

# **The Italian transition from a static to a dynamic reference frame: present transformation and future developments**

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## Outline

A general definition of positioning service and the present Italian situation: IGM95.

The need of a zero order PN and the first test.

The study of IGM95 deformations:

ItalPos PN adjustment in IGS and link to IGM95, the transformation from IG05 to IGM95.

The new official IGM network: RDN  
RDN adjustment in ITRF/IGS05.

Conclusions.

## Positioning RT services

A positioning service based on GNSS permanent stations distributes coordinates, data and network products both for cadastral (RT) and high precision (PP) applications.

**It materializes and distributes  
one or more reference frames to the user community:**

**ITRFyy for high precision applications,  
the official cartographic RF (in Europe some ETRFyy)  
for cadastral surveying.**

ITRF2005/IGS05: different 2005 realizations of ITRS;  
in the following adjustments, IGSS05 has been used.



## The present situation in Italy

$\approx 12^\circ \times 12^\circ$ , 301388 Km<sup>2</sup>

20 administrative regions:  
surfaces (Km<sup>2</sup>)

Mean  $\approx 15000$

Max = 25708 (Sicilia)

Min = 3262 (Aosta)

Positioning services are  
designed, created and  
managed at the  
Regions scale.

Usually adjusted in IGS  
(IGS05).

## The official cartographic Italian RF

**ETRF89-IGM95** is the official Italian cartographic RF:  
2000 benchmarks, adjusted in ETRF89,  $t_0=1989.0$ ;

due to elapsed time  
both spatially correlated deformations and sparse blunders.

Our opinion for the future:  
Italy should switch from the static ETRF89-IGM95 network  
to a continuously monitored realization (zero order PN) of ETRS89.

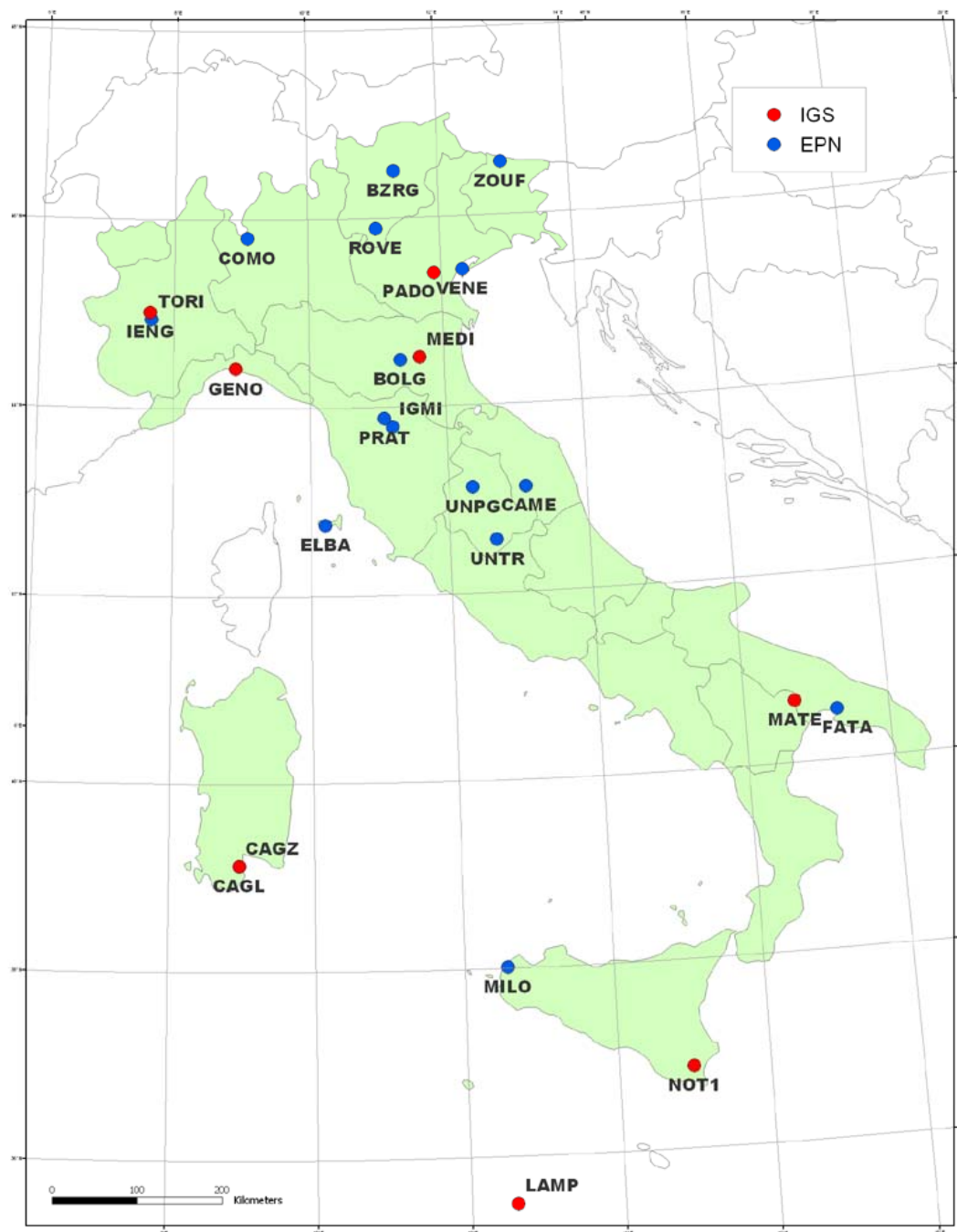
Present needs:  
a transformation between IGS05 and ETRF89-IGM95  
must be estimated and provided to the positioning services users.

# The requirements for a national zero order PN

(All in EUREF 2007 proceedings, same authors)

Minimal characteristics:

- 1) homogeneously distributed over the whole nation,
- 2) including the main PS's of EPN and IGS,
- 3) including the main PS's of the national geodynamics PN's ,
- 4) including at least 2 PS's for each local Positioning service,
- 5) strict rules for PS's, like for IGS and EPN;
- 6) RINEX data, log files,..., freely available to the community.



## The Italian need of a national zero order PN

IGS and EPN PN's alone cannot constitute the zero order PN in Italy:

- 1) too sparse and not homogeneously distributed;
- 2) not aimed to monitor/certify local subnetworks;
- 3) not aimed to materialize national cartographic RF's.

