

# A new GPS derived velocity field of the postglacial adjustment in Fennoscandia, and its implication for the maintenance of the European geodetic reference frame

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# Outline

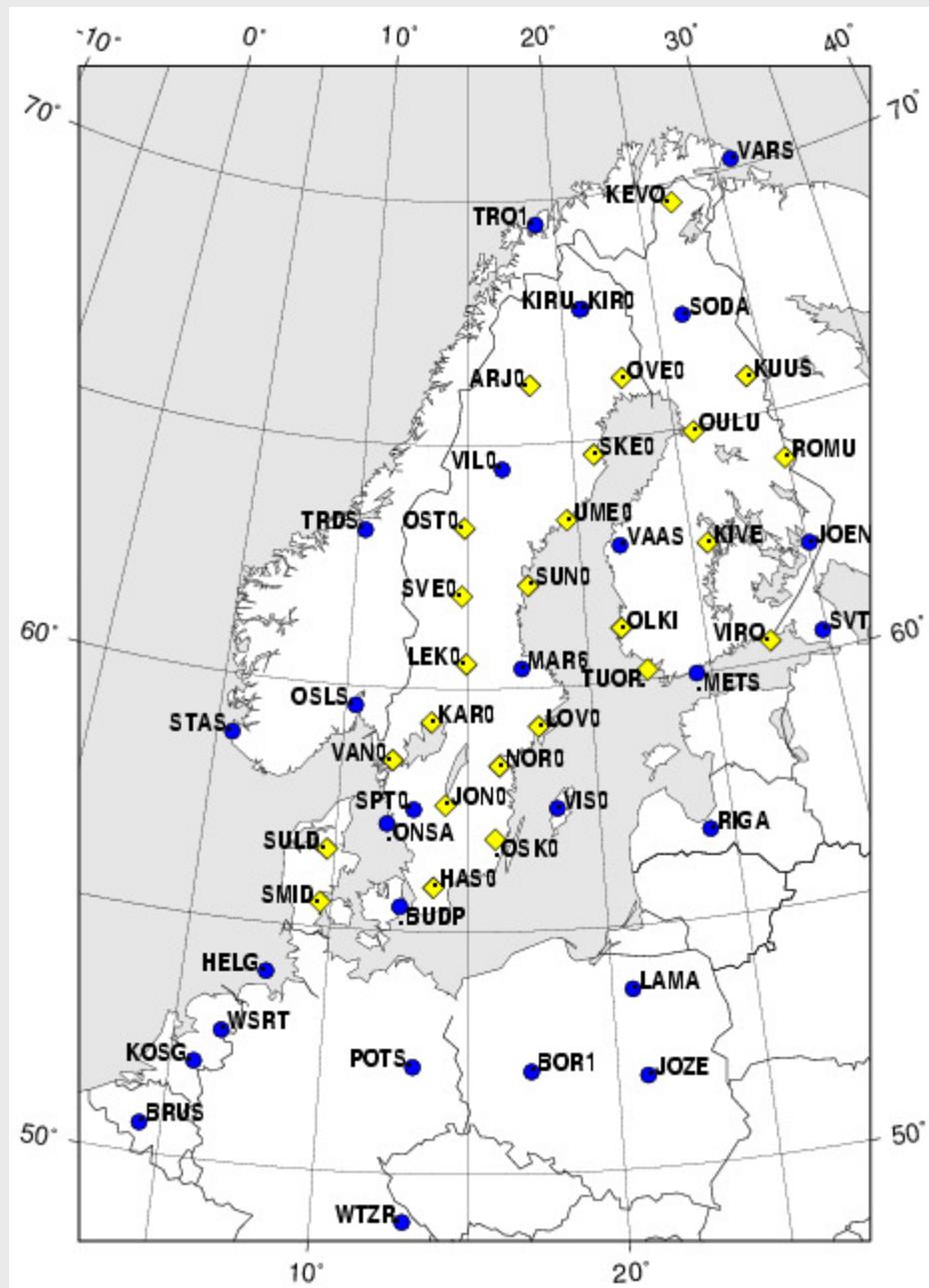
- The extended BIFROST network
- GPS analysis
- Time series analysis and data editing
- Evaluation of the velocity field
- Implications for European geodetic reference frame
- Conclusions



# The extended BIFROST network

Included GPS stations  
(Jan 1996 – June 2004)

- EPN station in Northern Europe (blue •)
- Finland
- Sweden (21 concrete pillars)
- Norway
- Denmark



# GPS analysis using GAMIT/GLOBK

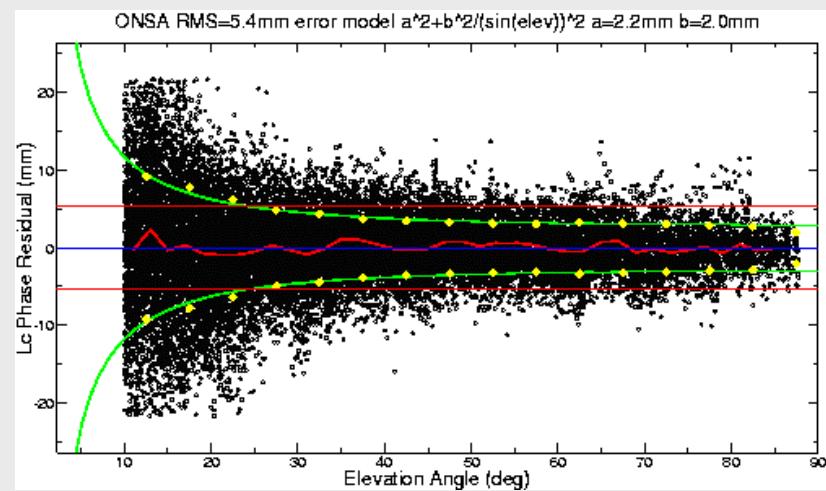
## GAMIT (GPS analysis)

- 10° elevation cut off angle
- tropospheric zenith delay parameters every 2<sup>nd</sup> hour (piece-wise-linear)
- daily gradient parameters
- the Niell mapping functions
- solve for integer phase ambiguities
- a priori orbits from SCRIPPS Orbit and Permanent Array Center (SOPAC) (g-files)
- 5 regional sub-networks
- individual elevation dependent weighting based on preliminary analysis



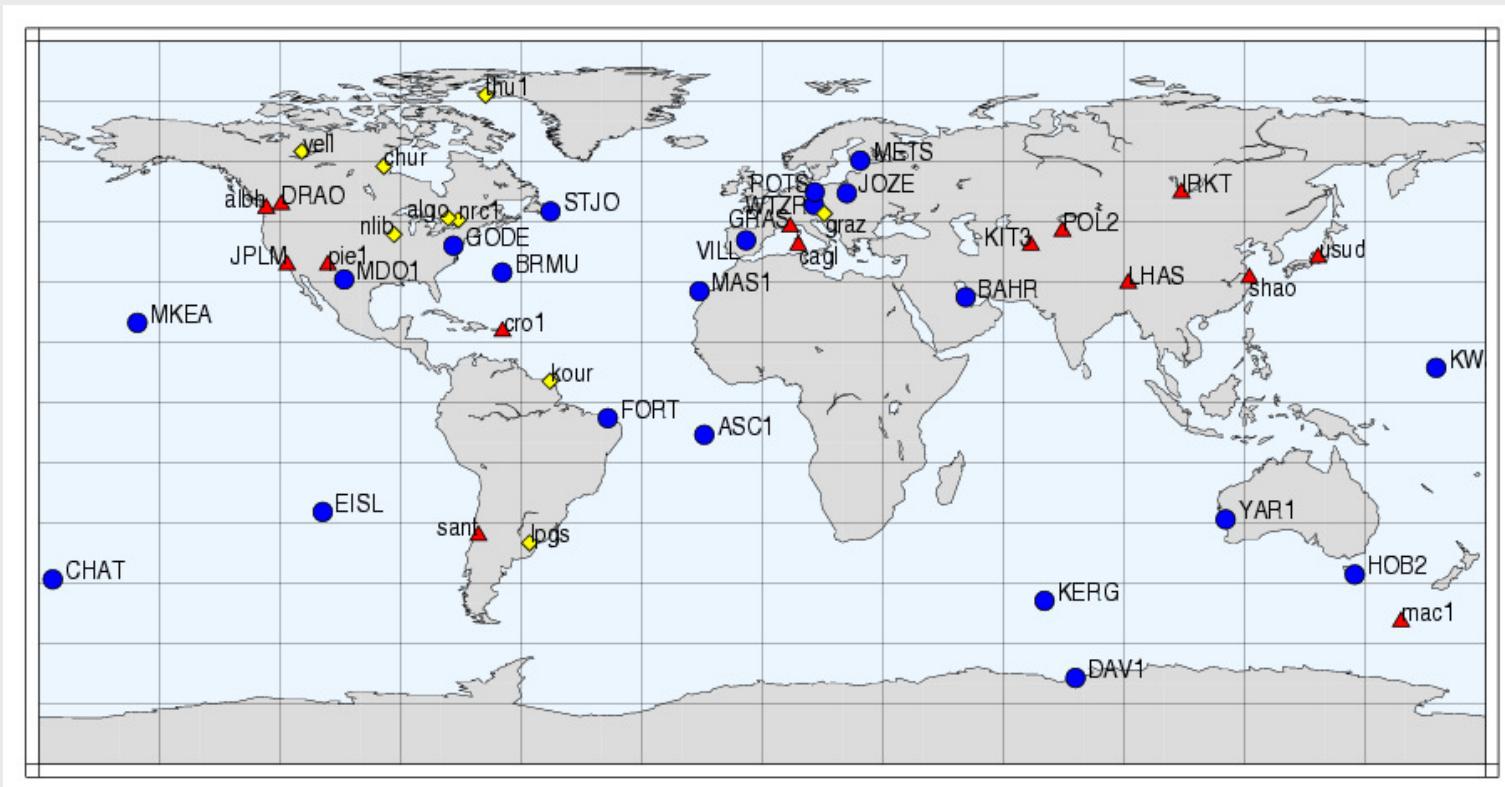
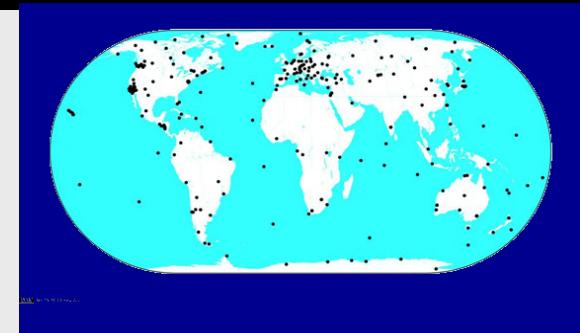
## GLOBK (combination & ref. frame)

- is used for combination of sub-networks and reference frame realization.
- Combination of our regional analysis with global products from SCRIPPS.
- Satellite orbits are given loose constraints in the quasi-observations - final coordinates are not (so much) affected by a priori orbit information.

