

# The International Terrestrial Reference System and ETRS89: Part II : ITRS & ETRS89 relationship

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# **International Terrestrial Reference System (ITRS)**

# International Terrestrial Reference System (ITRS): Definition (IERS Conventions)

- **Origin:** Center of mass of the whole Earth, including oceans and atmosphere
- **Unit of length:** meter SI, consistent with TCG (Geocentric Coordinate Time)
- **Orientation:** consistent with BIH (Bureau International de l'Heure) orientation at 1984.0.
- **Orientation time evolution:** ensured by using a No-Net-Rotation-Condition w.r.t. horizontal tectonic motions over the whole Earth

$$h = \int_C \mathbf{X} \times \mathbf{V} dm = 0$$

# How the ITRF is constructed ?

- **Input :**

- Time series of mean station positions (at weekly or daily sampling) and daily EOPs from the 4 techniques
- Local ties in co-location sites

- **Output :**

- Station positions at a reference epoch and linear velocities
- Earth Orientation Parameters

## Combination model

$$\left\{ \begin{array}{l} X_s^i = X_c^i + (t_s^i - t_0) \dot{X}_c^i \\ \quad + T_k + D_k X_c^i + R_k X_c^i \\ \quad + (t_s^i - t_k) [\dot{T}_k + \dot{D}_k X_c^i + \dot{R}_k X_c^i] \\ \\ \dot{X}_s^i = \dot{X}_c^i + \dot{T}_k + \dot{D}_k X_c^i + \dot{R}_k X_c^i \end{array} \right.$$

$$\left\{ \begin{array}{l} x_s^p = x_c^p + R2_k \\ y_s^p = y_c^p + R1_k \\ UT_s = UT_c - \frac{1}{f} R3_k \\ \dot{x}_s^p = \dot{x}_c^p \\ \dot{y}_s^p = \dot{y}_c^p \\ LOD_s = LOD_c \end{array} \right.$$

# Co-location site

- Site where two or more instruments are operating
- Surveyed in three dimensions, using classical or GPS geodesy

