

# **DETERMINATION OF GEOPOTENTIAL $W_{0,\text{ALICANTE}}$ AND ITS' CONNECTION TO $W_{0,\text{NAVD88}}$**

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**and**

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**SPECIAL STUDY GROUP  
GLOBAL GEODESY TOPICS: SATELLITE ALTIMETRY  
APPLICATIONS (SSG GGSA)**

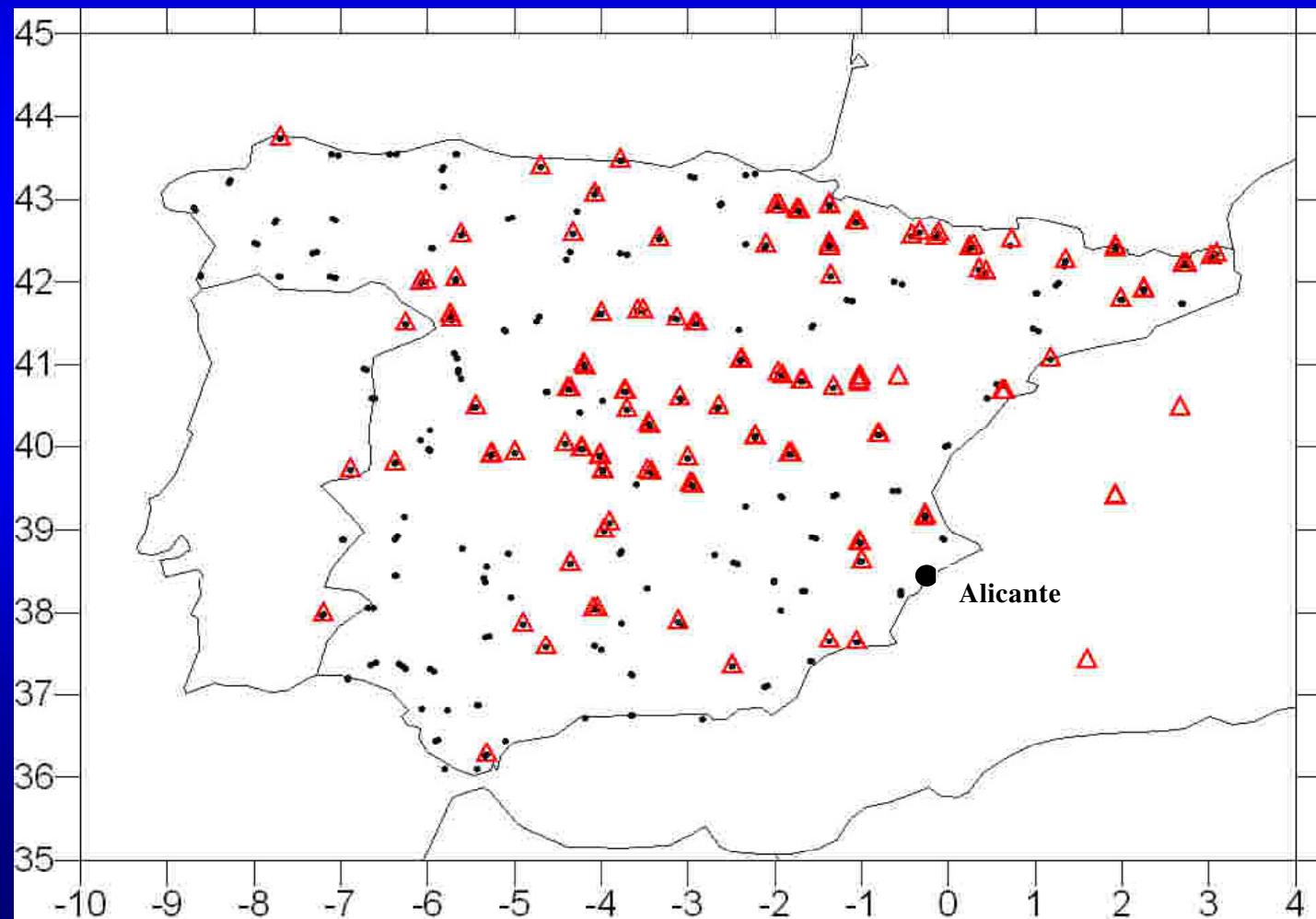
For a long time, SSG GGSA  
is working mainly at topics:

- Geopotential model testing
  - Development of geopotential value  $W_0$
  - Development of World Height System
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SSG GGSA very close cooperates  
with ICP- 1.2 of IAG (Dr. Ihde)

For this topics we have been collected necessary data, i.e. GPS/leveling sites – it covers about 70 % of the World