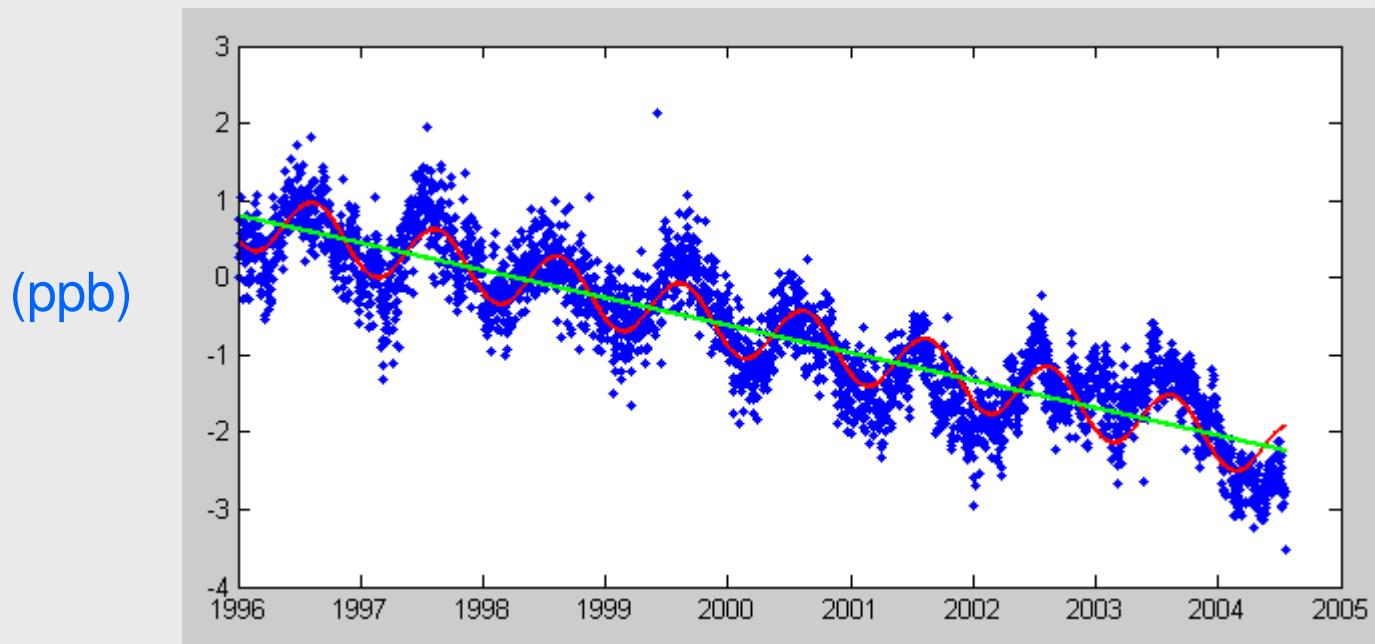


# Combination to get “global solution”

- Regional networks combined with global networks of “quasi-observations” from SOPAC
- stabilize to daily solutions in ITRF2000
- 44 “good” ITRF2000 stations used for stabilization
- 3 transl. + 3 rot. + 1 scale (daily)



# The scale in the stabilization



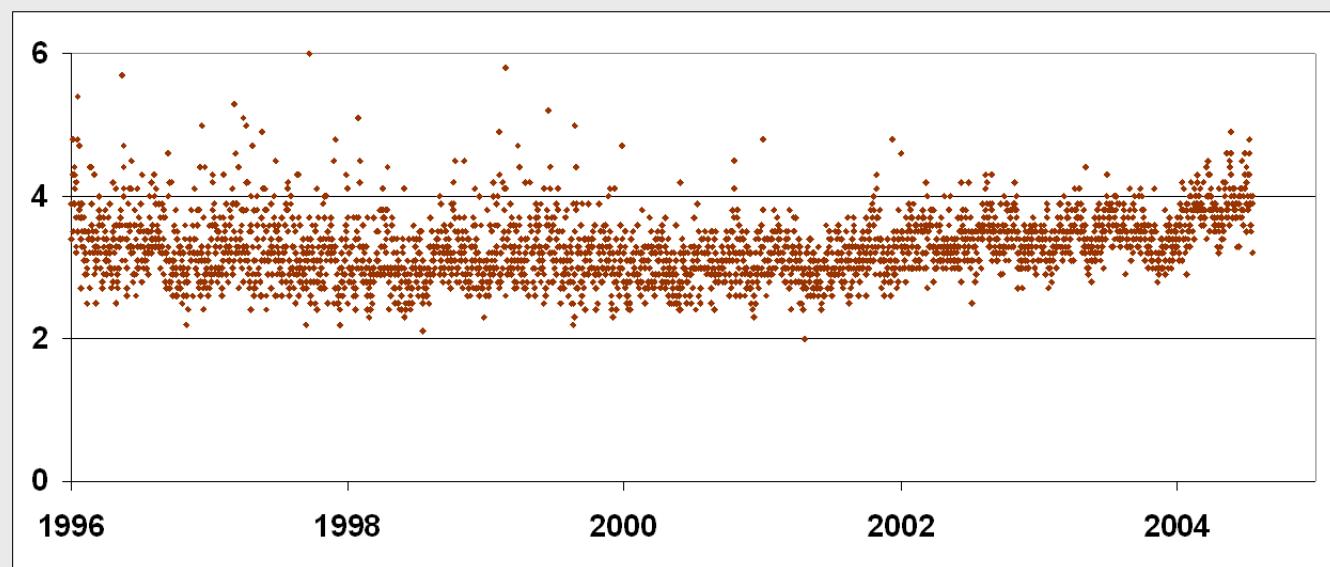
## Periodic effects in GPS time series

- Atmospheric mass loading
- Non-tidal ocean mass loading
- Snow and soil moisture mass loading
- Bedrock thermal expansion
- Glacier surge and internal ice flow
- Atmospheric modeling errors
- Phase center modeling and environmental influences

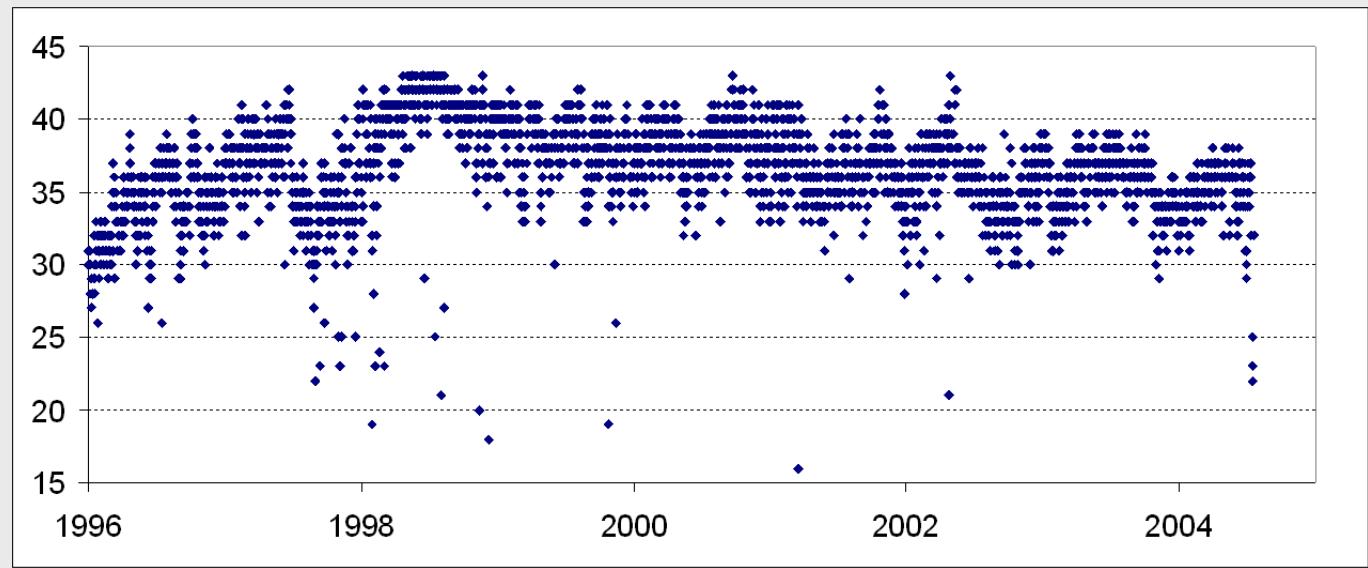


# Result of stabilization

Post-fit  
RMS (mm)



Number of  
sites used for  
stabilization

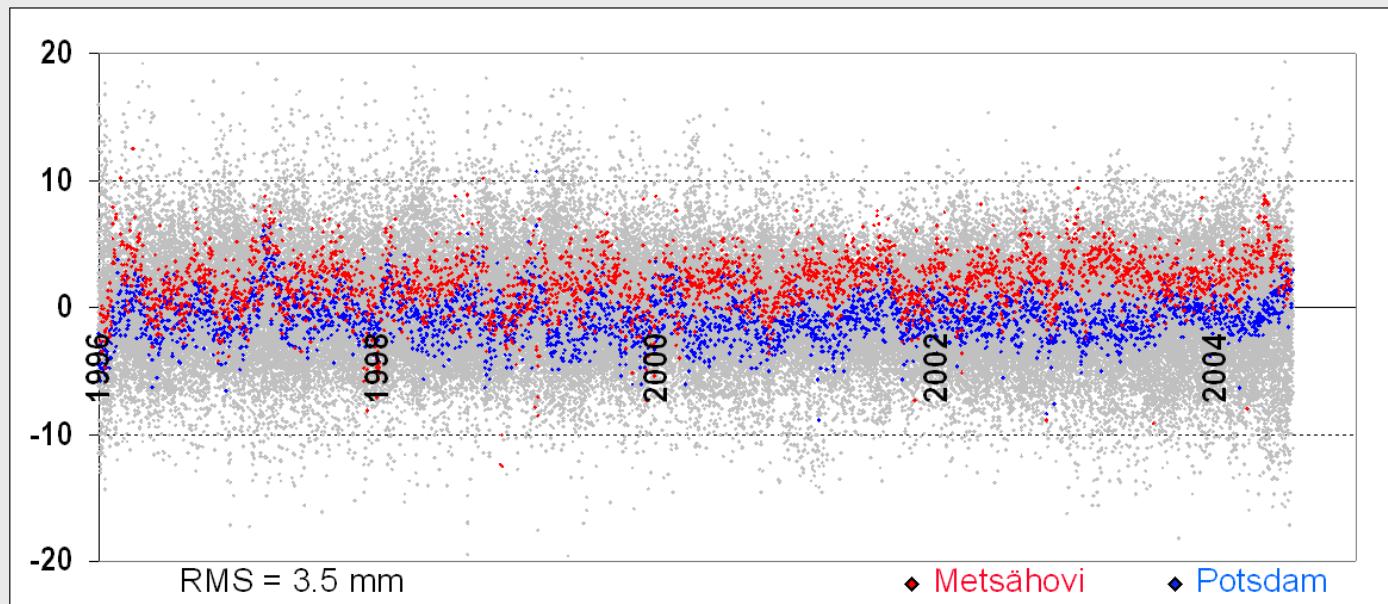


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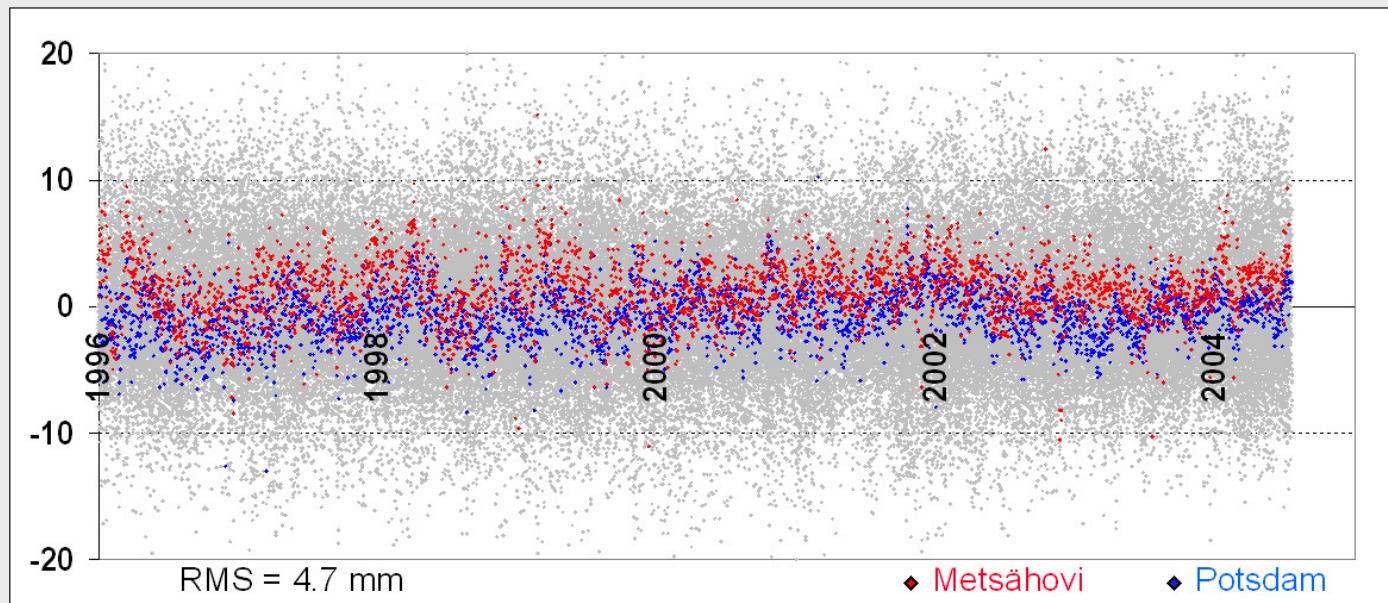