## The first test: 2007

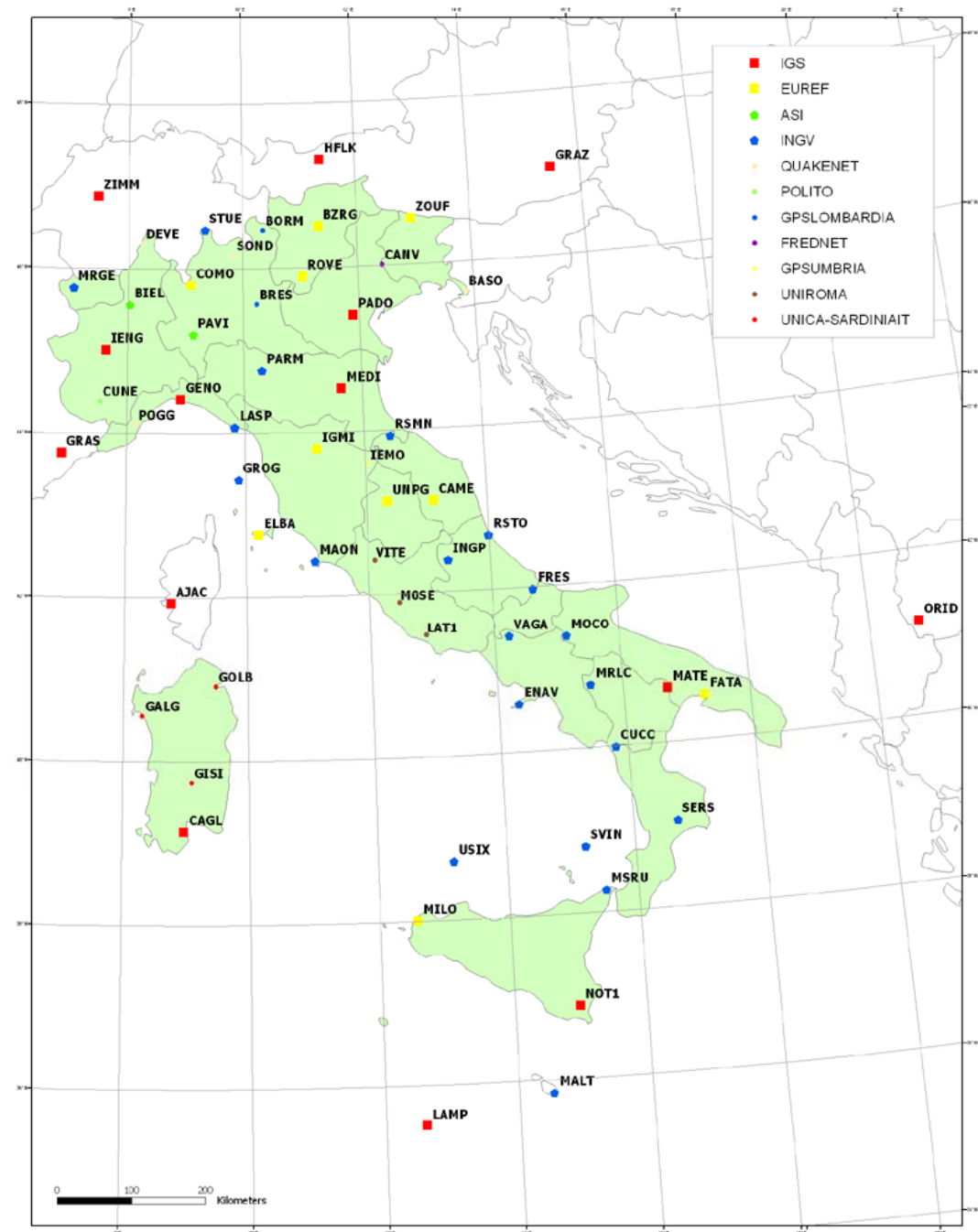
In Italy almost 400 PS's have been catalogued (2008):  
in 2007 a trivial test.

Selection of a subset:

62 PS's,  
mean distance 100 Km;  
analysis of 3 months  
(1.1.2007.0-31.3.2007).

Processing with BSW5.0:

extraction of quality indexes  
and outlier rejection.

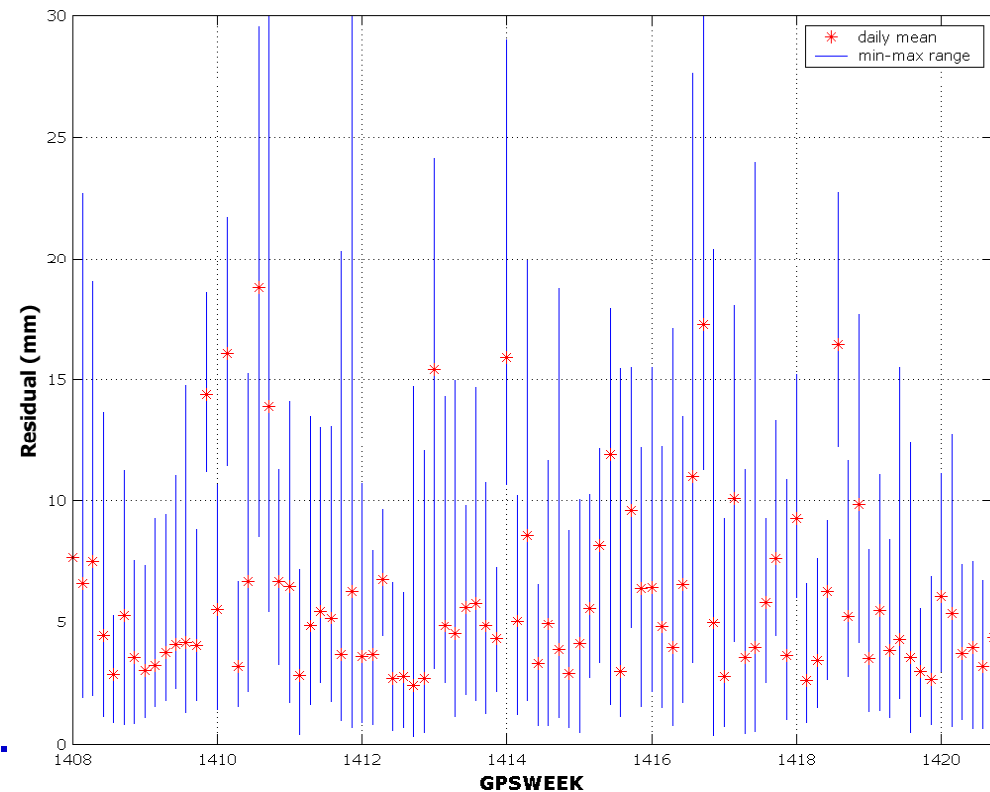




## The first test 2/2

Main problems due to RINEX reconstruction from RTCM streams;  
no other significant problems.

