 181010	239335,129	2306740,827	162,697	162,669	-0,028
Fed 160-1	263140,000	217246,770	73,082	73,094	0,012



EUREF 2011, Chisinau, 25-28 May, 2011

## Gridding for Transformation Message

### Source CRS - Grid



$P_i[(B,L,h)_{GNSS}]$

Generated Grid of Local  
Virtual Fitting Points  $P_i$

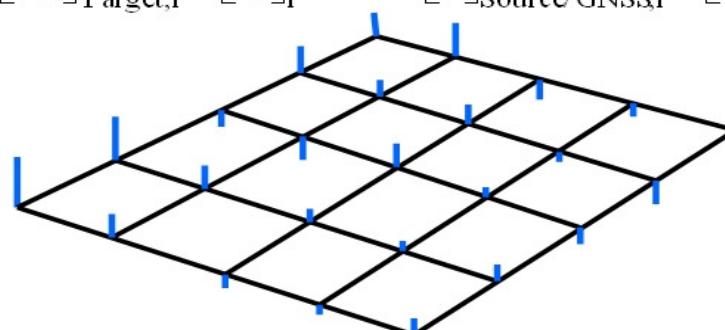
Any kind of  
individual  
Reference  
Transformation

Gridding into 1.] and/or 2.]

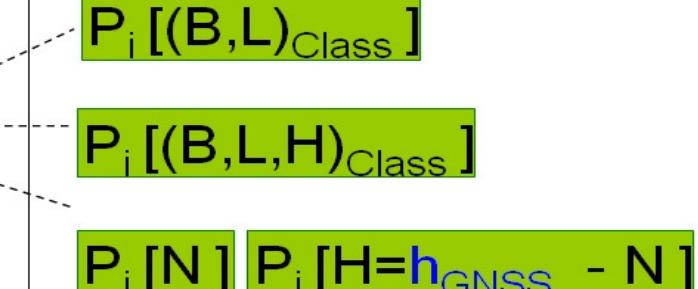
1.] 7 Parameter  
Transformation

2.] Geoid/HRS  
Grid

$$\begin{bmatrix} x_T \\ y_T \\ z_T \end{bmatrix}_{Target,i} + \begin{bmatrix} r_x \\ r_y \\ r_z \end{bmatrix}_i = s \cdot R \cdot \begin{bmatrix} x \\ y \\ z \end{bmatrix}_{Source/GNSS,i} + \begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}$$