# SSG GGSA has been available current GPS/leveling sites from territory of Spain



**It's opportunity to apply  
developed methodology  
for determination of geopotential  
 $W_0$ , ALICANTE and its'  
connection (for example) to  $W_0$ , NAVD88  
described in (Burša et al., 1999, 2002)**

## 1st STEP:

the Helmert orthometric heights on the territory of Spain were transformed into the Molodensky's normal heights, the tidal corrections were applied, i.e. tide-free model was used

## 2nd STEP:

The following constants have been adopted:

$$GM = (398\ 600\ 441.8 \pm 0.8) \times 10^6 \text{ m}^3\cdot\text{s}^{-2}$$

$$\omega = 7\ 292\ 115 \times 10^{-11} \text{ rad}\cdot\text{s}^{-1}$$

$$W_0 = 62\ 636\ 856.0 \text{ m}^2\cdot\text{s}^{-2}$$

the numerical value of  $W_0$  value  
is currently discussed in IAG, ICP - 1.2

The following gravity models  
have been adopted:

**EGM96**

(Solution I)

**EIGEN-CG01C**

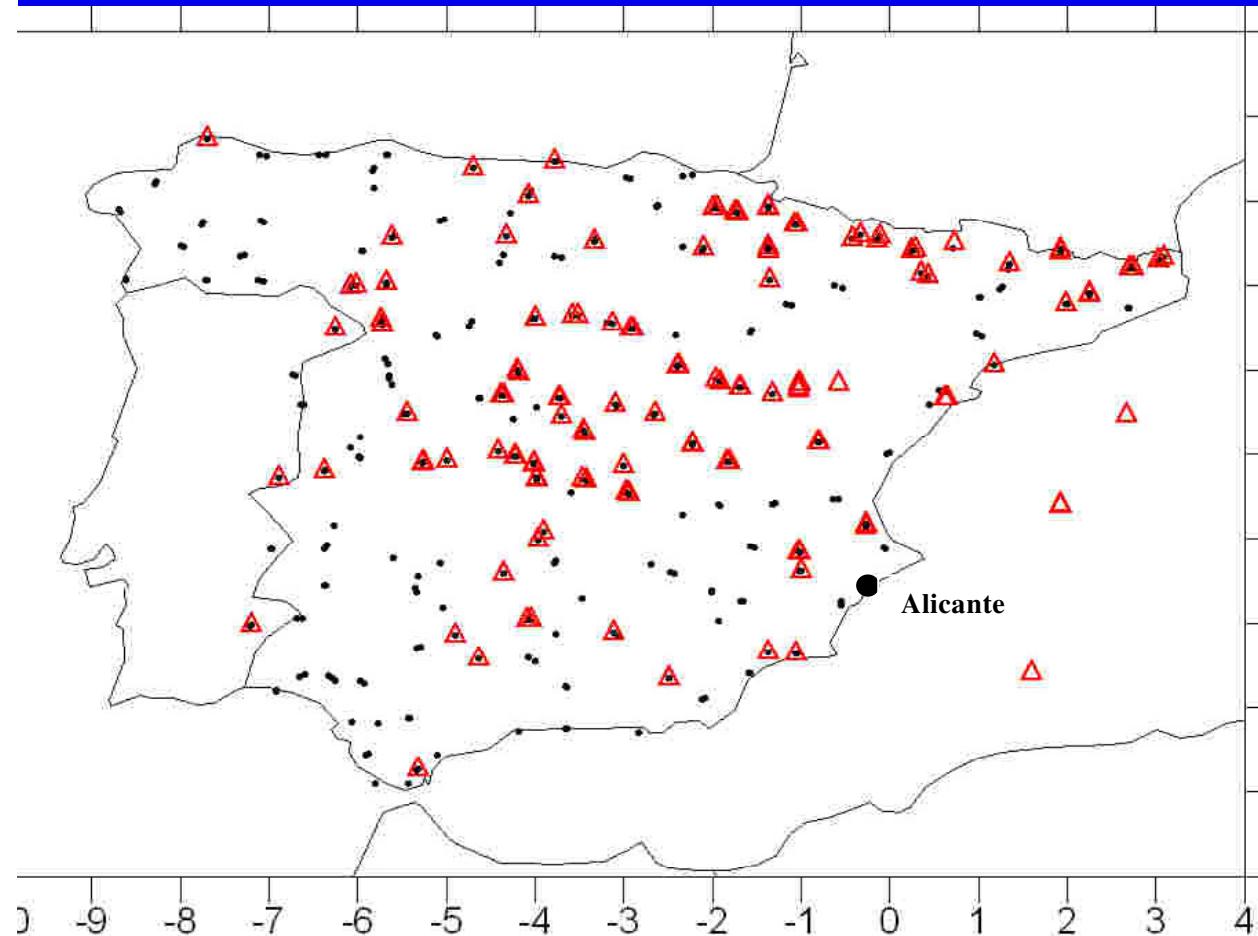
(Solution II)