A well distributed Italian ZO network can be established by **connecting and ruling** a subset of already existing PS's.



Multibase final RMS (mm)	
Mean	1.3
$\sigma$	0.2
Min	1.0
Max	1.9

Time series residuals (mm)			
	East	North	Height
Mean	0.0	0.0	0.0
$\sigma$	3.5	3.2	6.1
Min	-18.6	-14.3	-62.1
Max	15.6	26.7	63.0

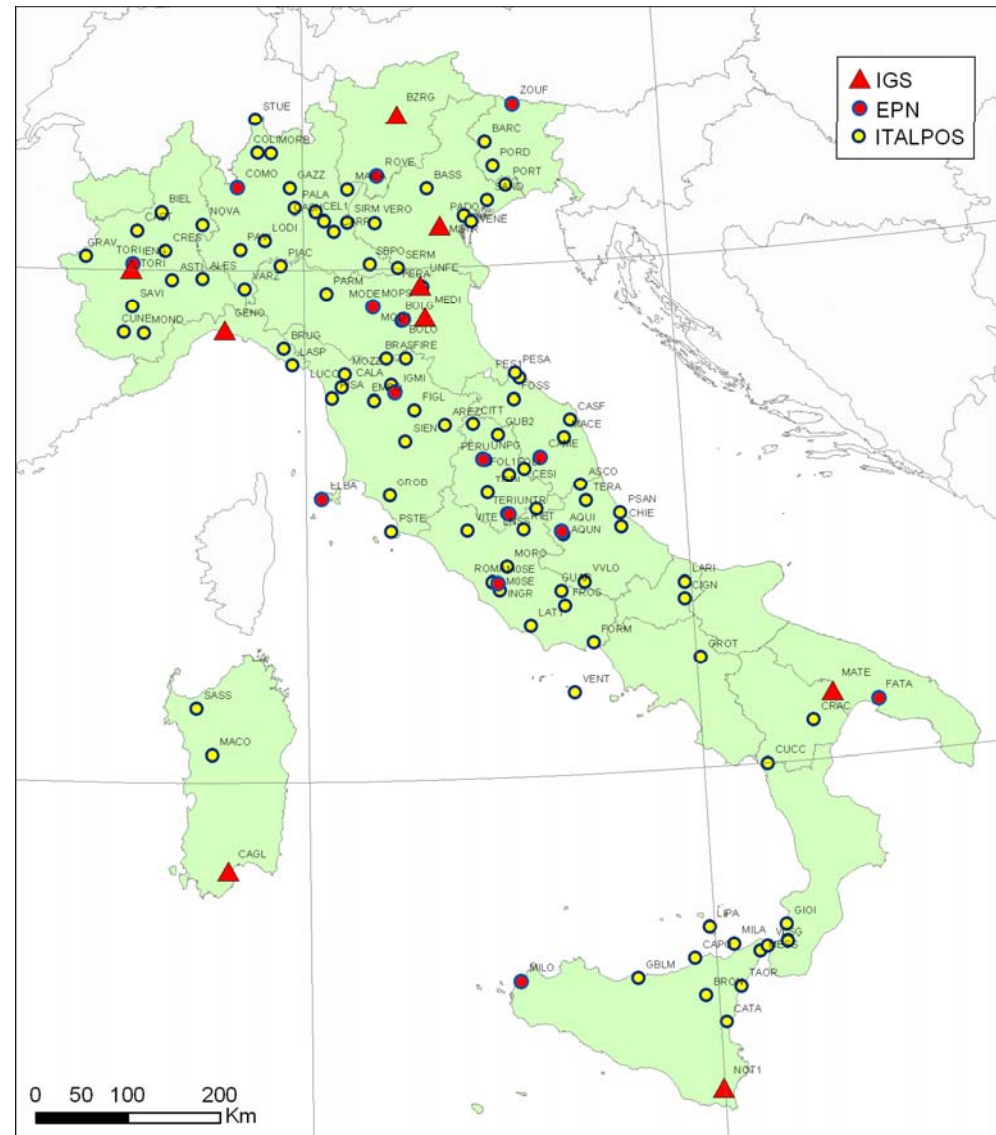
# The transformation: ItalPos case study

In Italy  
a national PN 104 PS's  
is operated by a private firm:  
ItalPos, Leica Geosystems.

By the  
adjustment of ItalPos in IGS,  
its link to IGM95:  
a first study at the national  
scale of

1. the transformation between  
ITRF2005 and IGM95,

2. the local IGM95  
deformations.



## Adjustment of ItalPos in IGS

Five weeks of data of ItalPos: GPSW 1452-1456, central epoch 2007.9.  
Only 7 IGS PS's continuously available and used in the selected period.

1) IGS PS's stochastically  
constrained to  
their official IGS coordinates;

2) adoption of the final IGS  
EOP, EPH and PCV's;

3) adoption of the IGS and EPN  
guidelines  
in the raw data elaboration.