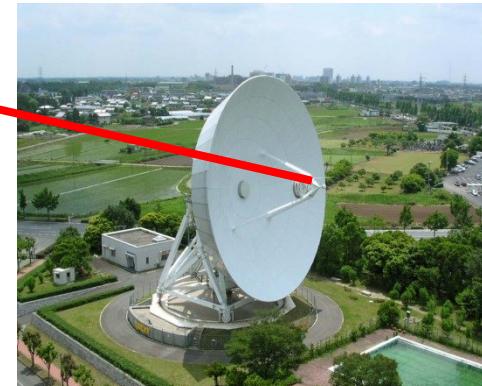


$$DX_{(GPS, VLBI)} = X_{VLBI} - X_{GPS}$$

SLR/LLR



GNSS

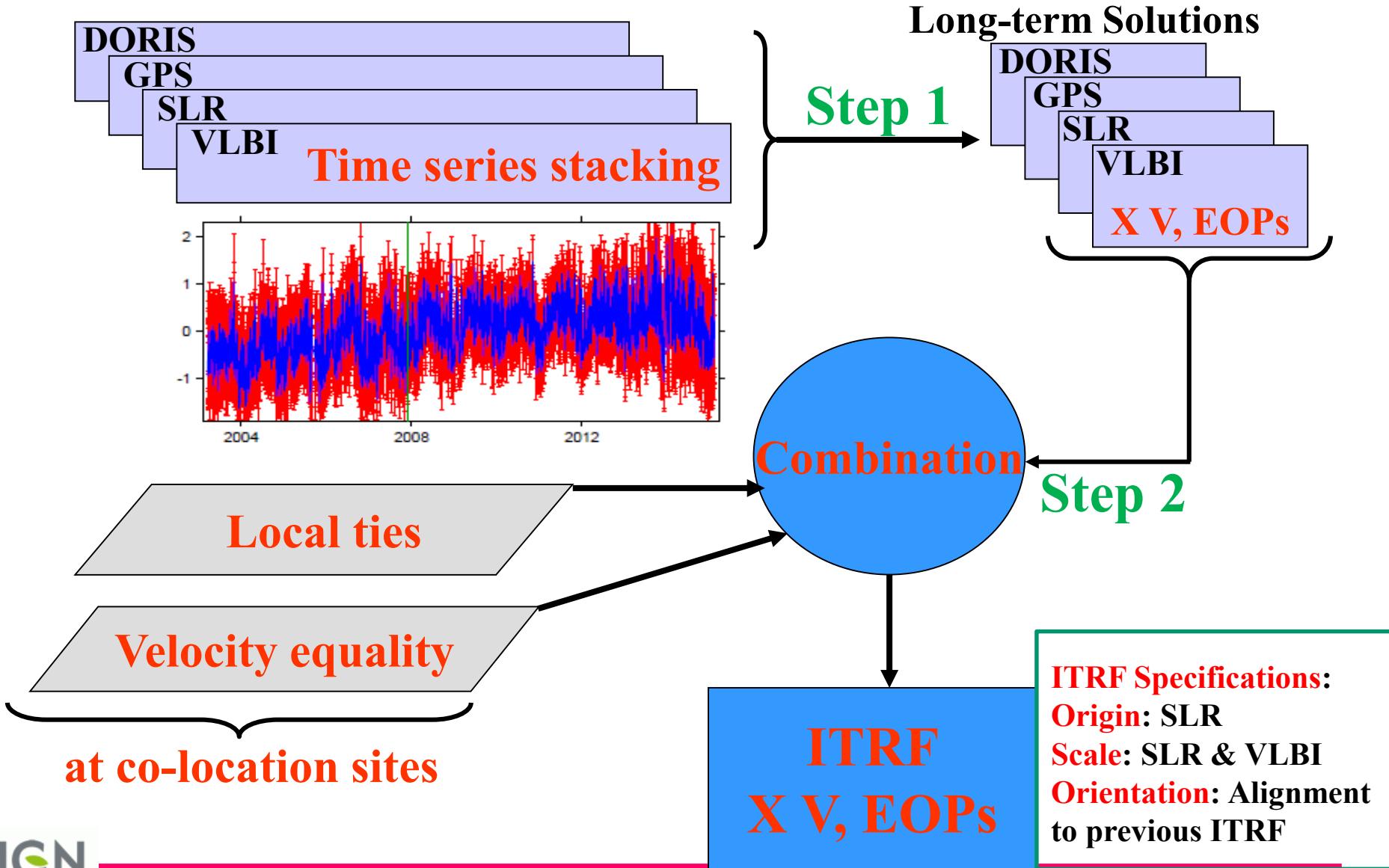


VLBI



DORIS

# ITRF Construction



# ITRF transformation parameters

Table 4.1: Transformation parameters from ITRF2008 to past ITRFs. “ppb” refers to parts per billion (or  $10^{-9}$ ). The units for rates are understood to be “per year.”

ITRF								
Solution	T1 (mm)	T2 (mm)	T3 (mm)	D (ppb)	R1 (mas)	R2 (mas)	R3 (mas)	Epoch
ITRF2005	-2.0	-0.9	-4.7	0.94	0.00	0.00	0.00	2000.0
rates	0.3	0.0	0.0	0.00	0.00	0.00	0.00	
ITRF2000	-1.9	-1.7	-10.5	1.34	0.00	0.00	0.00	2000.0
rates	0.1	0.1	-1.8	0.08	0.00	0.00	0.00	
ITRF97	4.8	2.6	-33.2	2.92	0.00	0.00	0.06	2000.0
rates	0.1	-0.5	-3.2	0.09	0.00	0.00	0.02	
ITRF96	4.8	2.6	-33.2	2.92	0.00	0.00	0.06	2000.0
rates	0.1	-0.5	-3.2	0.09	0.00	0.00	0.02	
ITRF94	4.8	2.6	-33.2	2.92	0.00	0.00	0.06	2000.0
rates	0.1	-0.5	-3.2	0.09	0.00	0.00	0.02	
ITRF93	-24.0	2.4	-38.6	3.41	-1.71	-1.48	-0.30	2000.0
rates	-2.8	-0.1	-2.4	0.09	-0.11	-0.19	0.07	
ITRF92	12.8	4.6	-41.2	2.21	0.00	0.00	0.06	2000.0
rates	0.1	-0.5	-3.2	0.09	0.00	0.00	0.02	
ITRF91	24.8	18.6	-47.2	3.61	0.00	0.00	0.06	2000.0
rates	0.1	-0.5	-3.2	0.09	0.00	0.00	0.02	
ITRF90	22.8	14.6	-63.2	3.91	0.00	0.00	0.06	2000.0
rates	0.1	-0.5	-3.2	0.09	0.00	0.00	0.02	
ITRF89	27.8	38.6	-101.2	7.31	0.00	0.00	0.06	2000.0
rates	0.1	-0.5	-3.2	0.09	0.00	0.00	0.02	
ITRF88	22.8	2.6	-125.2	10.41	0.10	0.00	0.06	2000.0
rates	0.1	-0.5	-3.2	0.09	0.00	0.00	0.02	