**EIGEN-CG03C**

(Solution III)

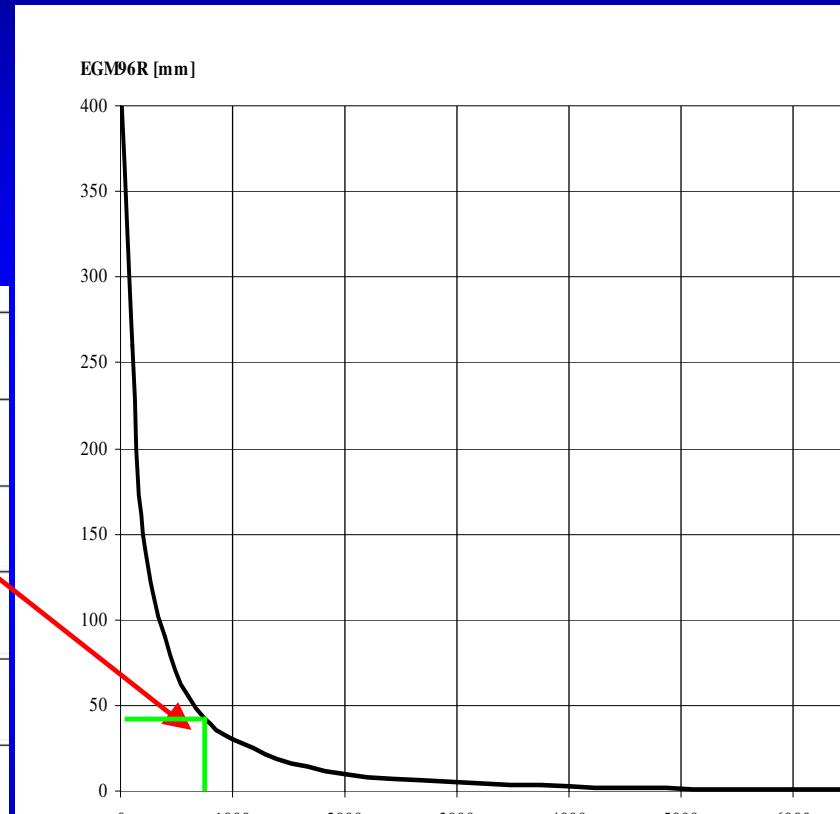
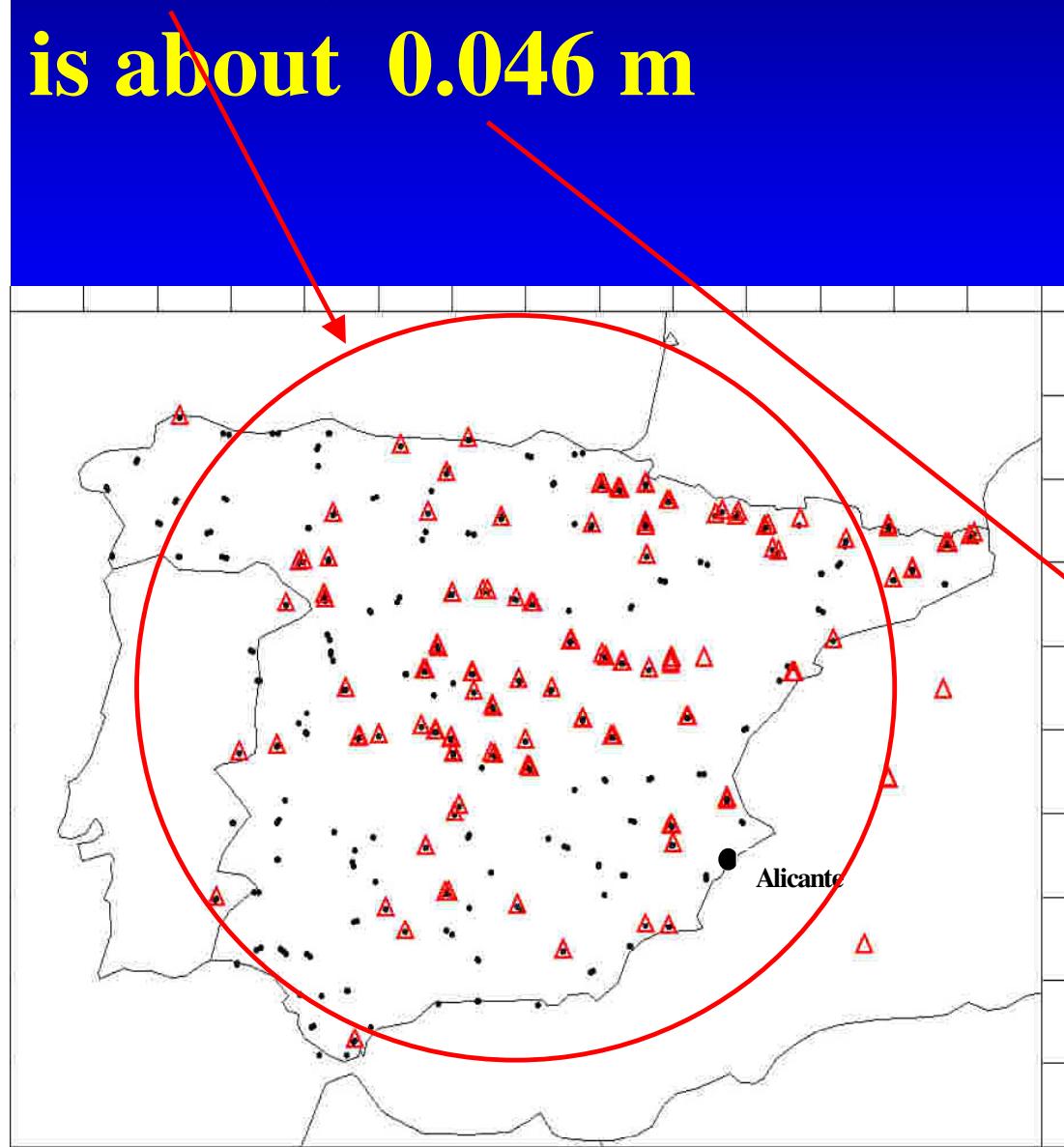
# Development of $W_0$ ,ALICANTE (Spain)