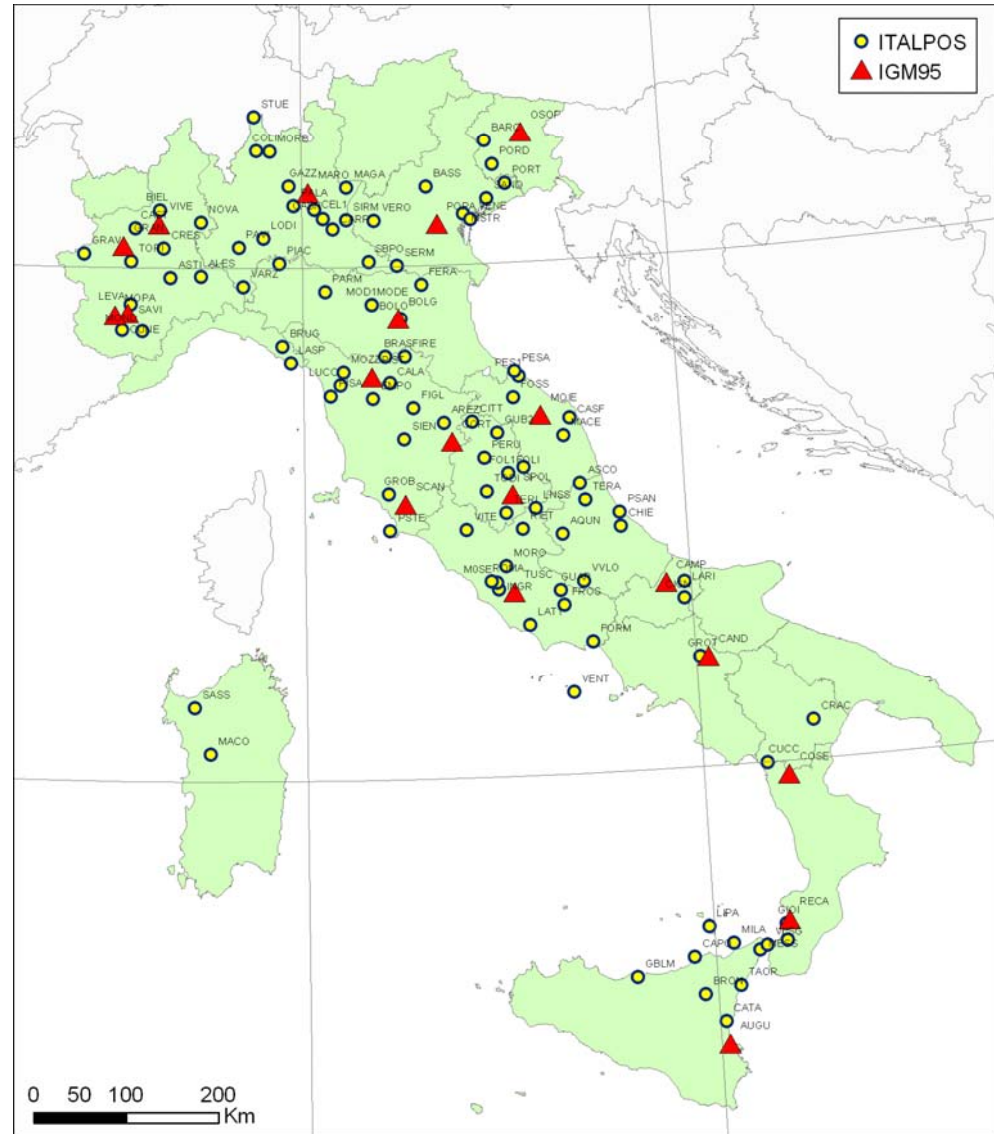
4) 180 out of 2800 solution  
discarded,  
satisfactory final statistics.

Global daily residuals time series			
(mm)	East	North	h
$\sigma$	3.4	2.8	7.5
min	-19.3	-12.8	-35.8
max	22.4	14.5	44.5

Single station RMS's			
(mm)	East	North	h
Mean	3.6	2.8	7.5
Max	8.5	8.4	13.6

## Connection of ItalPos to IGM95

- 1) 19 IGM95 benchmarks;  
3 to 6 hours sessions.
- 2) each benchmark  
connected to 2 to 4 PS's,  
constrained;
- 3) multibase BSW5.0,  
to estimate IGS coordinates of  
IGM95 benchmarks;
- 4) typically:  
80% of ambiguity fixing,  
formal RMS's of about 1.5 mm



Estimated IGS and monograph IGM95 coordinates:  
analysis of the transformation from IGS05 and IGM95.

# Transformation from IGS05 to IGM95: first method

## Starting hypotheses

At the national scale the transformation is the sum of a national similarity and a deformation field.

The similarity transformation can be estimated in two ways:

1. by the IGS PS's in Italy (IGS05 and ETRF2005 published coordinates);
2. by the IGM95 benchmarks (IGS05 estimated and ETRF89 monographs).

The deformation field can be estimated by least squares collocation on the IGM95 residuals.

At a smaller spatial scale the transformation can be modeled by a similarity transformation.

## Formulas

Similarity transformation between two RF's

$$\mathbf{x}_{II}(P_i) = \mathbf{t} + (1+k)\mathbf{R}(r_1, r_2, r_3)\mathbf{x}_I(P_i) + \Delta(P_i)$$

$$\mathbf{R} = \mathbf{I} - [\mathbf{r} \times]; (1+k)\mathbf{R} = \mathbf{I} + k\mathbf{I} - [\mathbf{r} \times]; \mathbf{r} = [r_1 \ r_2 \ r_3]^T$$

Observation equation for a point

$$\mathbf{x}_{II}(P_i) - \mathbf{x}_I(P_i) = [\mathbf{I} \quad [\mathbf{x}_I(P_i) \times] \quad \mathbf{x}_I(P_i)] \begin{bmatrix} \mathbf{t}^T & \mathbf{r}^T & k \end{bmatrix}^T + \Delta(P_i)$$

Deformation field

$$\Delta(P_i) \Rightarrow [\Delta E(P_i), \Delta N(P_i), \Delta h(P_i)]^T$$

$$\Delta_i = \Delta(\varphi, \lambda)_i + \boldsymbol{\delta}(\varphi, \lambda)_i + \boldsymbol{\varepsilon}_i$$

$$\Delta(\varphi, \lambda)_i = \mathbf{f}(\varphi, \lambda, a_1, \dots, a_n) \quad \text{parametric deterministic part}$$

$$\boldsymbol{\delta}(\varphi, \lambda) \square \boldsymbol{\delta}(\mathbf{0}, \mathbf{C}_{\boldsymbol{\delta}\boldsymbol{\delta}}) \quad \text{stochastic part}$$

## Estimation by IGS PS's

For each IGS PS:

1. official IGS05 coordinates, at the adjustment epoch;
2. official ETRF2005 coordinates, backpropagated at epoch 1989.0:  
backpropagation in time is needed to align the transformation to IGM95 t0)

For each IGM95 benchmark:

application of the transformation and residual analysis.