# Residuals at stabilization sites

North (mm)



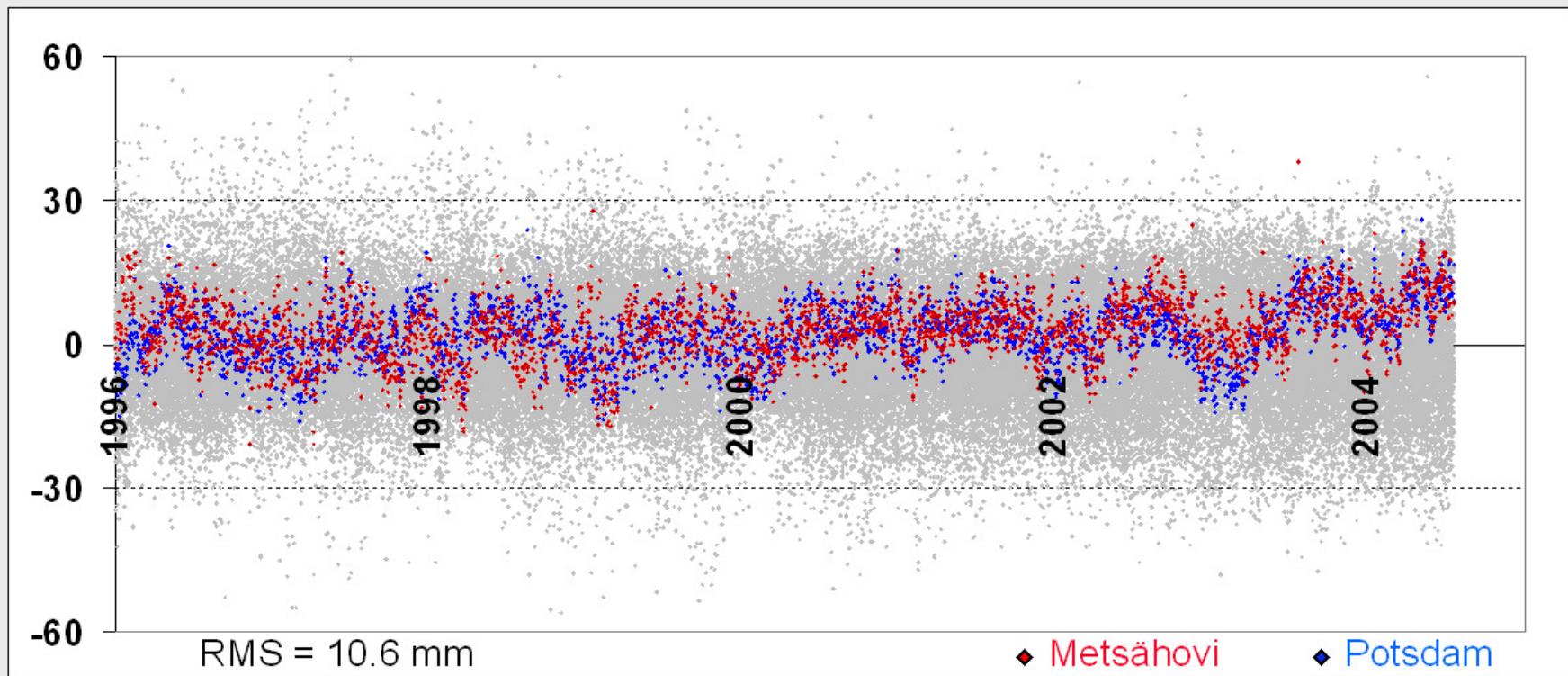
East (mm)



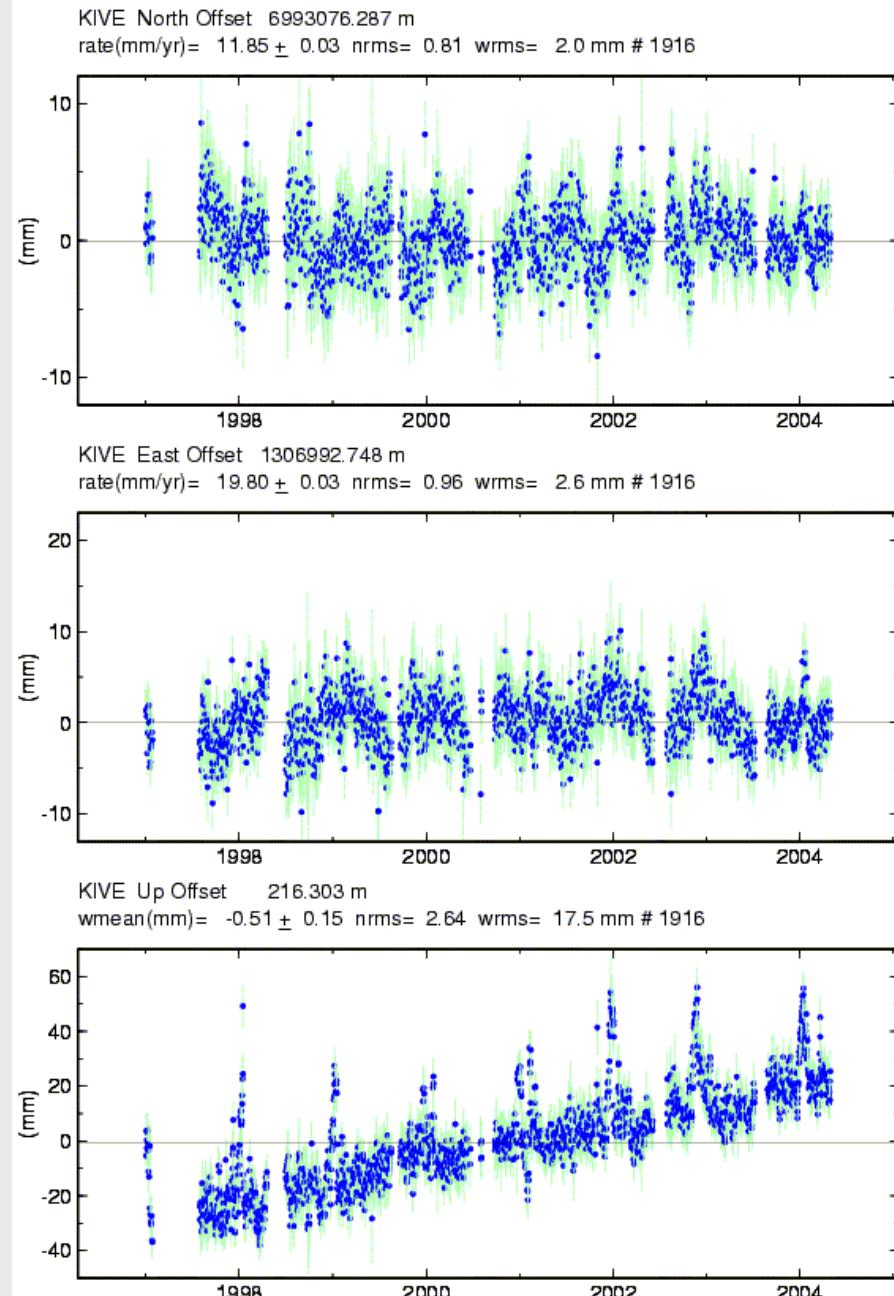
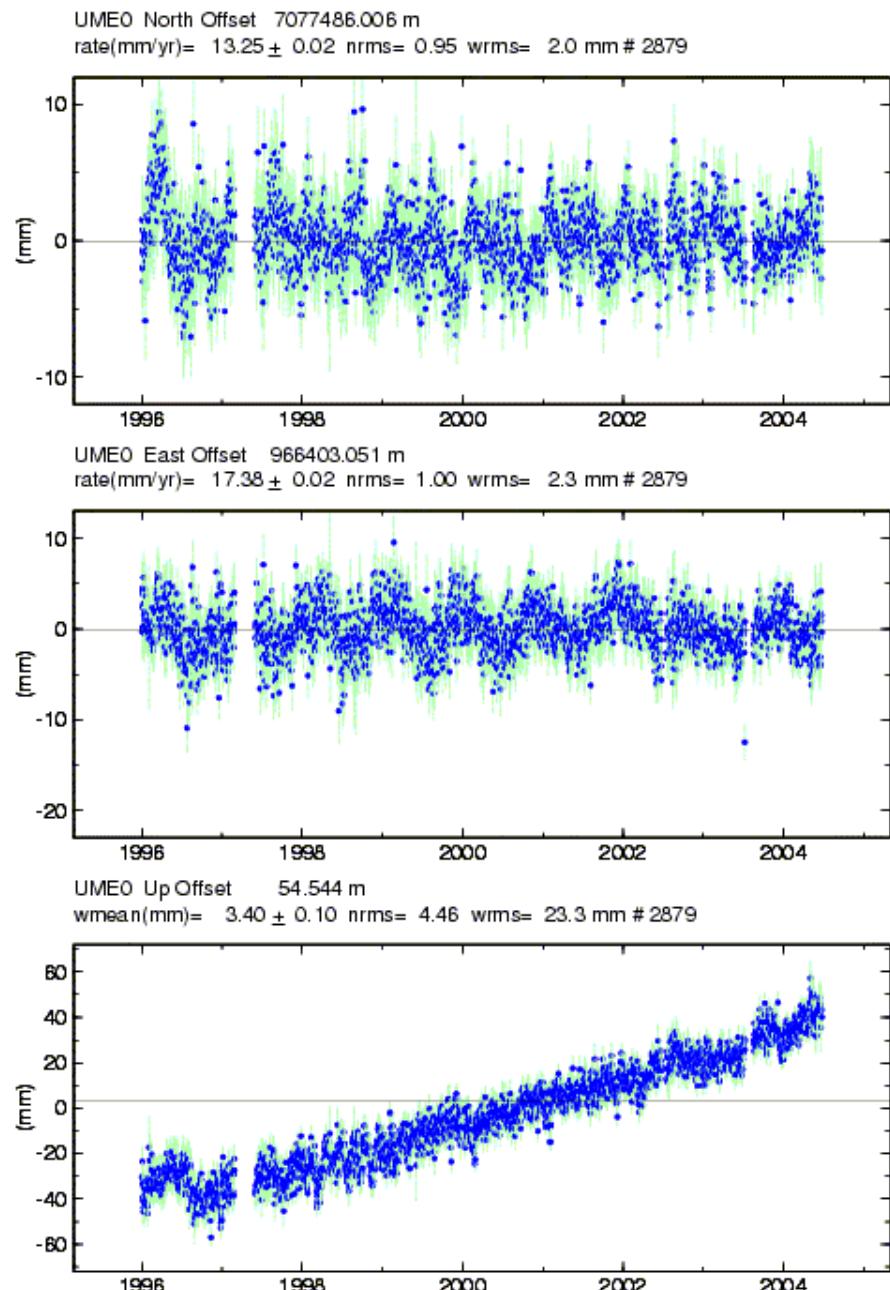
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# Residuals at stabilization sites