## The national territory of Spain is uniformly covered by the GPS/leveling sites



Distribution of  
GPS/leveling sites  
on the territory  
of Spain  
(325 black points)  
and  
geopotential  
numbers  
(128 triangles),<sub>9</sub>

The mean diameter of the area is about 750 km, so the resolution of EGM96 is about 0.046 m



# Solution of ALICANTE I, II, III

<b>Solution 325 GPS sites</b>	<b><math>W_0, \text{ALICANTE}</math> [m<sup>2</sup>.s<sup>-2</sup>]</b>
I EGM96	<b>62 636 860.56 ±0.70</b>
II EIGEN-CG01C	<b>62 636 861.88 ±0.70</b>
III EIGEN-CG03C)	<b>62 636 862.11±0.73</b>

# Solution of ALICANTE Ia, IIa, IIIa

<b>Solution 128 geopotential numbers</b>	<b><math>W_{0,\text{ALICANTE}}</math> [m<sup>2</sup>.s<sup>-2</sup>]</b>
Ia EGM96	<b>62 636 861.37±0.59</b>
IIa EIGEN-CG01C	<b>62 636 862.55±0.59</b>
IIIa EIGEN-CG03C)	<b>62 636 862.45±0.58<sub>12</sub></b>

# Solution of NAVD88

Solution	$W_{0,\text{NAVD88}}$ [m <sup>2</sup> .s <sup>-2</sup> ]
<u>U.S.A. , EGM96</u>	<b>62 636 861.27±0.51</b>
5 186 GPS sites	<b>62 636 861.22±0.51</b>
1 804 geopot. numbers	
<u>Canada, EGM96</u>	
1 311 GPS sites	<b>62 636 861.54±0.53</b>
1 248 geopot. numbers	<b>62 636 861.98±0.<sub>13</sub>51</b>

# RESULT

The mean LVD<sub>0,ALICANTE</sub> vertical shift  
with respect to LVD<sub>0,NAVD88</sub>

$$\delta H(\text{ALICANTE}) - \delta H(\text{NAVD88}) \\ \approx (-3.2 \pm 4.2) \text{ cm}$$

# CONCLUSION

By this way could be developed:

- mutual vertical shifts of all LVDs'
- vertical shifts of all LVDs' to the geopotential value  $W_0$
- World Height System

All this question are discussed in IAG, ICP 1.2

# SSG GGSA papers on GVRS, GVRF, and $W_0$

- Burša M., Kouba J., Raděj K., True S. A., Vatrt V., Vojtíšková M., 1999a: Determination of the geopotential at the tide gauge defining the North American Vertical Datum 1988 (NAVD88). *Geomatica*, 53, 459-466.
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