Clear biases of IGM95 residuals plus a spatial covariance structure:

IGS PS's Residuals			
(cm)	East	North	h
Mean	0.0	0.0	0.0
$\sigma$	2.3	2.5	1.9
Min	-3.5	-3.6	-2.5
Max	3.4	3.2	2.6

IGM95 residuals			
(cm)	East	North	h
Mean	1.5	0.8	-3.5
$\sigma$	4.1	3.3	6.3
Min	-7.1	-2.6	-16.0
Max	8.6	8.5	8.9

## Note on the estimation by IGS PS's

Relatively high residuals on IGS PS's due to the need of backpropagation in time.

very small residuals in the transformation IGS05-ETRF2005 at the same epoch (2007.9)

(cm)	East	North	h
Mean	0.0	0.0	0.0
$\sigma$	0.1	0.1	0.1
Min	-0.2	-0.2	-0.2
Max	0.1	0.1	0.1



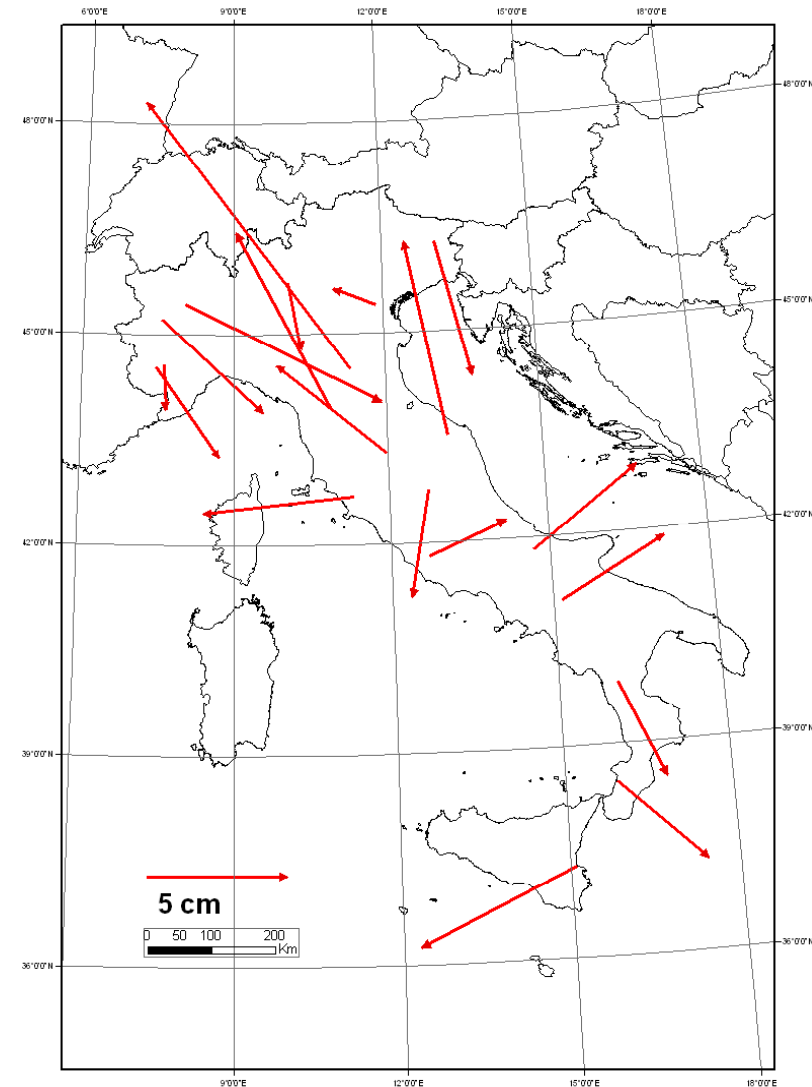
## Estimation by IGM95 points

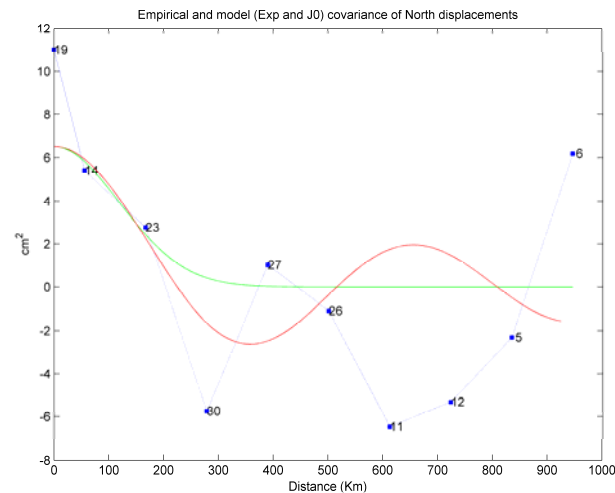
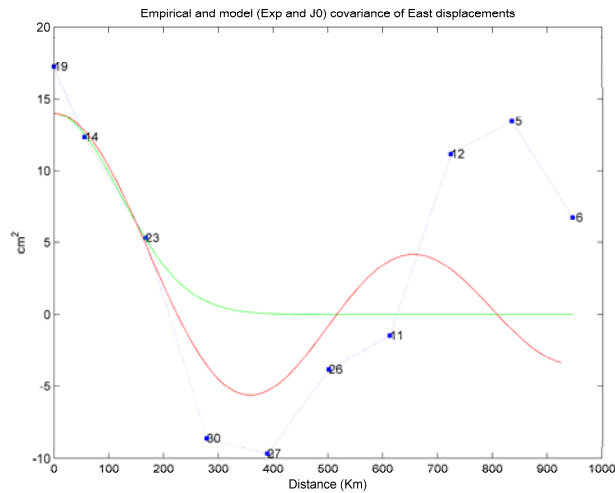
Estimation of a  
national similarity transformation.

Analysis of the residuals:  
a clear spatial structure.

Not 20 years geodynamics:  
spatial errors propagation!

(cm)	East	North	h
Mean	0	0	0
$\sigma$	4.1	3.2	6.2
Min	-8.3	-3.8	-12.0
Max	7.7	7.6	10.9