### Target CRS - Grid



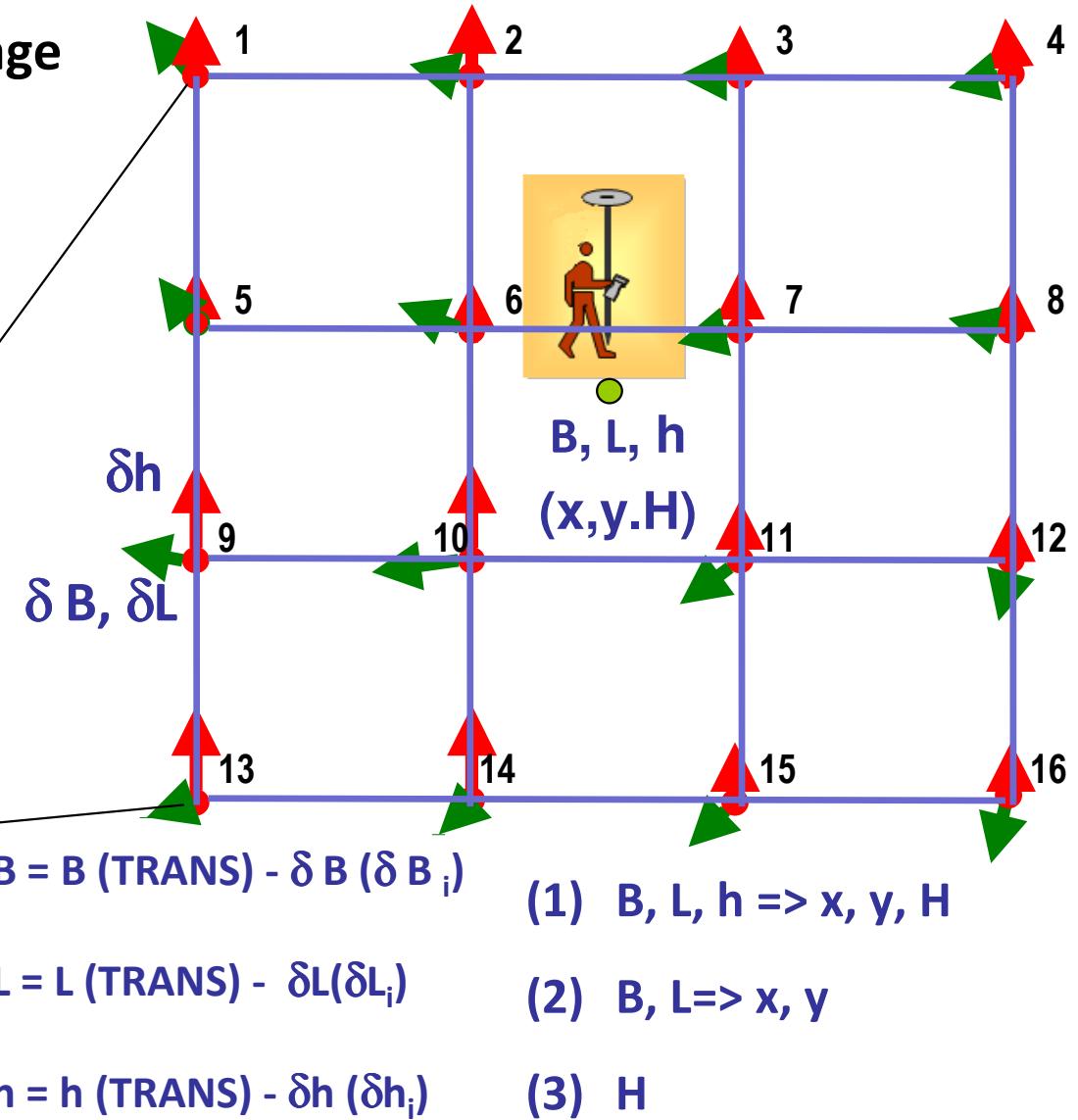
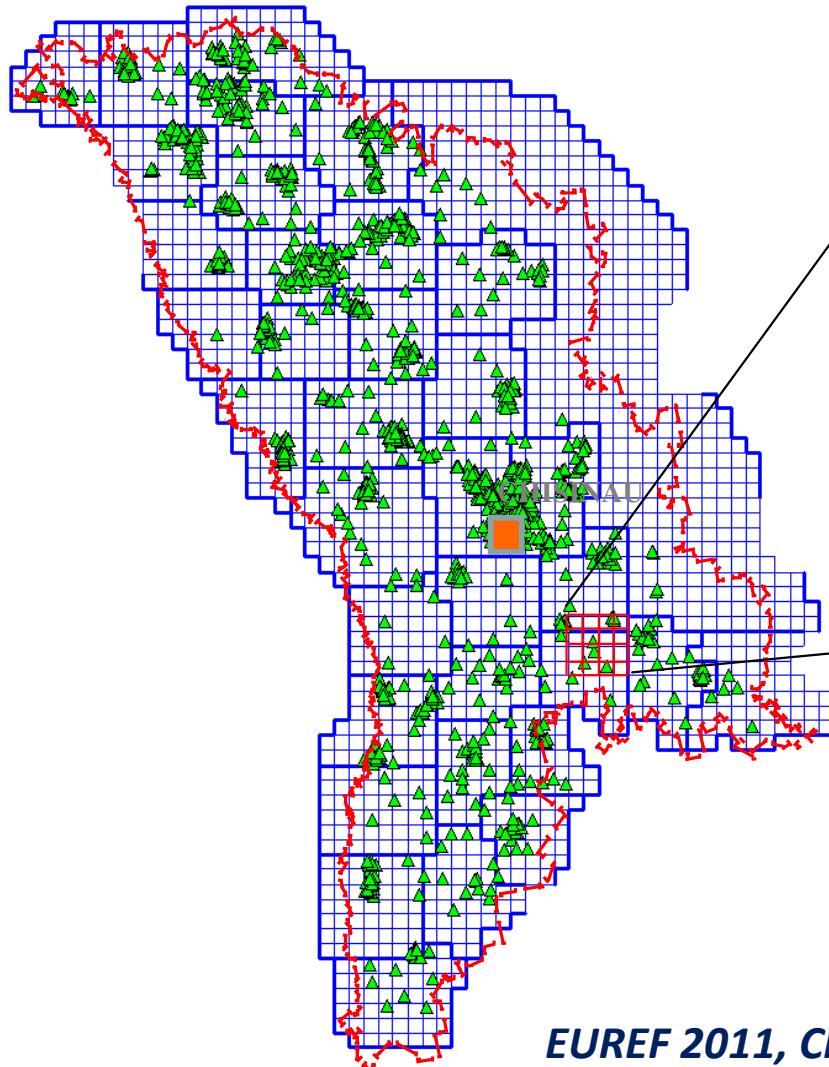
Resulting Local Virtual  
Fitting Points  $P_i$