# Access to the ITRF and the IGS role (1/2)

- How to express a GNSS network in the ITRF using IGS products (orbit, clocks, ERP: all expressed in the ITRF) ?
- Select a reference set of ITRF/IGS stations and collect RINEX data from IGS data centers;
- Process your stations together with ITRF/IGS ones:
- Fix IGS orbits, clocks and ERPs
- Eventually, add minimum constraints conditions in the processing:

$$\boxed{X_R = X_c + A\theta} \xrightarrow{\theta = \theta} \boxed{(A^T A)^{-1} A^T (X_R - X_c) = 0}$$

↑                    ↑  
ITRF                Your Solution

## Access to the ITRF and the IGS role (2/2)

==> Your solution will be expressed in the ITRFyy  
consistent with IGS orbits

- Propagate official ITRF station positions at the central epoch ( $t_c$ ) of the observations:

$$X(t_c) = X(t_0) + \dot{X}(t_c - t_0)$$

- Compare your estimated ITRF station positions to official ITRF values and check for consistency:
  - Transformation parameters should be zeros
  - No outliers: residuals smaller than a certain threshold.

# European Terrestrial Reference System ETRS89: Definition

- **Coincides with ITRS at epoch 1989.0:**
  - **Definition at a reference epoch (1989.0)**
  - **The 7 parameters between ITRS and ETRS89 are zero at 1989.0**
- **Fixed to the stable part of the Eurasian plate**
  - **Co-moving with the plate: law of time evolution**
  - **Time derivatives of the transformation parameters are zero except the 3 rotation rates**

# ETRS89 Realization

Fundamentally based on transformation from ITRS to ETRS89

Transformation formula ITRFyy ==> ETRFyy

Positions

$$X^E(t_c) = X_{YY}^I(t_c) + T_{YY} + \begin{pmatrix} 0 & -\dot{R}_{3YY} & \dot{R}_{2YY} \\ \dot{R}_{3YY} & 0 & -\dot{R}_{1YY} \\ -\dot{R}_{2YY} & \dot{R}_{1YY} & 0 \end{pmatrix} \times X_{YY}^I(t_c). (t_c - 1989.0)$$

Velocities

$$\begin{pmatrix} \dot{X}_{YY}^E \\ \dot{Y}_{YY}^E \\ \dot{Z}_{YY}^E \end{pmatrix} = \begin{pmatrix} \dot{X}_{YY}^I \\ \dot{Y}_{YY}^I \\ \dot{Z}_{YY}^I \end{pmatrix} + \begin{pmatrix} 0 & -\dot{R}_{3YY} & \dot{R}_{2YY} \\ \dot{R}_{3YY} & 0 & -\dot{R}_{1YY} \\ -\dot{R}_{2YY} & \dot{R}_{1YY} & 0 \end{pmatrix} \times \begin{pmatrix} X_{YY}^I \\ Y_{YY}^I \\ Z_{YY}^I \end{pmatrix}$$

# ITRFyy: Translation Parameters

**Table 3:** Estimation of  $T_{YY}$

$YY$		T1 cm	T2 cm	T3 cm
89		0	0	0
90	A	1.9	2.8	-2.3
	B	2.6	2.5	-2.6
	±	0.7	0.7	0.7
91	A	2.1	2.5	-3.7
	B	2.3	2.1	-3.1
	±	0.7	0.7	0.7
92	A	3.8	4.0	-3.7
	B	4.3	3.4	-3.2
	±	0.8	0.8	0.8
93	A	1.9	5.3	-2.1
	B	1.0	5.9	-1.4
	±	0.5	0.5	0.6

**Table 3 : (cont'd)**

94	A	4.1	4.1	-4.9
	B	2.9	4.3	-3.6
	±	0.4	0.5	0.5
96	A	4.1	4.1	-4.9
	B	3.9	4.1	-3.9
	±	0.4	0.4	0.4
97	A	4.1	4.1	-4.9
	B	3.4	4.4	-4.3
	±	0.4	0.4	0.4
00	A	5.4	5.1	-4.8
	B	4.2	5.1	-4.6
	±	0.4	0.4	0.4
05*	A	5.6	4.8	-3.7
	B	3.6	4.2	-4.1
	±	0.4	0.4	0.4