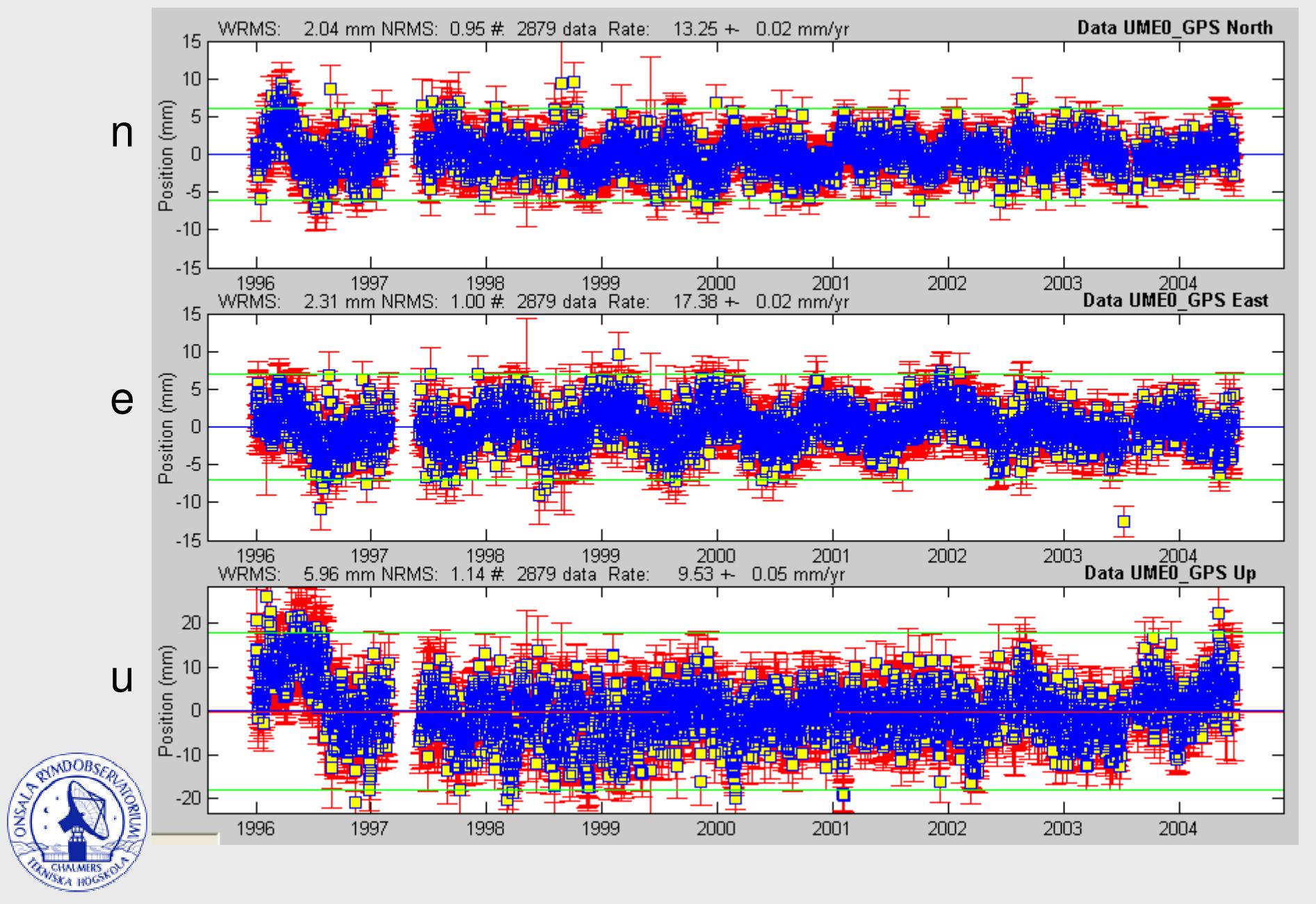
Up component (mm)



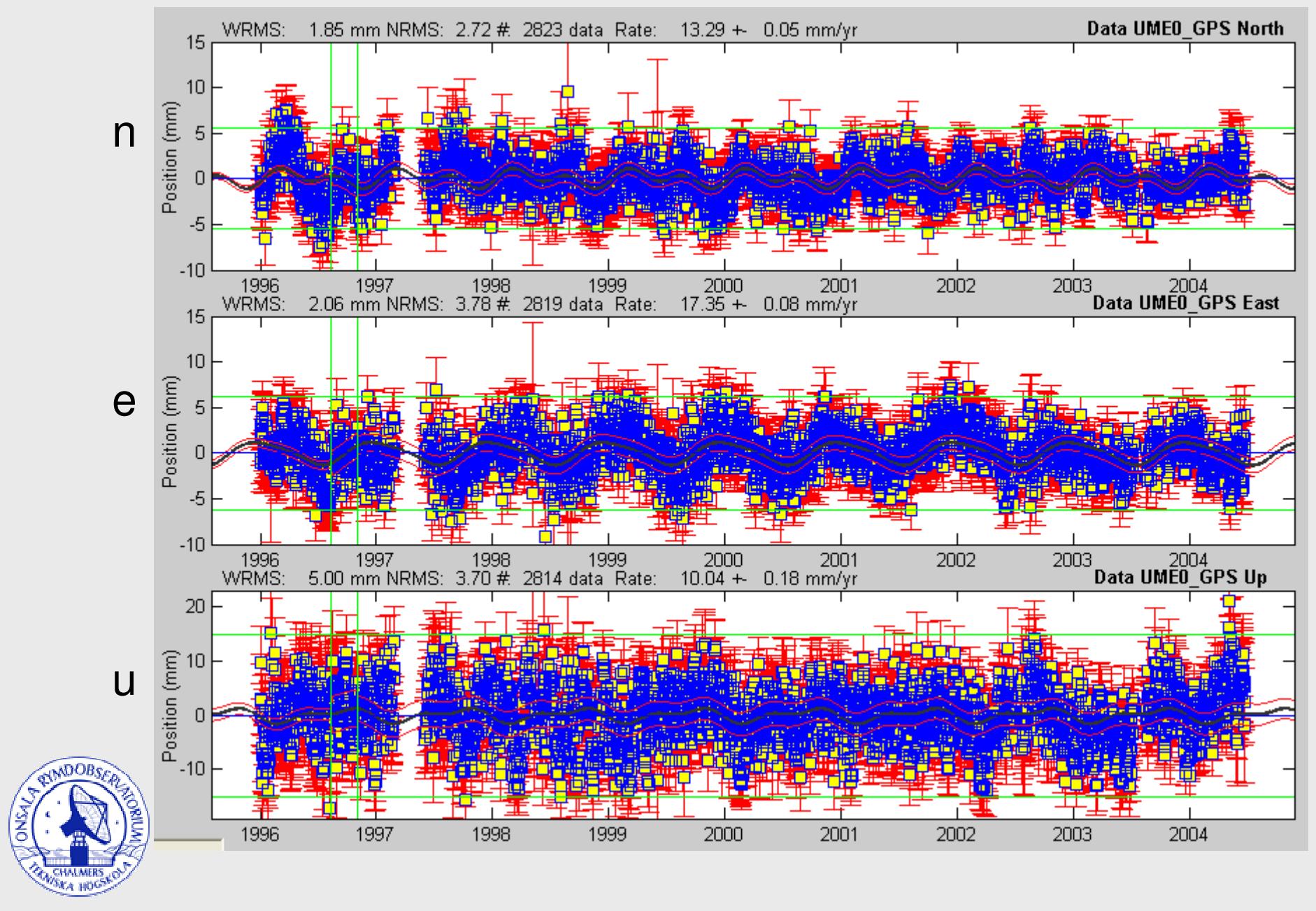
# Time series of GPS positions before editing



# Time series of Umeå



# Time series of Umeå: seasonal cycles, realistic $\sigma$



# Estimating realistic velocity uncertainties

Least square solution

$$\hat{X} = (A^T C^{-1} A)^{-1} A^T C^{-1} Y$$

$$\hat{C}_X = \hat{\sigma}_0^2 (A^T C^{-1} A)^{-1}$$

Estimated  $\sigma_0^2$

$$\hat{\sigma}_0^2 = \frac{V^T C^{-1} V}{N - np}$$

Assume 1<sup>st</sup> order GM process

$$v(i) = a^* v(i-1) + w(i); \quad 0 < a < 1$$

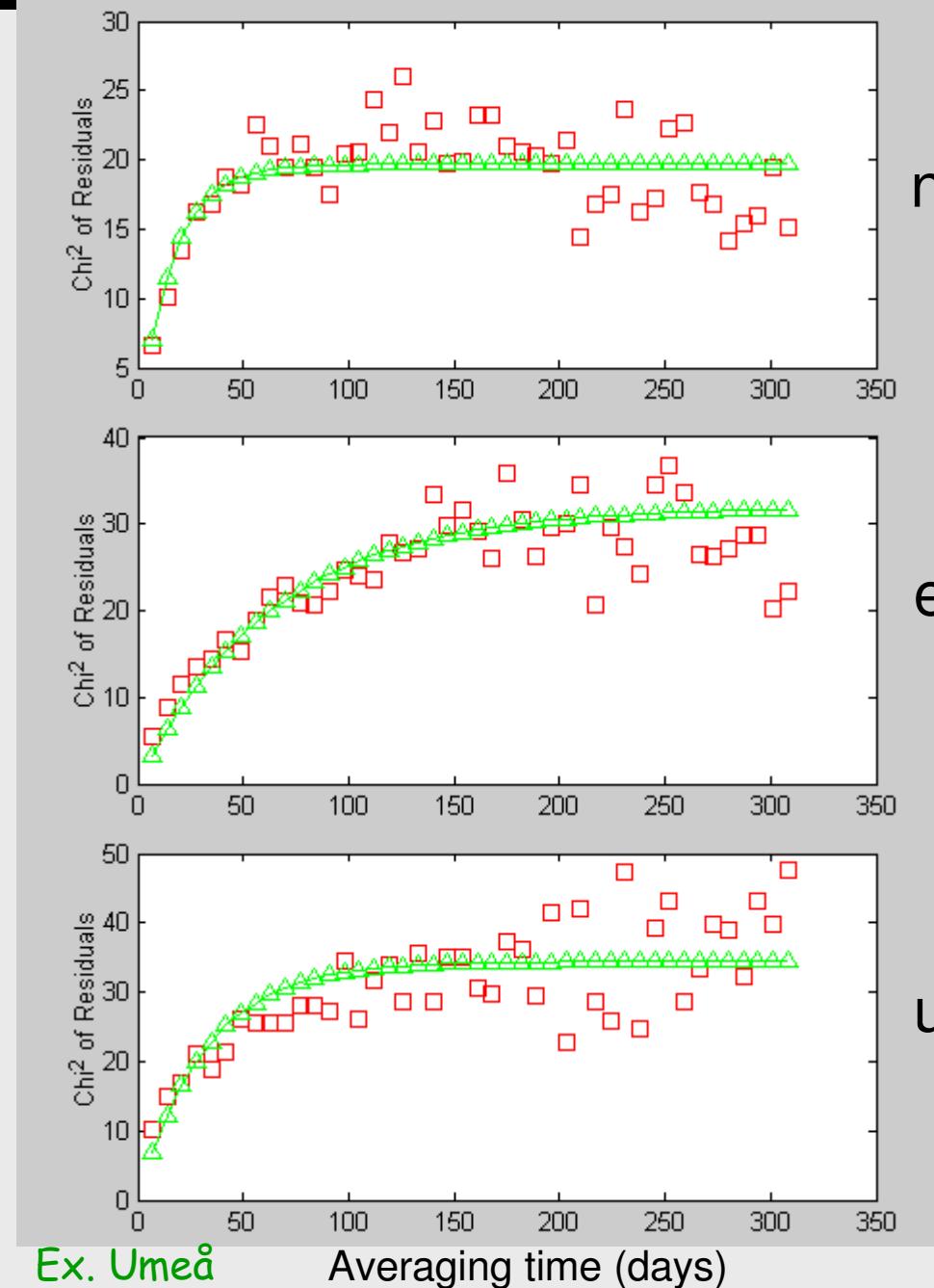
Compute weighted means of the residuals,  
including weights for the means;  
- then compute weighted scatter of the  
weighted means