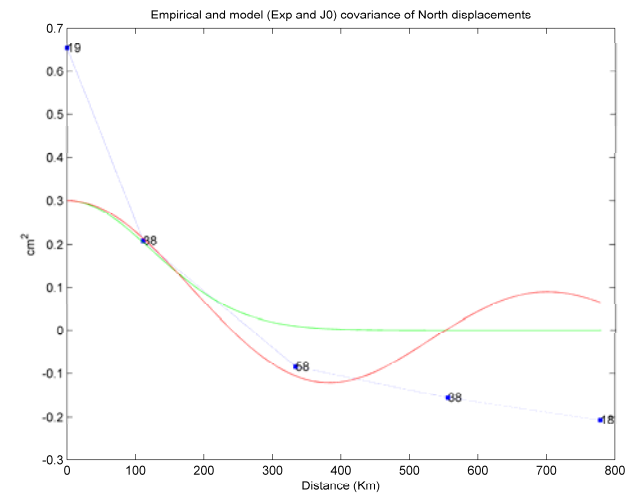
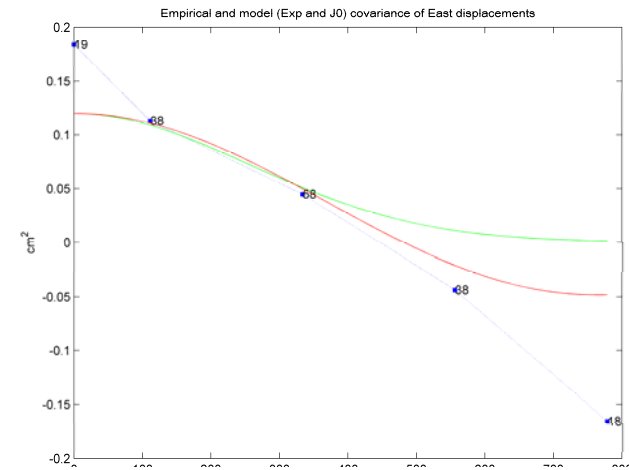
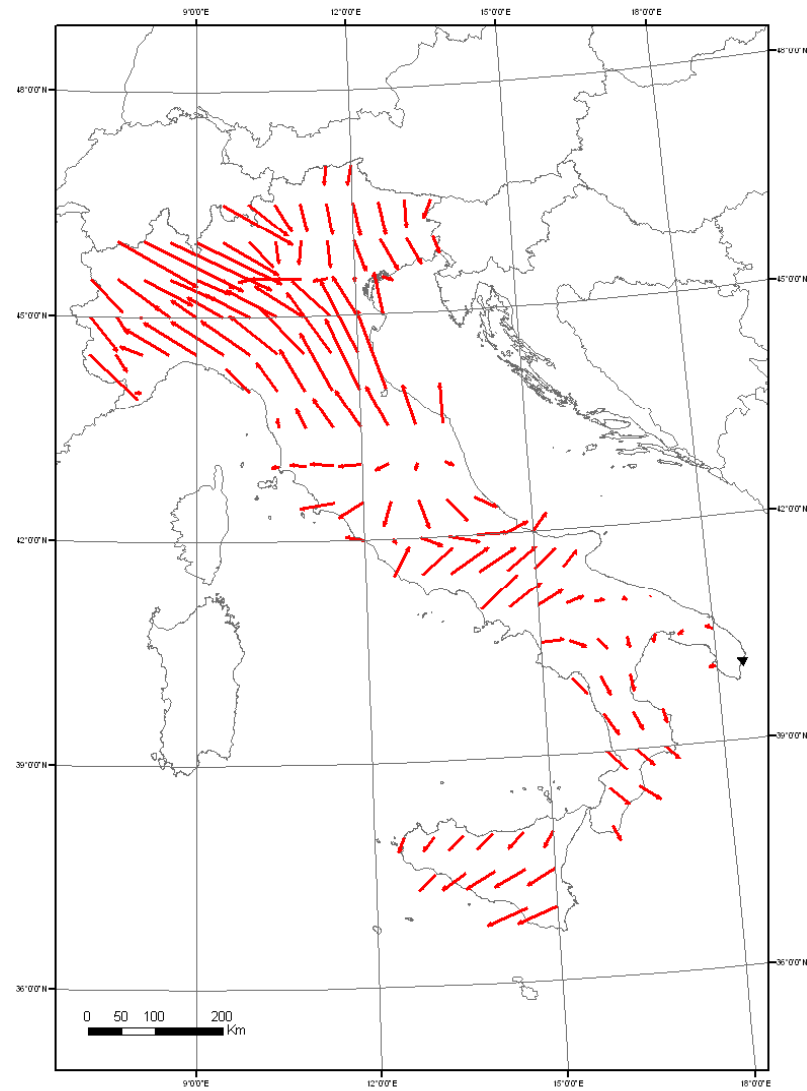
## Modeling the residuals

Prediction on a  $0.5^\circ \times 0.5^\circ$  grid  
by collocation approach  
(Biagi, Dermanis).

A numerical exercise:  
few data,  
spatially not well distributed;  
RT users cannot use  
deformation fields.

Useful for future,  
more complete analyses;  
final residuals uncorrelated.

# Prediction and residuals covariance



## The partitioned approach

Italy split into three regions:

Northern (10 points (\*)),

Central (9 points (\*) (\*\*)),

Southern (6 points (\*\*)).