\* See the Memo: Boucher & Altamimi, 2011: memo-V8.pdf

# ITRFyy Eurasia Rotation Poles

Table 4: Estimation of  $\dot{R}_{YY}$

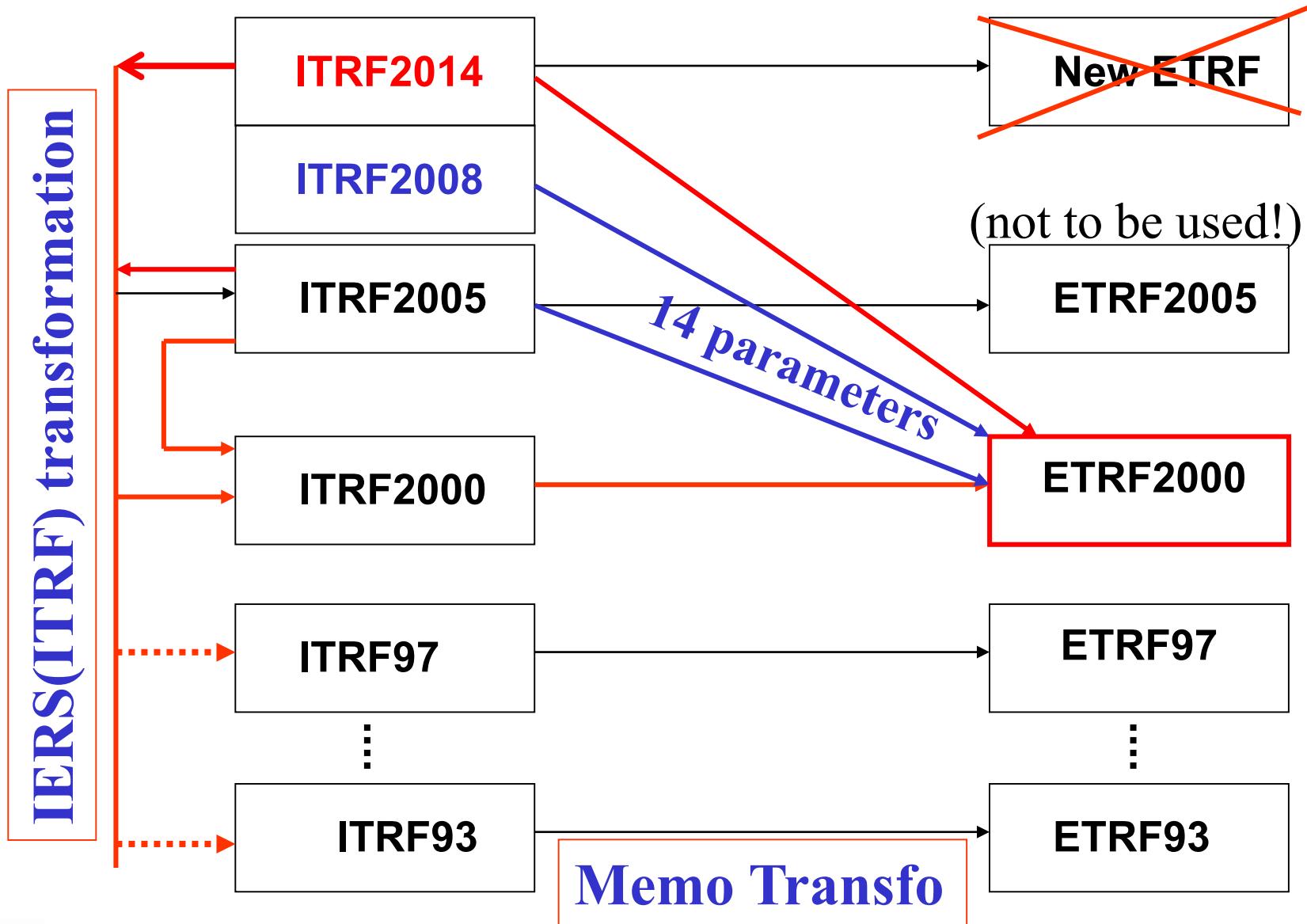
$YY$	$\dot{R}1$ mas/y	$\dot{R}2$ mas/y	$\dot{R}3$ mas/y
89	0.11	0.57	-0.71
90	0.11	0.57	-0.71
91	0.21	0.52	-0.68
92	0.21	0.52	-0.68
93	0.32	0.78	-0.67
94	0.20	0.50	-0.65
96	0.20	0.50	-0.65
97	0.20	0.50	-0.65
00	0.081	0.490	-0.792
	$\pm 0.021$	$\pm 0.008$	$\pm 0.026$
05*	0.054	0.518	-0.781
	$\pm 0.009$	$\pm 0.006$	$\pm 0.011$