7 Parameter Trend  
and 3D „Small“  
Residual Grid



Grid of  $N_i$

## Gridding for Transformation Message



# Generation of RTCM Transformation messages

## Structure of RTCM messages 1021 /1022

Data FIELD	DF NUMBER	Values	Remarks
Message Number	DF002	1021	
Source-Name Counter	DF+1	4	
Source-Name	DF+2	4258	ETRS89, Europa
Target-Name Counter	DF+3	7	
Target-Name	DF+4	31467	DHDN, GK-3
System identification number	DF+5	1	
Involved Transformation message	DF+6	0000000110	
Plate number	DF+7	7	
Computation Indicator	DF+8	1	
Height Indicator	DF+9	2	
$\phi_v$	DF+10	49.0102	
$\lambda_v$	DF+11	8.3921	
$\Delta\phi_v$	DF+12	0.04	
$\Delta\lambda_v$	DF+13	0.06	
dX	DF+14	-617.880	
dY	DF+15	-253.456	
dZ	DF+16	-315.690	
$R_1$	DF+17	5.79748	
$R_2$	DF+18	-2.44443	
$R_3$	DF+19	-5.1534	
dS	DF+20	-13.51806	
add $a_s$	DF+24	8137.000	GRS80
add $b_s$	DF+25	6752.314	
add $a_T$	DF+26	7397.155	Bessel
add $b_T$	DF+27	6078.963	
Horizontal 7P Quality Indicator	DF+76	2	

Geoid-Grid or not

Grid  
Location&Size

7 Parameters

Ellipsoid  
Parameters  
Source / Target

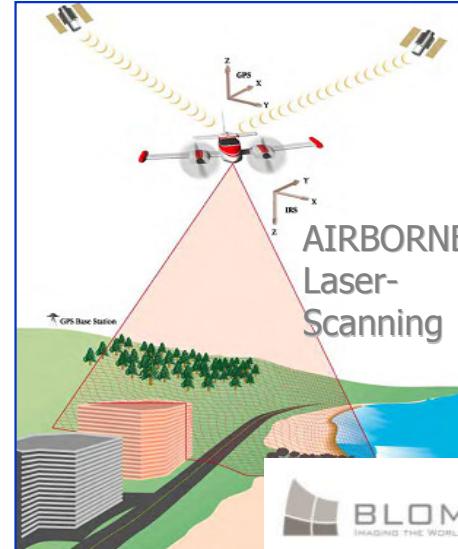
## Structure of RTCM message 1023 /1024

$\delta N_{14}$	Residuals $P_{14}$	DF+71	0.001	:
$\delta E_{14}$		DF+72	0.013	
$\delta h_{14}$		DF+73	0.049	
$\delta N_{15}$	Residuals $P_{15}$	DF+71	0.005	
$\delta E_{15}$		DF+72	0.009	
$\delta h_{15}$		DF+73	0.088	
$\delta N_{16}$	Residuals $P_{16}$	DF+71	0.006	
$\delta E_{16}$		DF+72	-0.002	
$\delta h_{16}$		DF+73	0.129	
Horizontal interpolation method indicator		DF+74	0	
Vertical interpolation method indicator		DF+75	0	
Horizontal Grid Quality Indicator		DF+78	1	
Vertical Grid Quality Indicator		DF+79	1	
Modified Julian Day (MJD) Number		DF+80	53570	