$$\text{chi}^2/\text{dof} \text{ of mean} \sim \alpha \times (1 - \exp(-m/\tau))$$

$$\text{new } \hat{\sigma}_0^2 = \hat{\sigma}_0^2 \times \alpha$$

Averaging time

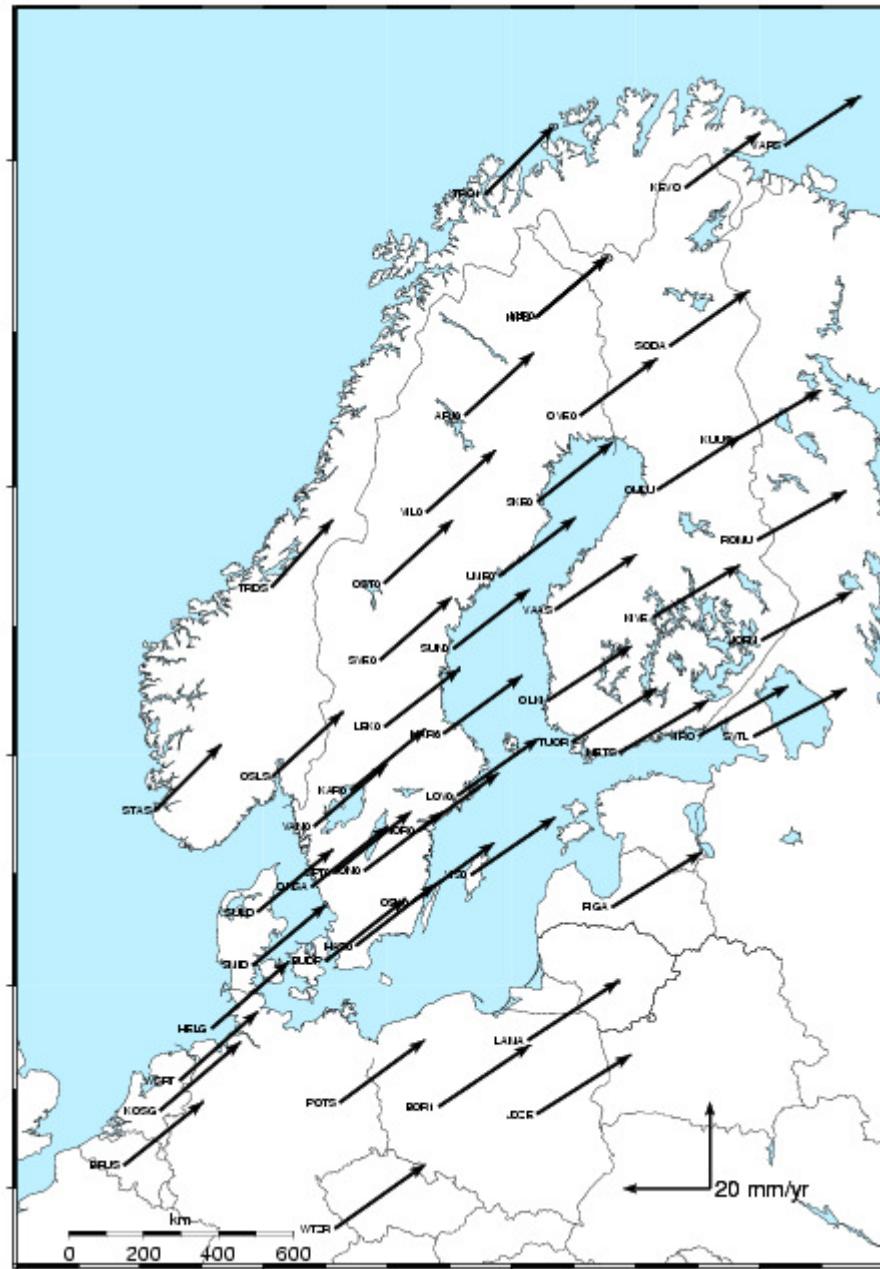
correlation  
time parameter



# Derived horizontal velocity field

Horizontal velocities in  
ITRF2000

we see the  
tectonic motion  
of the  
Eurasia tectonic plate



# Derived velocity field relative to Eurasia

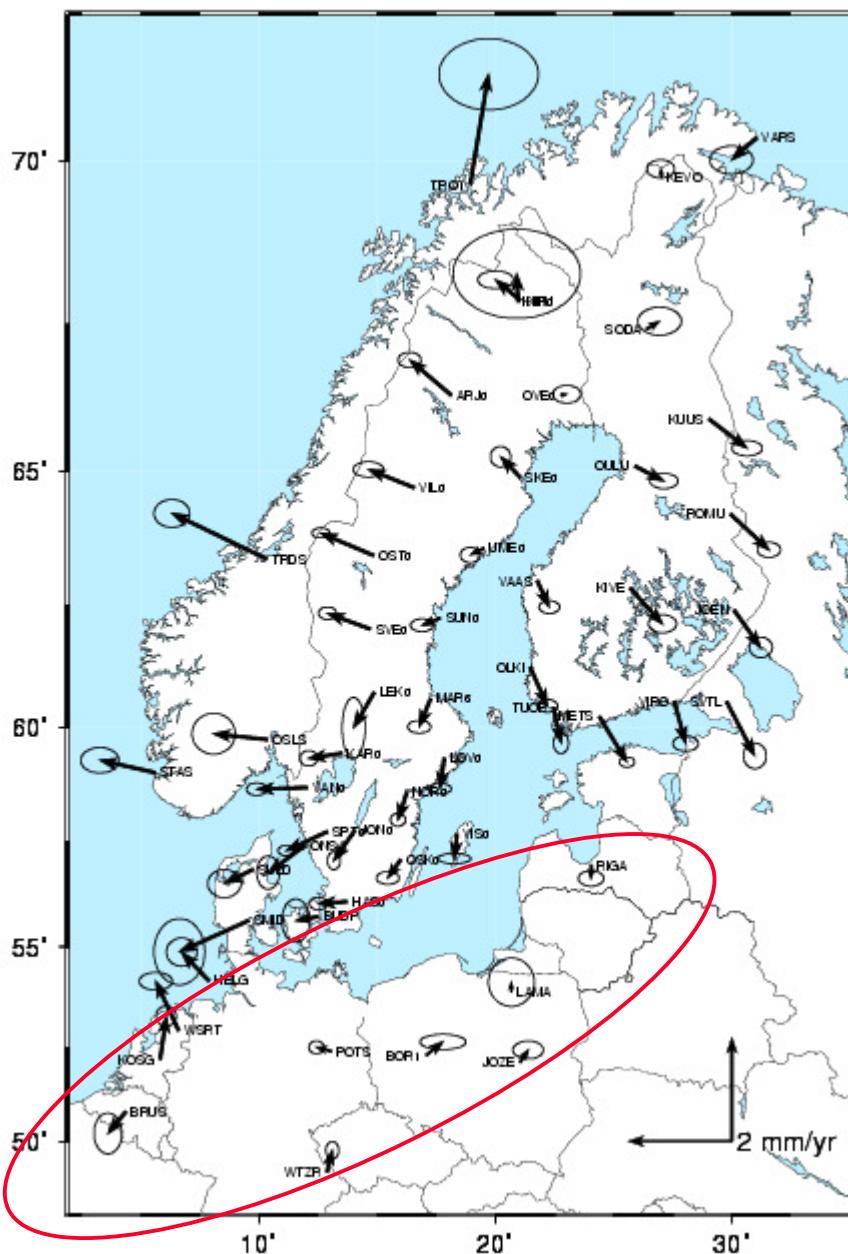
The Eurasia plate tectonic motion has been removed using the ITRF2000 Euler pole for Europe

RMS of velocity at 8 “stable European sites” 0.5 mm/yr

In case of:

- no deformations
  - correct Euler pole fore Europe  
(formal error  $\sim 0.6$  mm/yr)
  - and no errors in the GPS derived velocity field

... the RMS value should have been =0



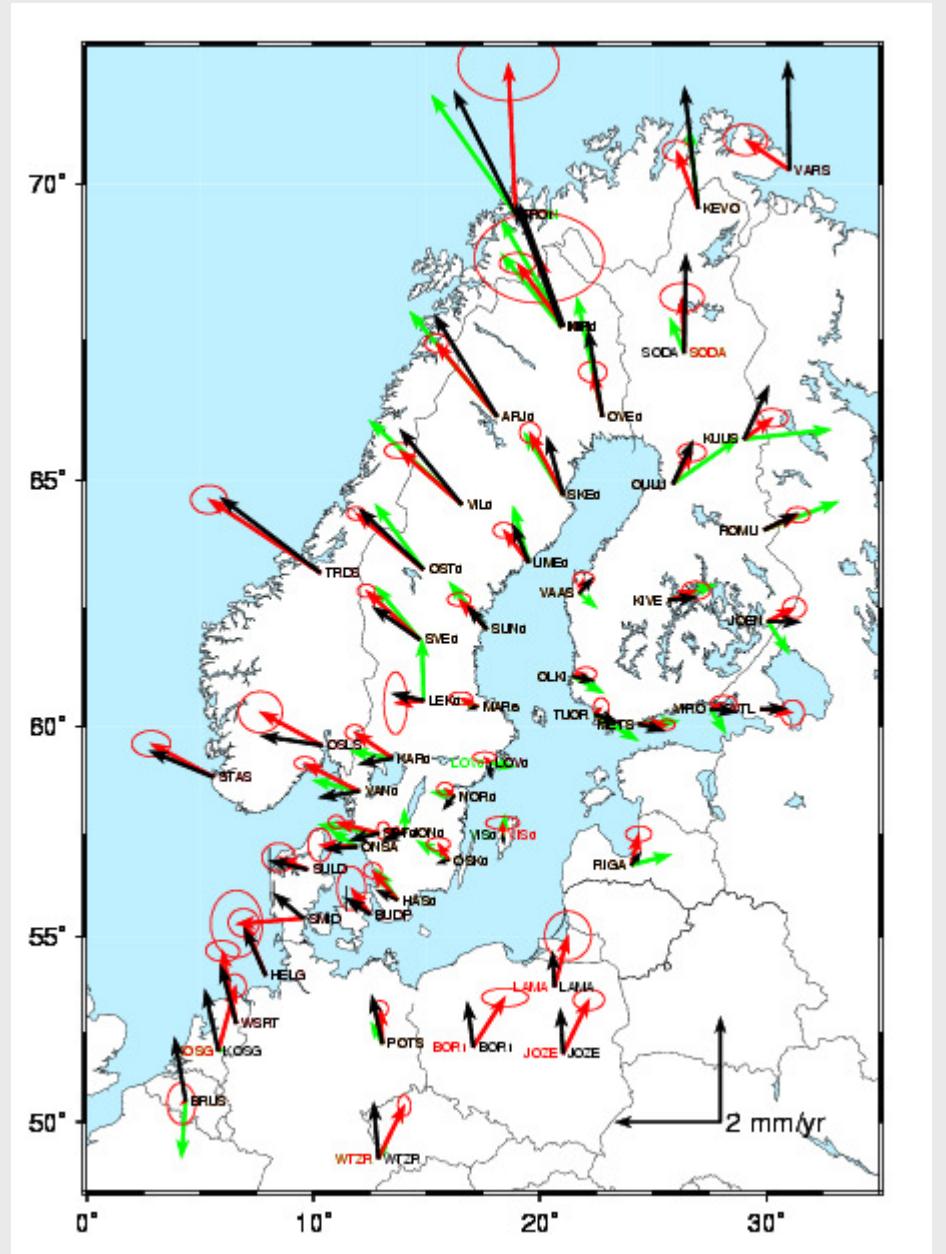
# Comparing with previous BIFROST and a model