\* See TWG recommendation §4

# TWG Recommendation

- Adopt ETRF2000 as a conventional frame of the ETRS89 system
- Provide transformation parameters (14) from ITRFyy to ETRF2000
- Goal:
  - harmonize the ETRS89 realization overall Europe
  - avoid coordinates jumps due to reference frame changes

# ITRFyy to ETRFyy



# Transformation parameters from ITRF<sub>yy</sub> to ETRF2000

**Table 5:** Transformation parameters from ITRF<sub>yy</sub> to ETRF2000 **at epoch 2000.0**  
and their rates/year

ITRF Solution	T1 mm	T2 mm	T3 mm	D $10^{-9}$	R1 mas	R2 mas	R3 mas
ITRF2008	52.1	49.3	-58.5	1.34	0.891	5.390	-8.712
Rates	0.1	0.1	-1.8	0.08	0.081	0.490	-0.792
ITRF2005	54.1	50.2	-53.8	0.40	0.891	5.390	-8.712
Rates	-0.2	0.1	-1.8	0.08	0.081	0.490	-0.792
ITRF2000	54.0	51.0	-48.0	0.00	0.891	5.390	-8.712
Rates	0.0	0.0	0.0	0.00	0.081	0.490	-0.792
ITRF97	47.3	46.7	-25.3	-1.58	0.891	5.390	-8.772
Rates	0.0	0.6	1.4	-0.01	0.081	0.490	-0.812
ITRF96	47.3	46.7	-25.3	-1.58	0.891	5.390	-8.772
Rates	0.0	0.6	1.4	-0.01	0.081	0.490	-0.812
ITRF94	47.3	46.7	-25.3	-1.58	0.891	5.390	-8.772
Rates	0.0	0.6	1.4	-0.01	0.081	0.490	-0.812
ITRF93	76.1	46.9	-19.9	-2.07	2.601	6.870	-8.412
Rates	2.9	0.2	0.6	-0.01	0.191	0.680	-0.862
ITRF92	39.3	44.7	-17.3	-0.87	0.891	5.390	-8.772
Rates	0.0	0.6	1.4	-0.01	0.081	0.490	-0.812
ITRF91	27.3	30.7	-11.3	-2.27	0.891	5.390	-8.772
Rates	0.0	0.6	1.4	-0.01	0.081	0.490	-0.812
ITRF90	29.3	34.7	4.7	-2.57	0.891	5.390	-8.772
Rates	0.0	0.6	1.4	-0.01	0.081	0.490	-0.812
ITRF89	24.3	10.7	42.7	-5.97	0.891	5.390	-8.772
Rates	0.0	0.6	1.4	-0.01	0.081	0.490	-0.812

# How to express a GNSS network in the ETRS89 (ETRF2000)?

- Process GNSS data of your stations, together with IGS/ITRF stations as described at slides 8 & 9
- ==> Coordinates are expressed in ITRFyy at the central epoch ( $t_c$ ) of the observations
- Transform into ETRF2000 using values at slide 16, and formula at slide 11

# Transfo ITRF2014 ==> ETRF2000

**Table 5:** Transformation parameters from ITRF<sub>yy</sub> to ETRF2000 **at epoch 2000.0** and their rates/year



ITRF Solution	T1 mm	T2 mm	T3 mm	D $10^{-9}$	R1 mas	R2 mas	R3 mas
ITRF2008	52.1	49.3	-58.5	1.34	0.891	5.390	-8.712
Rates	0.1	0.1	-1.8	0.08	0.081	0.490	-0.792
ITRF2005	54.1	50.2	-53.8	0.40	0.891	5.390	-8.712
Rates	-0.2	0.1	-1.8	0.08	0.081	0.490	-0.792
ITRF2000	54.0	51.0	-48.0	0.00	0.891	5.390	-8.712
Rates	0.0	0.0	0.0	0.00	0.081	0.490	-0.792