(\*) 3 in common

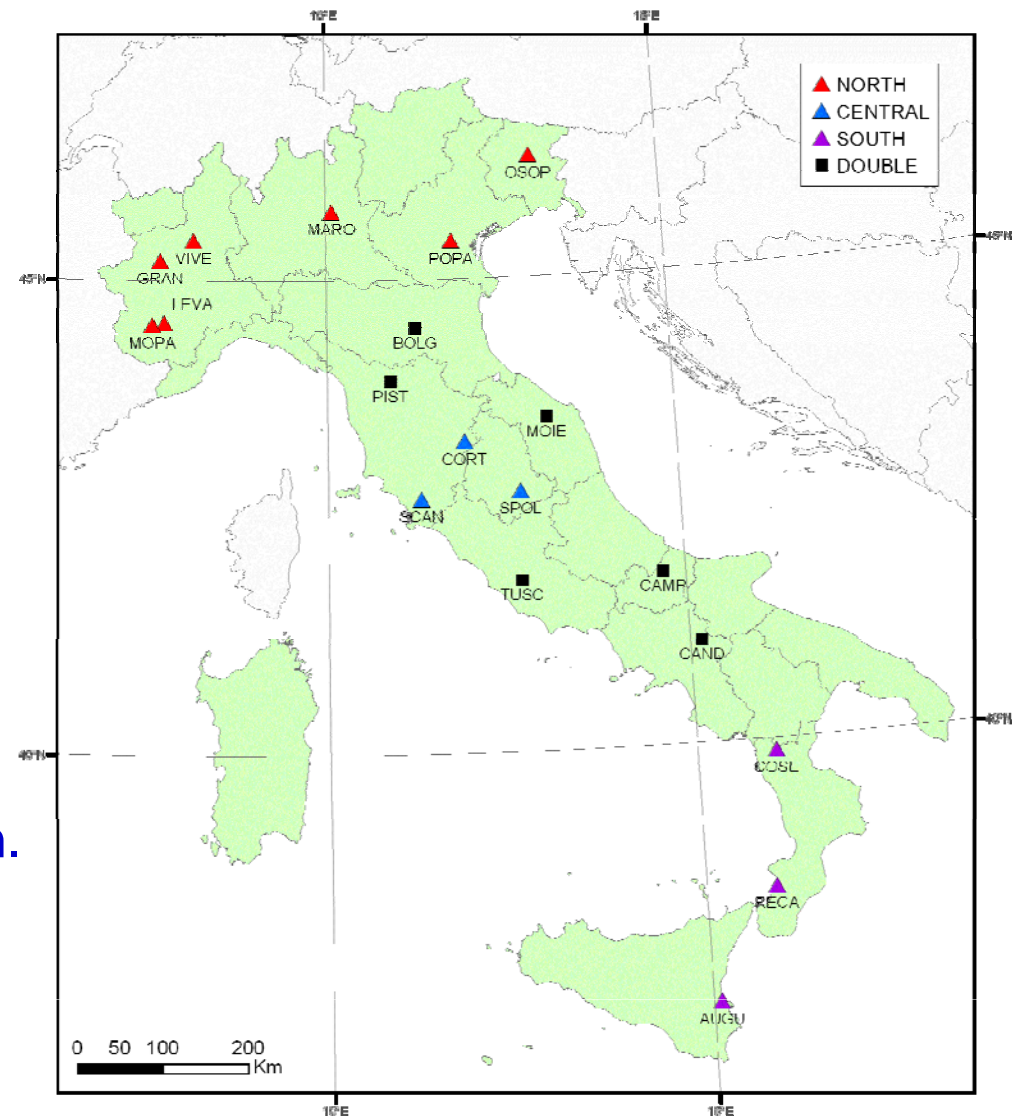
between North and Center

(\*\*) 3 in common

between Center and South

For each region a

different similarity transformation.



## Results: residual analysis (cm)

More points needed in South.

Satisfactory results for  
Center and South.

Unsatisfactory results for North:  
more points needed in the  
southern Padana Plain  
to split into two separate regions.

Different transformations in  
common points produce:  
5 cm differences in North/Center,  
3 cm differences in Center/South.

North	East	North	h
$\sigma$	4.0	2.7	5.8
min	-7.0	-2.8	-12.1
max	6.1	6.1	7.1

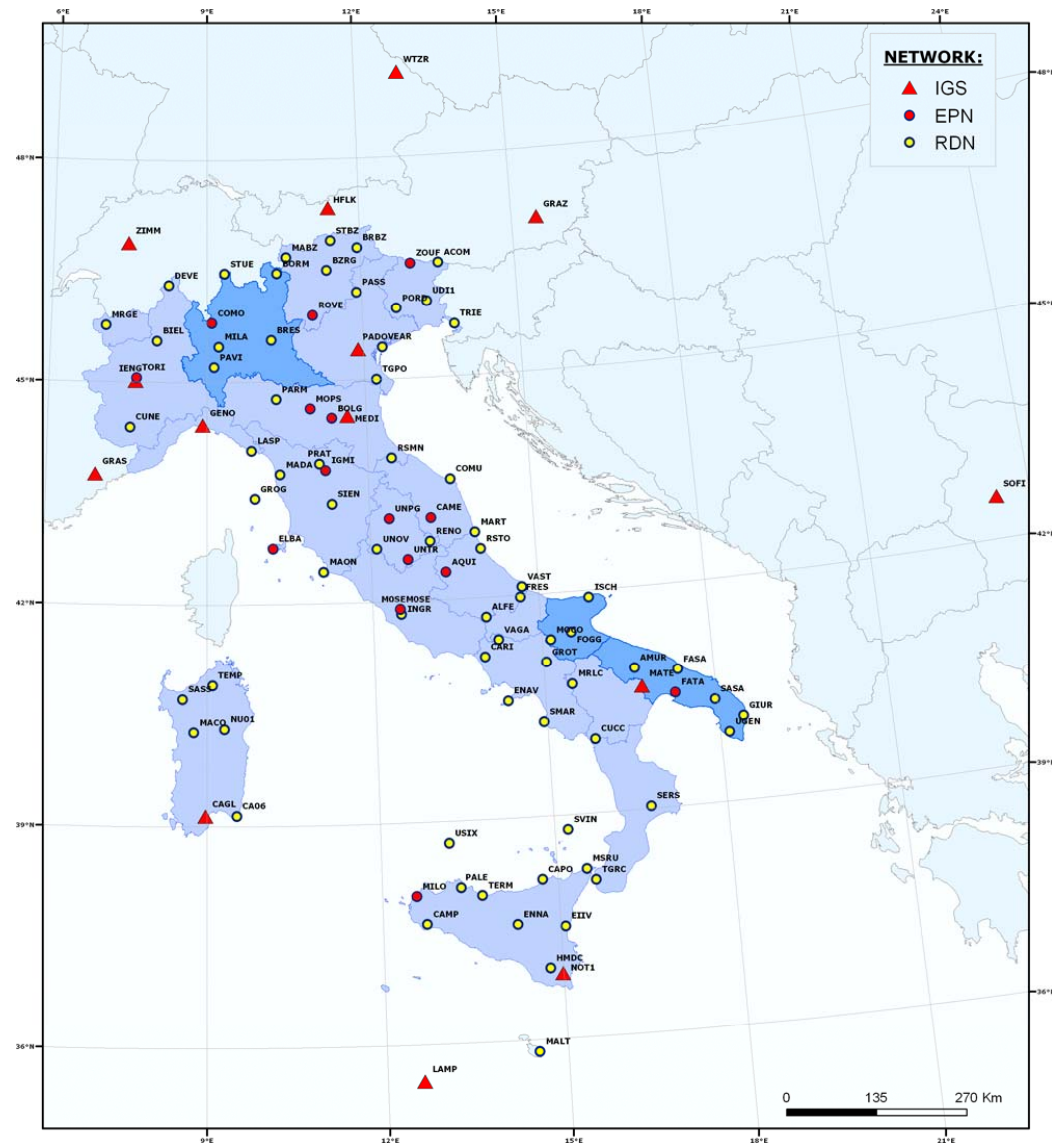
Center	East	North	h
$\sigma$	1.9	2.2	3.1
min	-1.9	-5.4	-5.4
max	3.0	2.1	4.6

South	East	North	h
$\sigma$	2.1	1.5	3.5
min	-3.2	-2.5	-4.8
max	3.3	1.6	3.7

# The new IGM network: RDN (Dynamic National Network)

96 PS's  
(7 IGS's outside Italy)  
permanently monumented,  
at present  
not permanently monitored.

One month of data;  
**(almost)** independent  
adjustments  
by IGM, UniPA, our group,  
in order to  
cross validate the results.