The winter edited version of  
previous BIFROST solution  
(Johansson et al 2002, Scherneck et al 2002)

GIA model from Milne et al (2001)  
Ice history model from Lambeck  
120 km lithosphere,  
upper mantle visc.  $8 \times 10^{20}$  Pas  
lower mantle visc.  $1 \times 10^{22}$  Pas

This solution

Gamit to model:  
0.5 mm/yr ( $1\sigma$ ) using all 53 sites  
(BRUS, KIRU, KIR0, KEVO, TRO1,  
VARS)  $> 1$  mm/yr



# Vertical velocity

Comparing different land uplift estimates

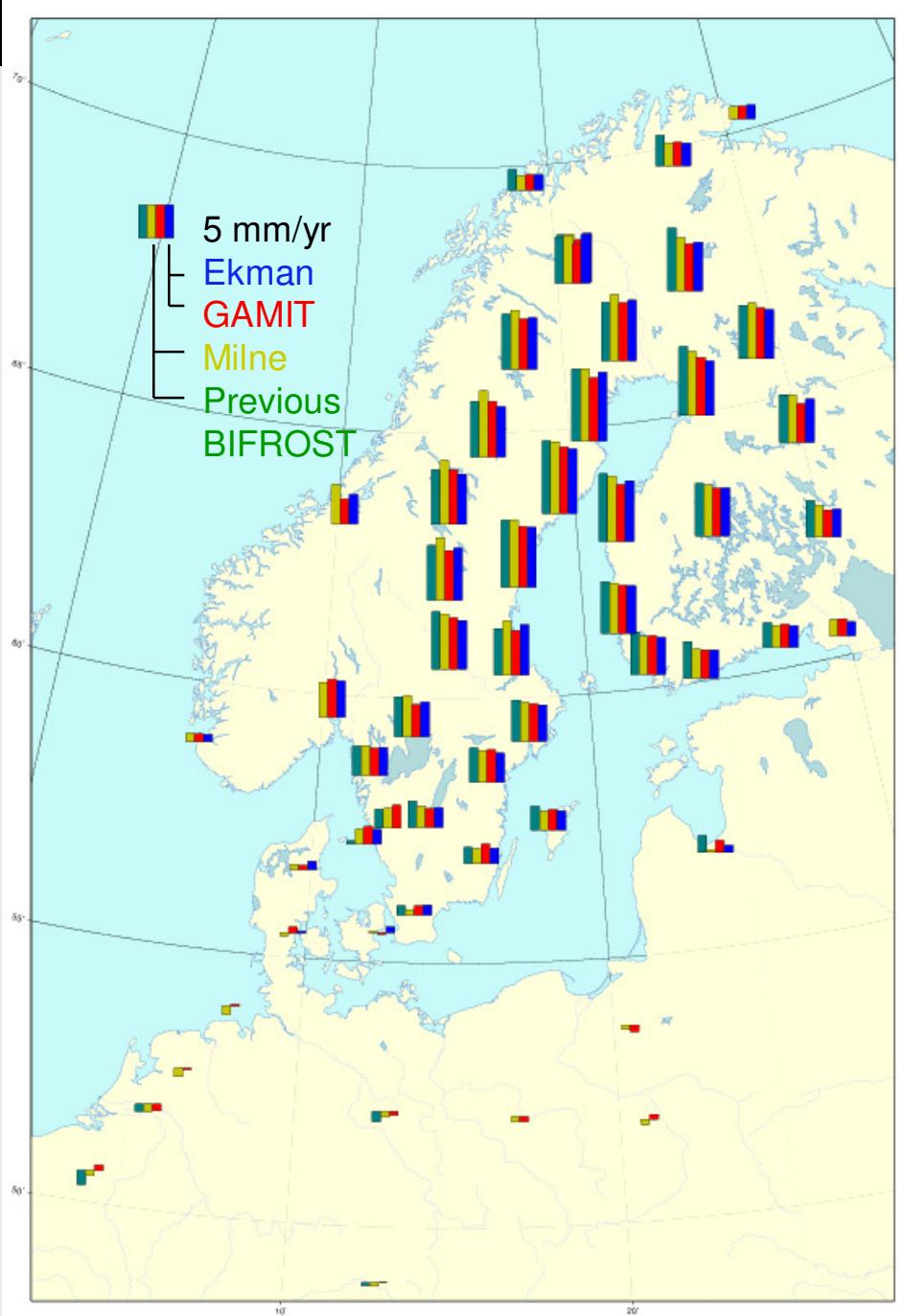
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This solution

Ekman (1998) based on:

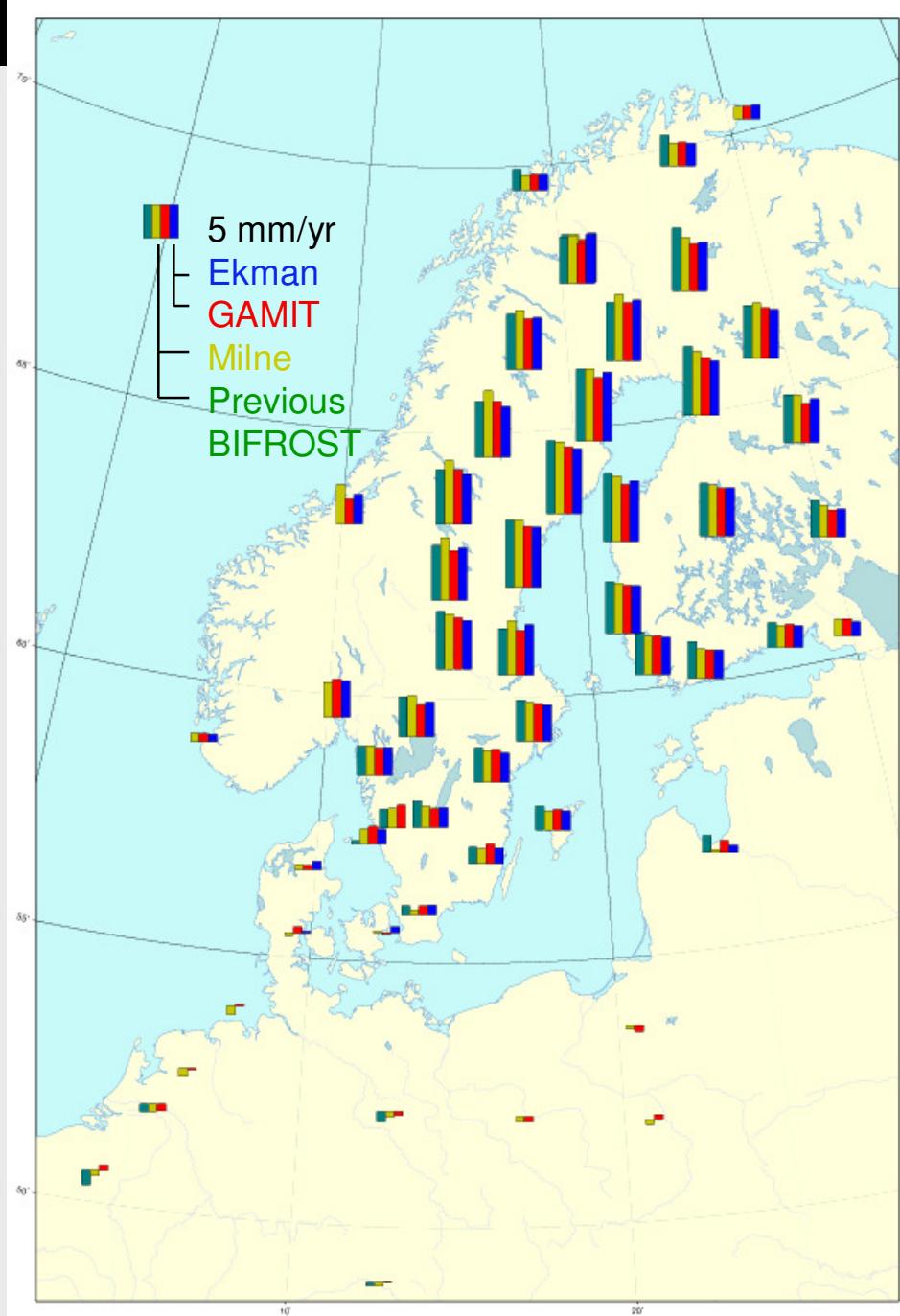
- mareographs and levellings,
- 1.2 mm/yr eustatic sea level rise
- change of the geoid based on Ekman & Mäkinen (1998)



# Vertical velocity

Differences to the  
GAMIT solution  
(mm/yr)

	mean	RMS
Previous BIFROST	0.5	1.0
Milne GIA model	0.3	0.9
Ekman	0.1	0.5
Ekman best stn.	0	0.4