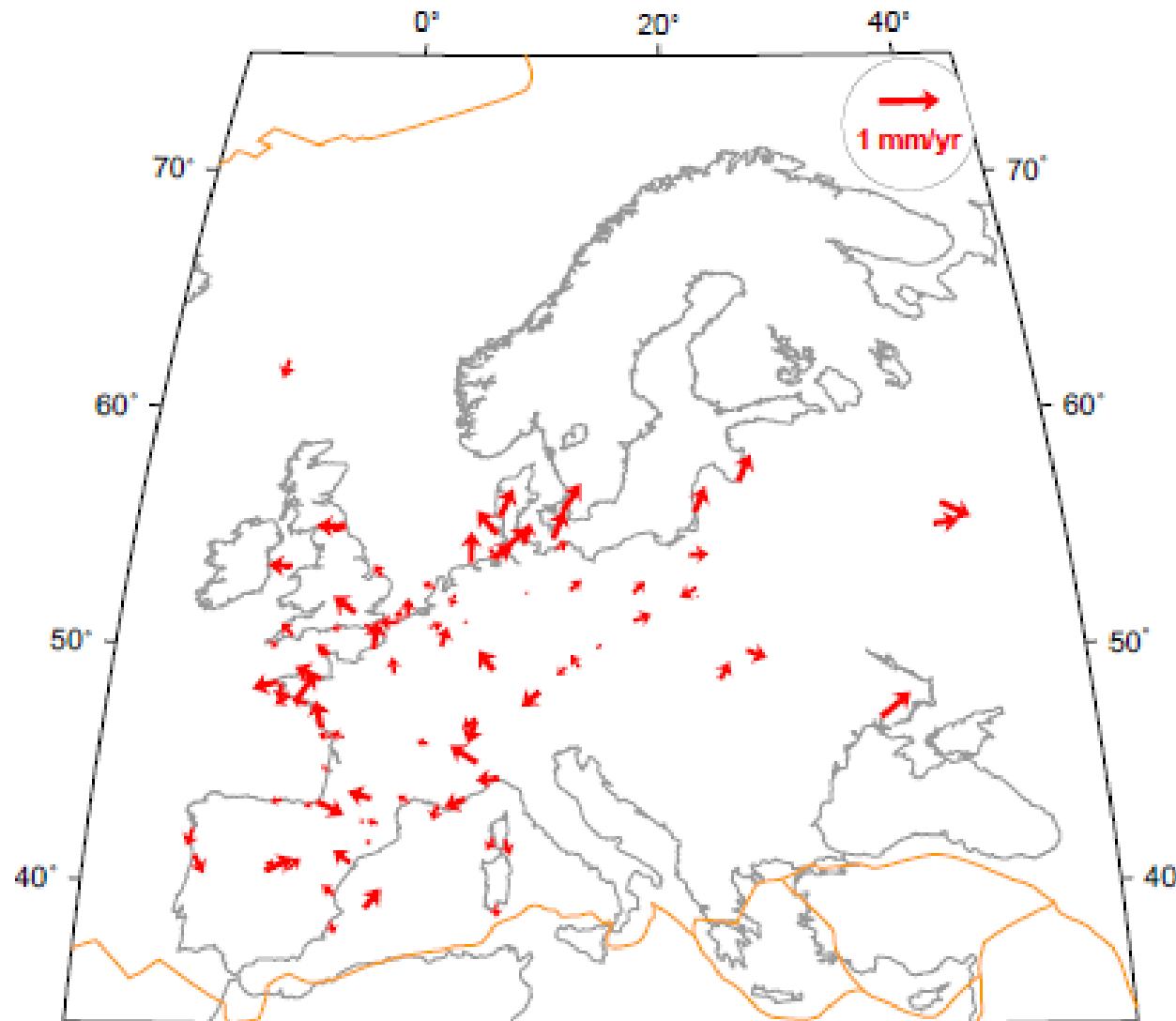
**Table 5:** Transformation parameters from ITRF<sub>yy</sub> to ETRF2000 **at epoch 2000.0** and their rates/year

ITRF Solution	T1 mm	T2 mm	T3 mm	D $10^{-9}$	R1 mas	R2 mas	R3 mas
ITRF2014	53.7	51.2	-55.1	1.020	0.891	5.390	-8.712
Rates	0.1	0.1	-1.9	0.110	0.081	0.490	-0.792
ITRF2008	52.1	49.3	-58.5	1.34	0.891	5.390	-8.712
Rates	0.1	0.1	-1.8	0.08	0.081	0.490	-0.792