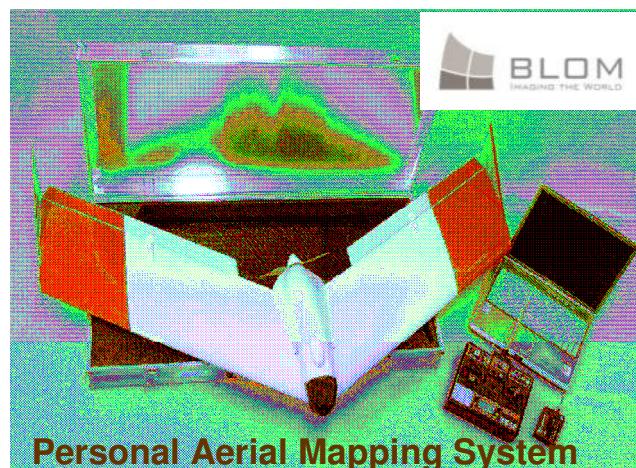
DFHRS Database use in direct access on controllers or for setting up the RTCM3.1 transformation-message, height indicator =2

$$H = h - NFEM(p | B, L)$$

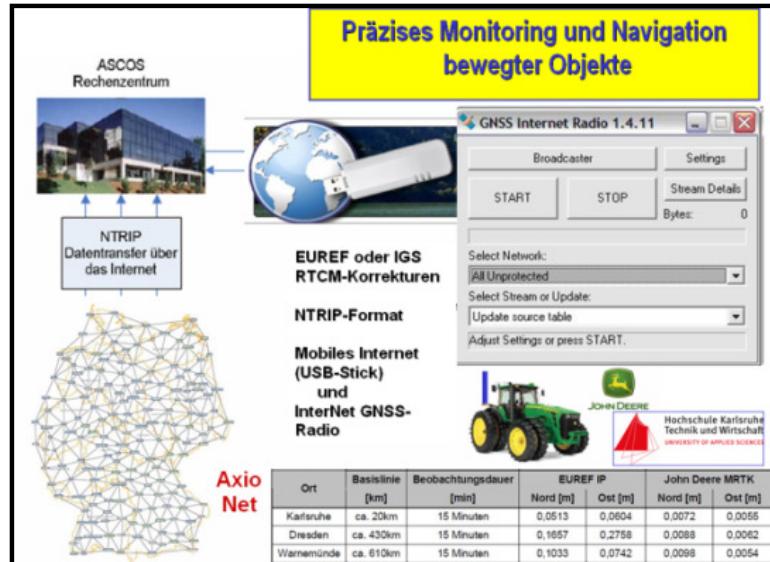
## GNSS-Positioning Services – User-Groups



## GNSS-based and Multisensor Low-Cost Platforms for Navigation and Object-Georeferencing



## Growth of GNSS-Positioning Services User-Groups



# Conclusions

- High precision Quasigeoid model will improve normal height determination from GNSS measurements using the MOLDPOS service
- Transformation Parameters data bases can be used by a large spectrum of users (geodetic works, cadastral surveying, GIS applications, mapping and boundary marking, etc.) and support of scientific applications (landslide and floods monitoring, environmental research, geohazard prediction, geodynamic investigations etc.)
- The new RTCM 3.1 transformation messages allows the GNSS service to provide their users with all necessary information for 2D positioning and GNSS-based height computation related to the national HRS
- For future improvement of Quasigeoid model accuracy a fitting GNSS/Leveling points related to 1st and 2nd order leveling networks, Gravity values of the national gravity network and vertical deflection measured by digital zenith camera along the state border to be included in the model



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# Thanks for attention

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*Peter Spohn*

[www.moldpos.eu](http://www.moldpos.eu)