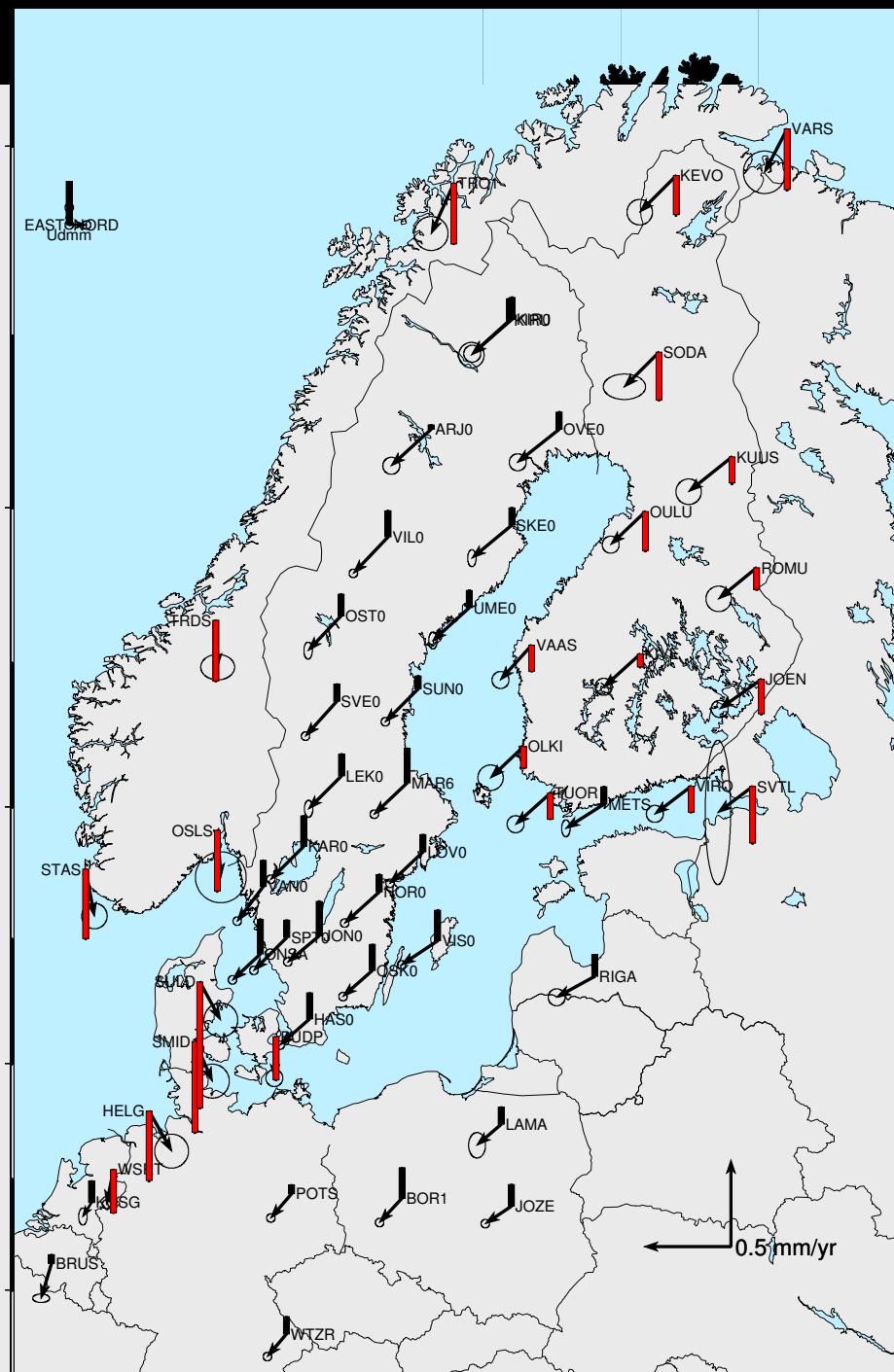


# 44 vs. 21 stabilization sites

Comparison between using 44 or 21 sites for reference frame realization,

Horizontal:  $\sim 0.2 \text{ mm/yr}$   
Vertical:  $\sim 0.1 \text{ mm/yr}$

However, systematic differences due to length of time series.



# Conclusion and outlook

- A new GPS derived 3D velocity field for the Fennoscandian GIA area presented
- Global adaptation to the ITRF2000 velocity field at sub-mm/yr level
- external assessment indicate
  - 0.2 mm/yr level ( $1\sigma$ ) horizontal
  - 0.5 mm/yr level ( $1\sigma$ ) vertically

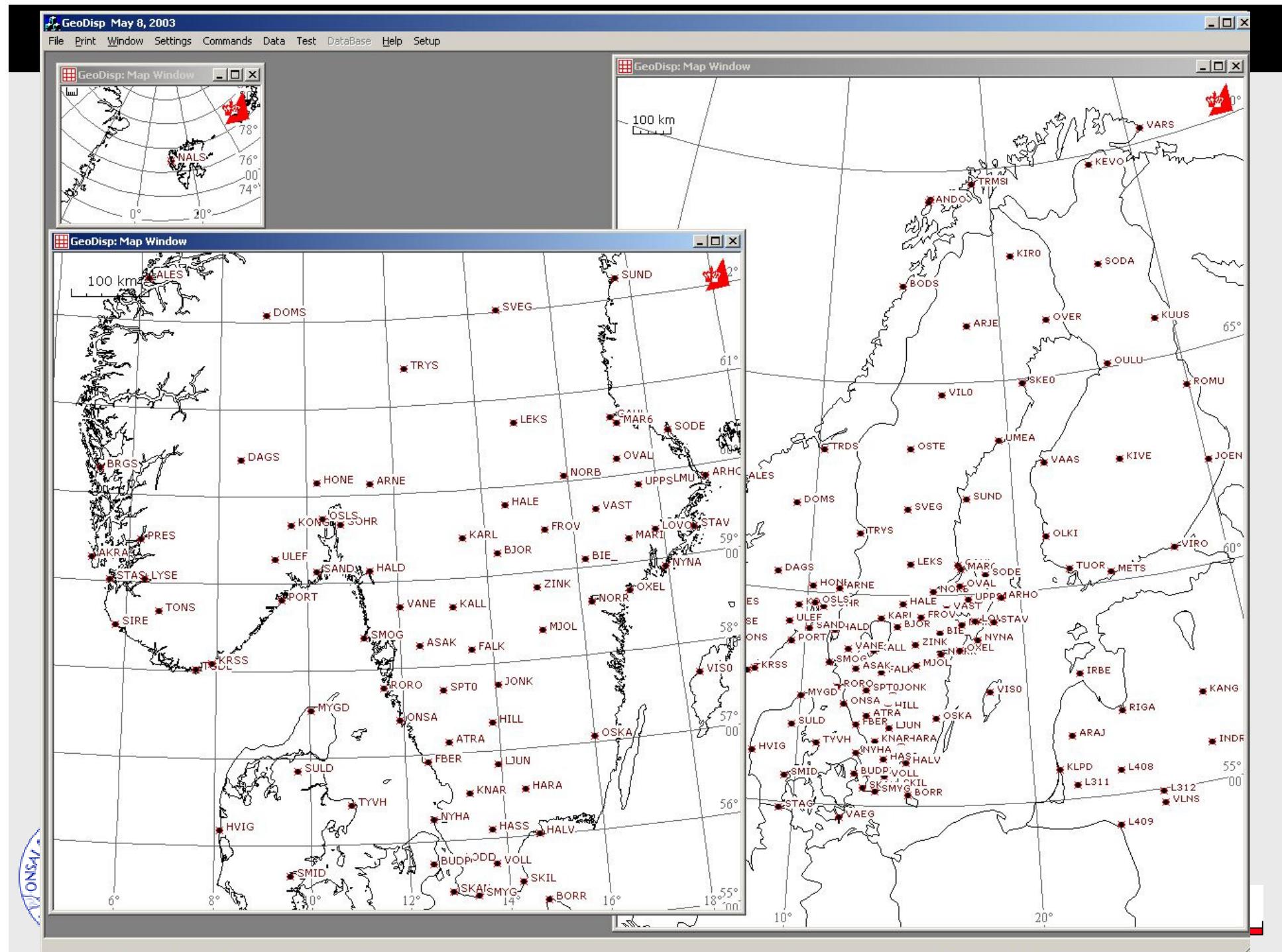
## EUREF implications:

- Vertical station velocities used in land uplift modeling for Nordic leveling work (Mäkinen, session 5)
- The signal (10 mm/yr) of the Fennoscandia GIA process can be modeled to 1mm/yr (90%), and better models foreseen;
- Intraplate deformations should be considered in future ETRS89 realizations, but is 1989 a good target epoch for this (Norway 1995, Finland 1997, Sweden 1999.5)??

## Next step:

- GPS analysis: 1993 to 2005, absolute calibrated antennas, higher order ionosphere effects, GIPSY (PPP and amb. Fix.), extended noise analysis...  
adjusting the GIA model using the improved velocity field.





# NKG 2003 vs. official ETRS89 realizations

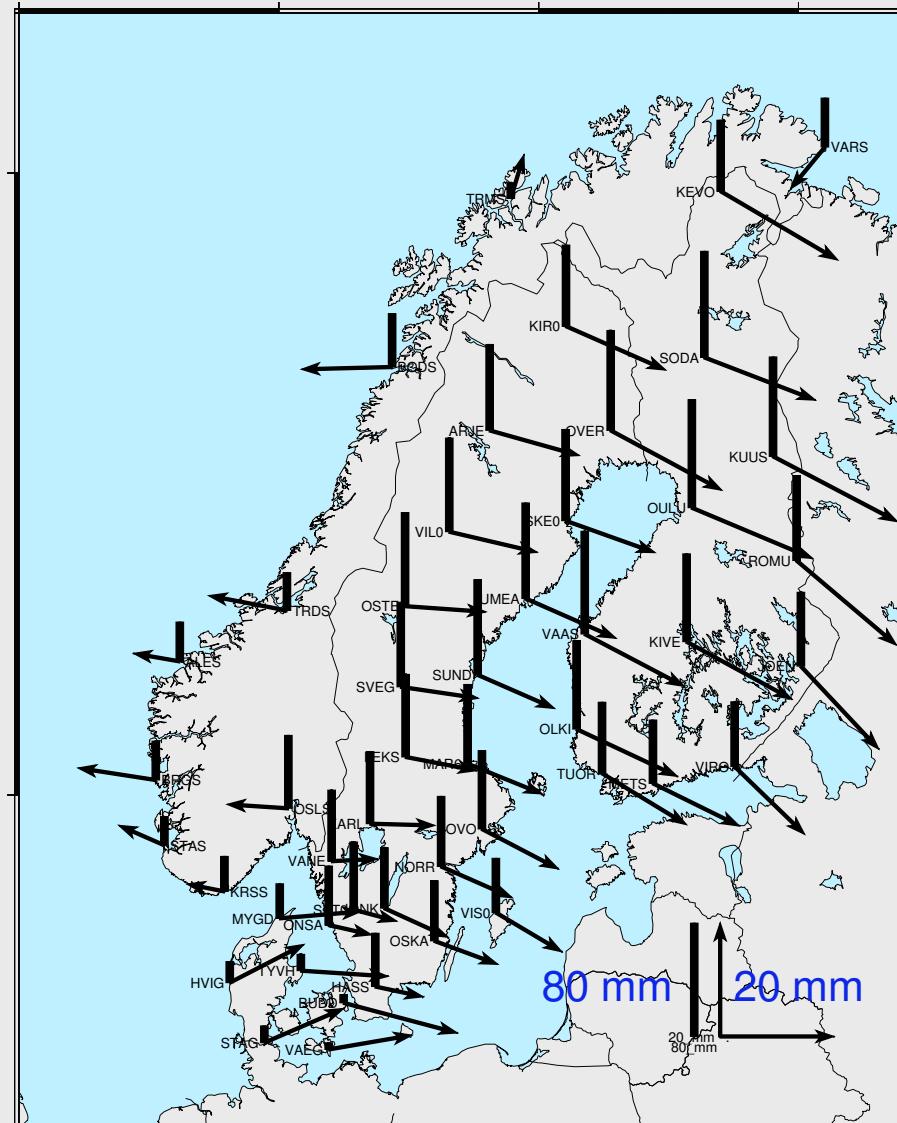
The NKG 2003 GPS campaign

- in ETRS89  
(Boucher & Altamimi MEMO)
- compared to official ETRS89 realizations