An exercise  
Derive an ETRF2014P  
from ITRF2014

# **Preliminary estimation of Eurasia Rotation Pole, through an ITRF2014 Plate Motion Model under construction**

# Preliminary Eurasia Rotation Pole Estimation: Residuals



# Transformation parameters

T1 mm	T2 mm	T3 mm	D 10 <sup>-9</sup>	R1 mas	R2 mas	R3 mas	Epoch y
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**From ITRF2000 to ETRF2000:**

54.0	51.0	-48.0	0.0	1.701	10.290	-16.632	10:001
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Rates	0.0	0.0	0.0	0.0	0.081	0.490	-0.792
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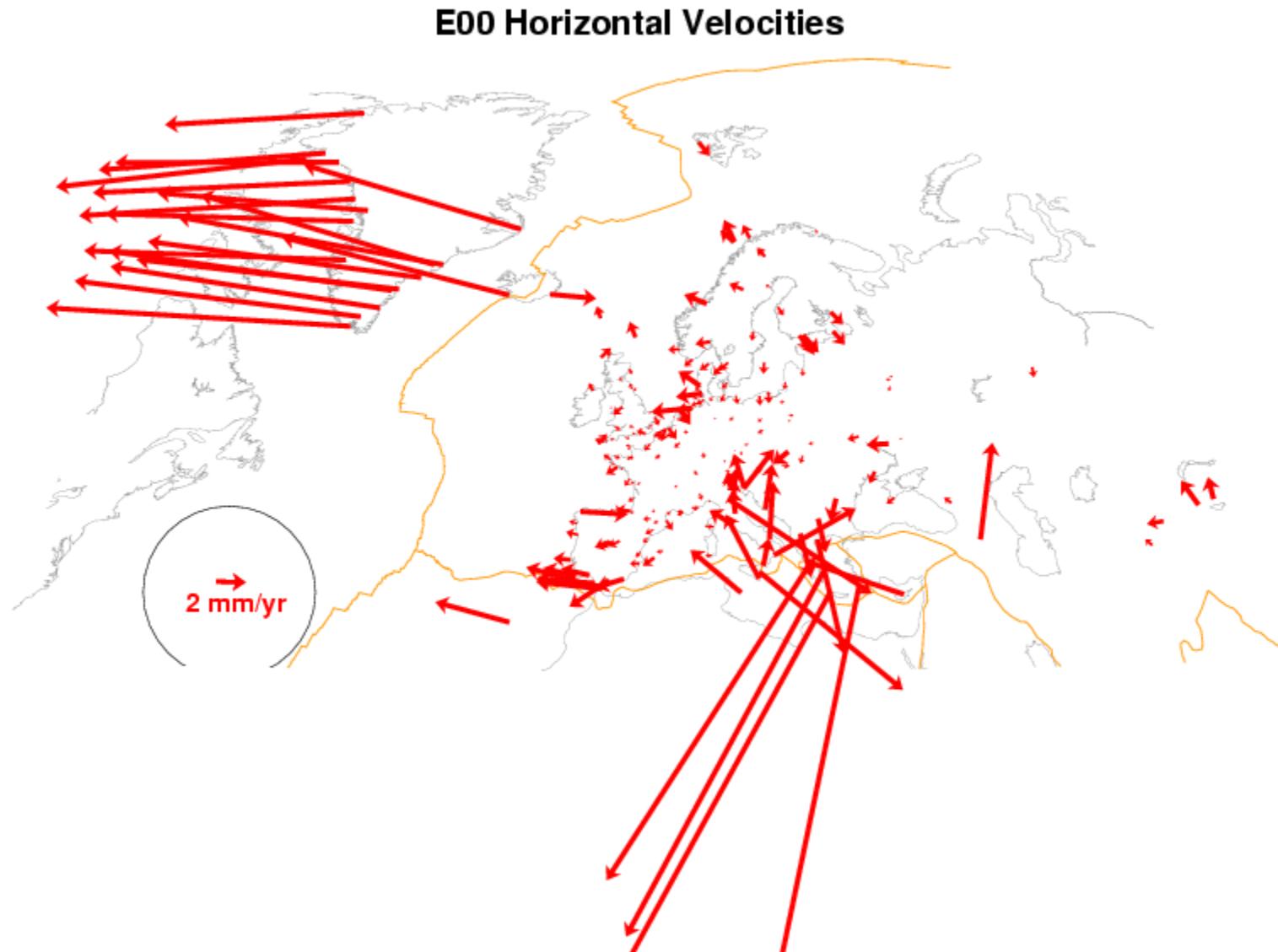
**Angular velocity of Eurasia**