## RDN adjustment approach

Inclusion of all the Italian and neighboring IGS PS's;  
IGS PS's stochastically constrained to IGS estimates;  
adoption of final IGS products and absolute PCV;

adjustment with BSW5.0, according to BSW guidelines;  
30 daily solutions and

### **outlier rejection:**

- a) incomplete files,**
- b) high RMS's in some processing step,**
- c) great coordinates residuals wrt monthly mean;**

Final adjustment of accepted data.

# Results

Expected files:

2688

Not available:

196 (7.3%)

Excluded for data gaps:

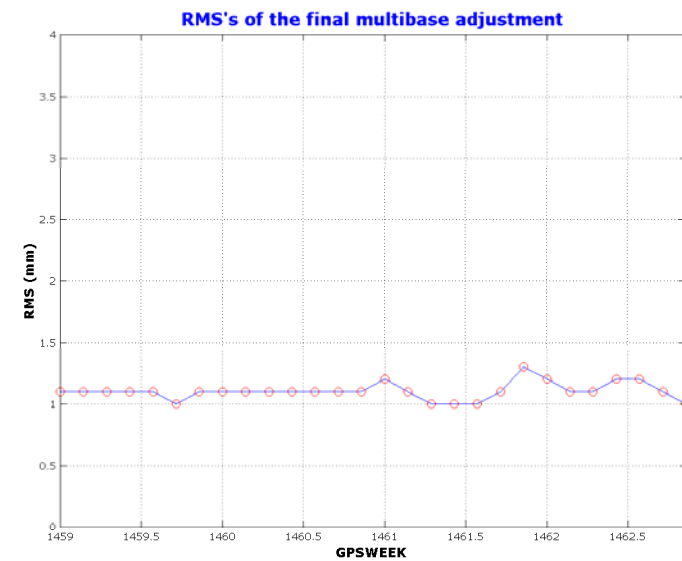
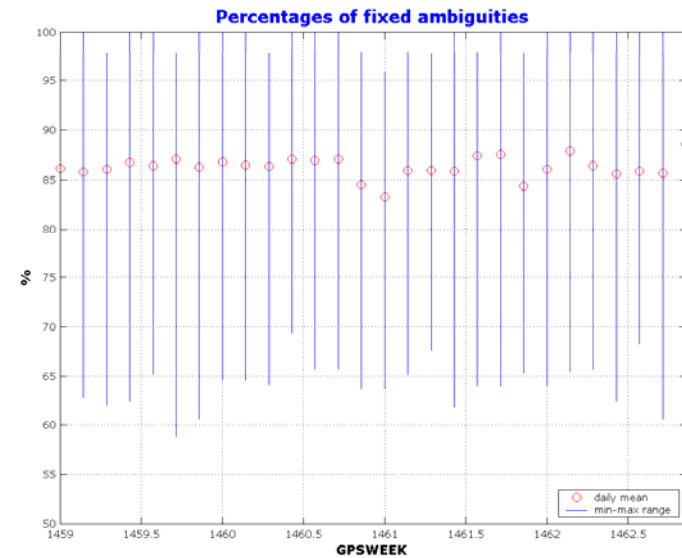
118 (4.4%)

Excluded for quality check:

67 (2.5%)

Final processed:

2307 (85.8%)

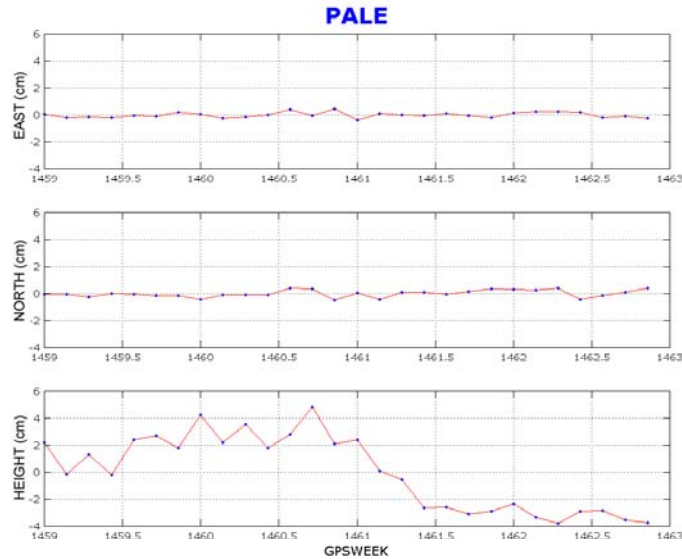




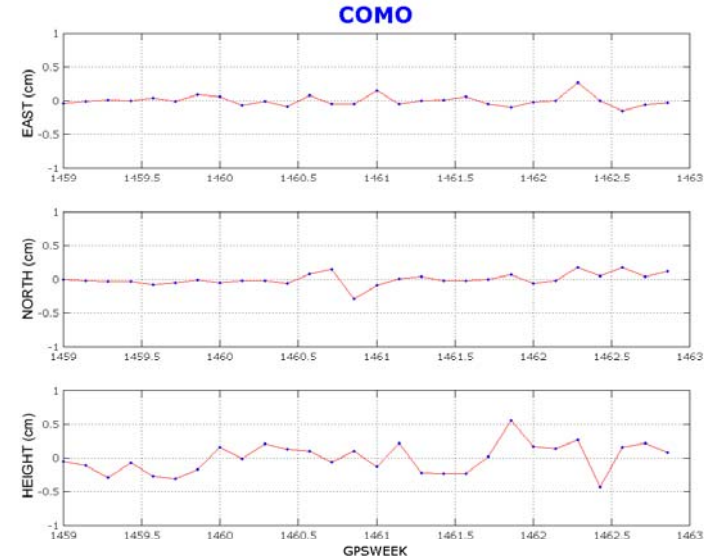
## Coordinates estimates

Daily residuals time series			
(mm)	East	North	h
$\sigma$	1.2	1.2	3.1
min	-7.0	-2.8	-12.1
max	6.1	6.1	7.1

Daily formal RMS's			
(mm)	East	North	h
Mean( $\sigma$ )	1.2	1.2	4.0
Max( $\sigma$ )	2.9	3.3	7.3



Rejected station



Accepted station

## Future work and conclusions

Compare IGS05/ITRF2005 in the adjustment;  
compare our with IGM, UniPD results;  
connect RDN to IGM95;  
definitely study the transformation  
between IGS05/ITRF2005 and ETRF89-IGM95.

From first results:

**IGM95 presents significant deformations and blunders;  
time is to switch to a continuously monitored national RF,  
by a continuous adjustment of a zero order PN (“RDN”).**

**Needs:**

**No new HW but guidelines/rules for RDN PS's,  
management, adjustment and monitoring implementation.**