RMS n = 10 mm

RMS e = 19 mm

RMS u = 52 mm



# NKG 2003 vs. official ETRS89 (with internal deformations)

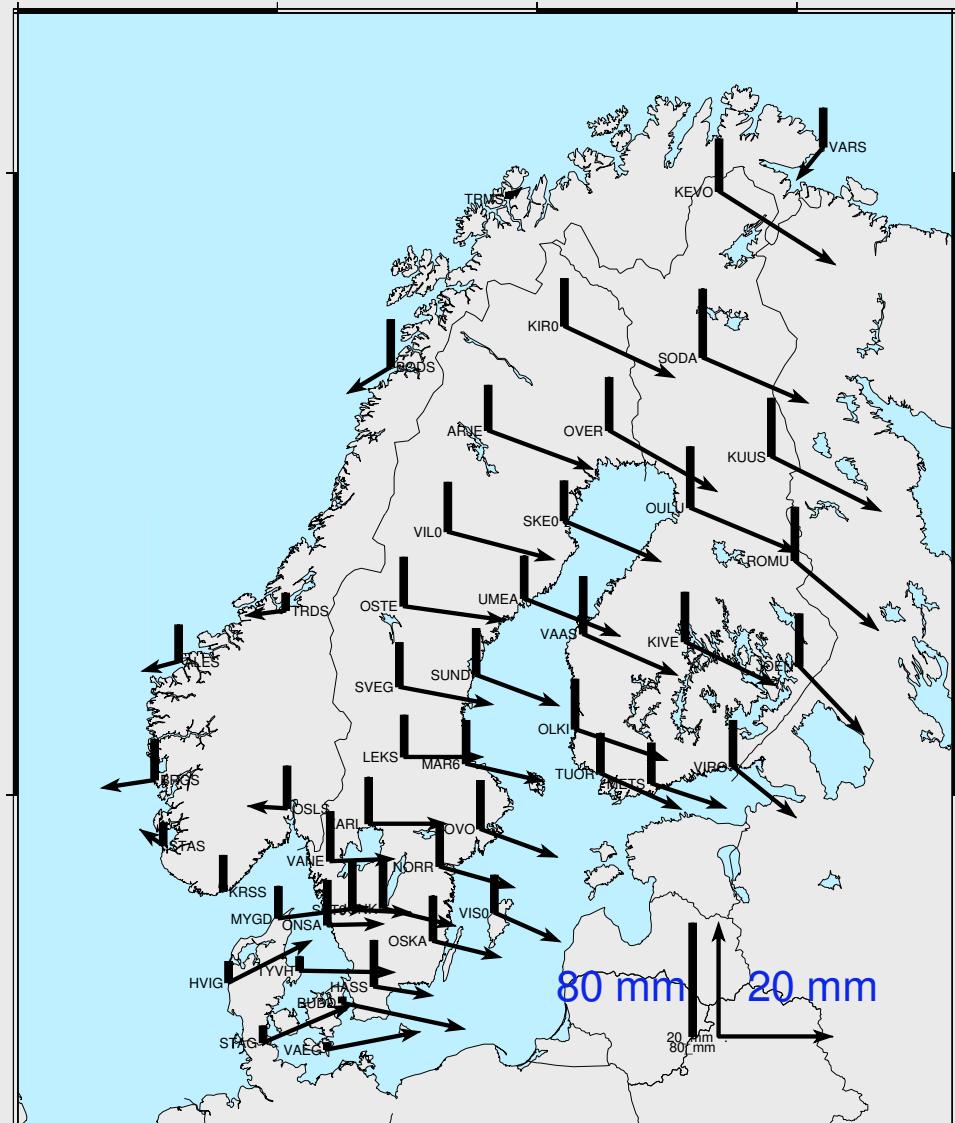
The NKG 2003 GPS campaign

- in ETRS89  
(Boucher & Altamimi MEMO)
- internal deformations reduced to year 2000 using computed station velocities
- compared to official ETRS89 realizations

RMS n = 6 mm

RMS e = 14 mm

RMS u = 30 mm



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# NKG 2003 vs. SWEREF 99 (station velocities 2003.75 - 1999.5)

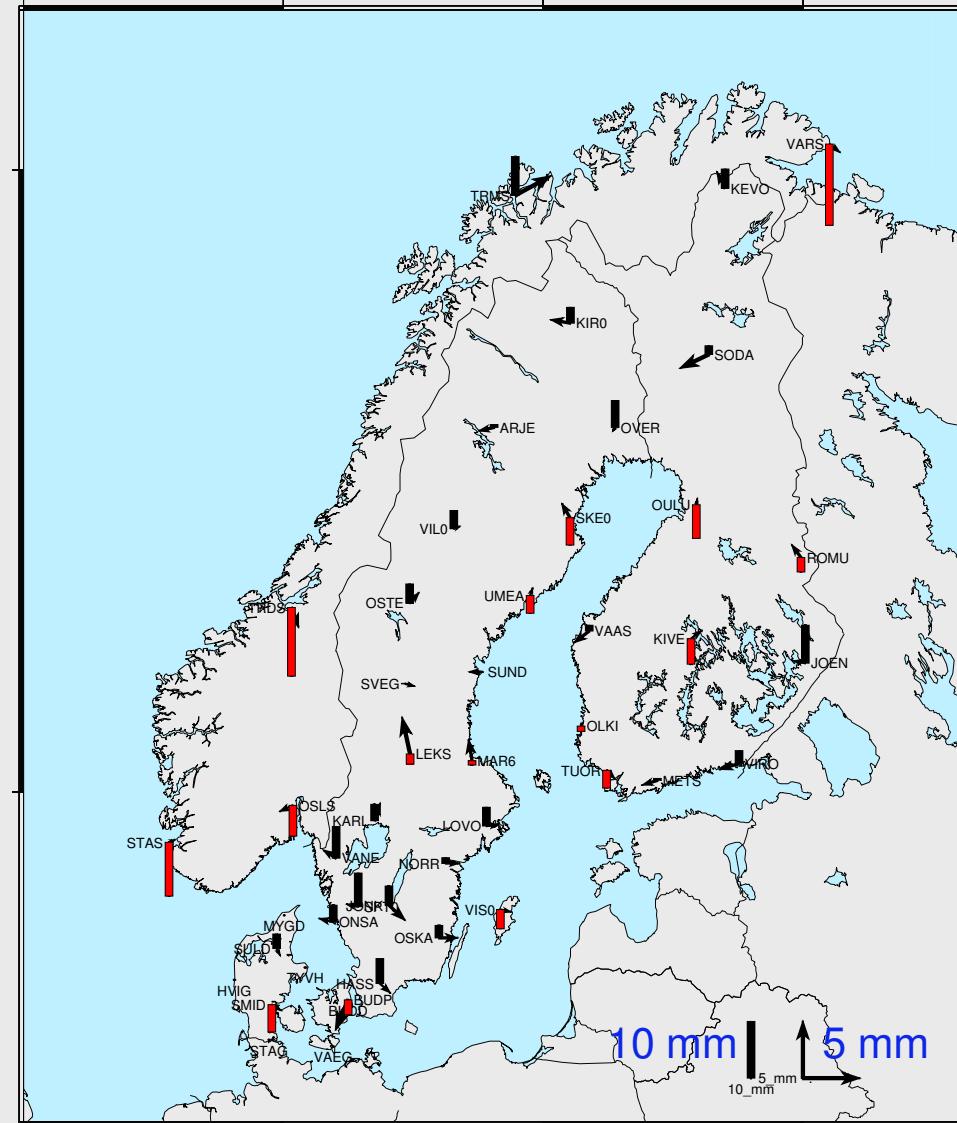
The NKG 2003 GPS campaign

- internal deformations reduced to 1999.5 using computed station velocities
- transformed (7-par.) to the SWEREF 99 GPS campaign

RMS n = 1.1mm

RMS e = 1.2 mm

RMS u = 5.2 mm



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# NKG 2003 vs. SWEREF 99 (GIA model 2003.75 - 1999.5)

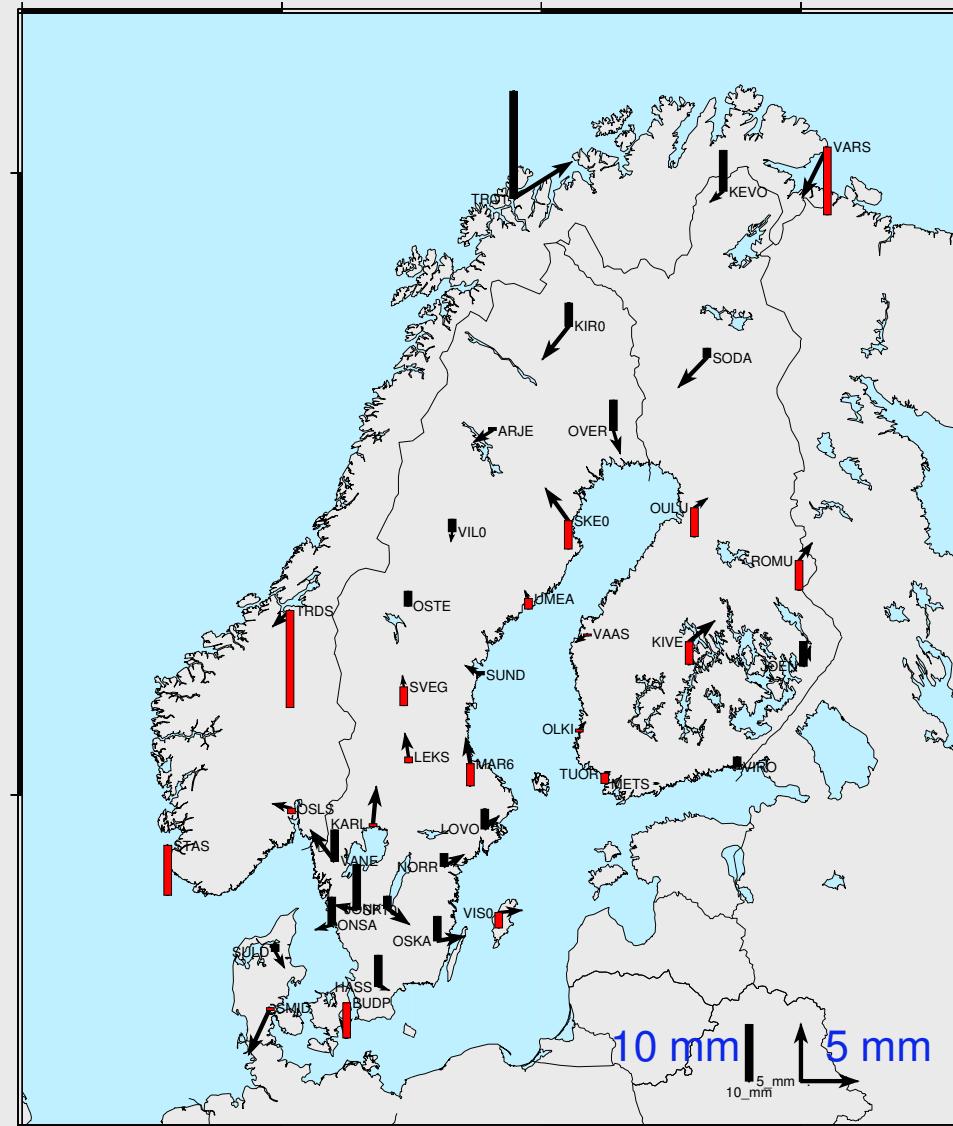
The NKG 2003 GPS campaign

- internal deformations reduced to 1999.5 using GIA model  
(Milne et al 2001)
- transformed (7-par.) to the SWEREF 99 GPS campaign

RMS n = 1.9 mm

RMS e = 1.6 mm

RMS u = 5.9 mm



# Conclusion and outlook

- A new GPS derived 3D velocity field for the Fennoscandian GIA area presented
- Global adaptation to the ITRF2000 velocity field at sub-mm/yr level
- external assessment indicate
  - 0.2 mm/yr level ( $1\sigma$ ) horizontal
  - 0.5 mm/yr level ( $1\sigma$ ) vertically

EUREF implications:

- Correction for internal deformations needed
- Due to (ignored) internal deformations, and height system epoch of year 2000:
  - an epoch of intraplate deformations of ETRS89 at year 2000 may better suit users of ETRS89

Next step:

- GPS analysis: 1993 to 2005, absolute calibrated antennas, higher order ionosphere effects, GIPSY (PPP and amb. Fix.)
- adjusting the GIA model using the improved velocity field.