**From ITRF2014 to ETRF2014P (Preliminary) :**

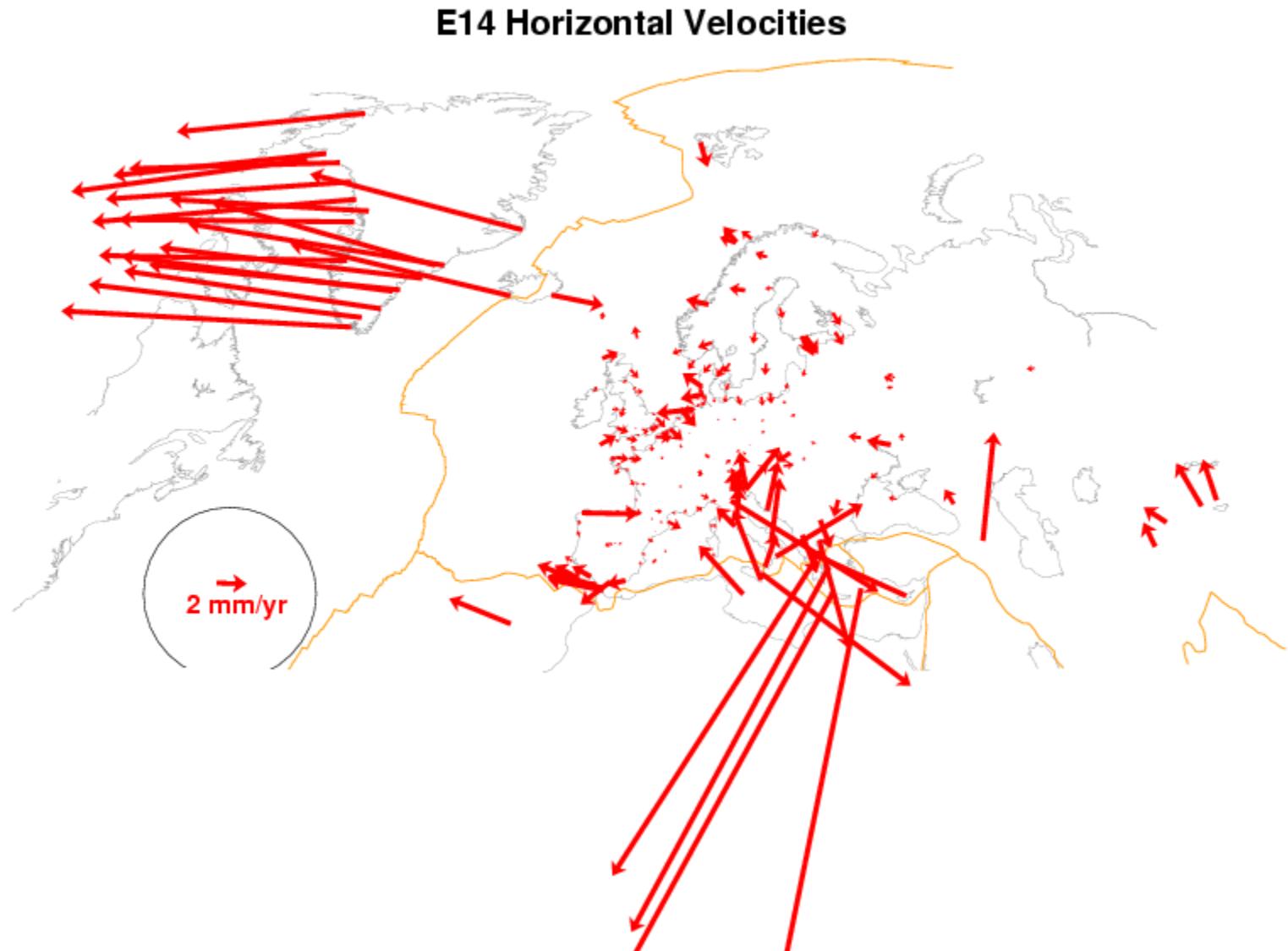
55.3	53.1	-52.7	0.0	1.848	11.172	-15.939	10:001
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Rates	0.0	0.0	0.0	0.0	0.088	0.532	-0.759
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# ITRF2014 → ETRF2000: Horizontal Velocities

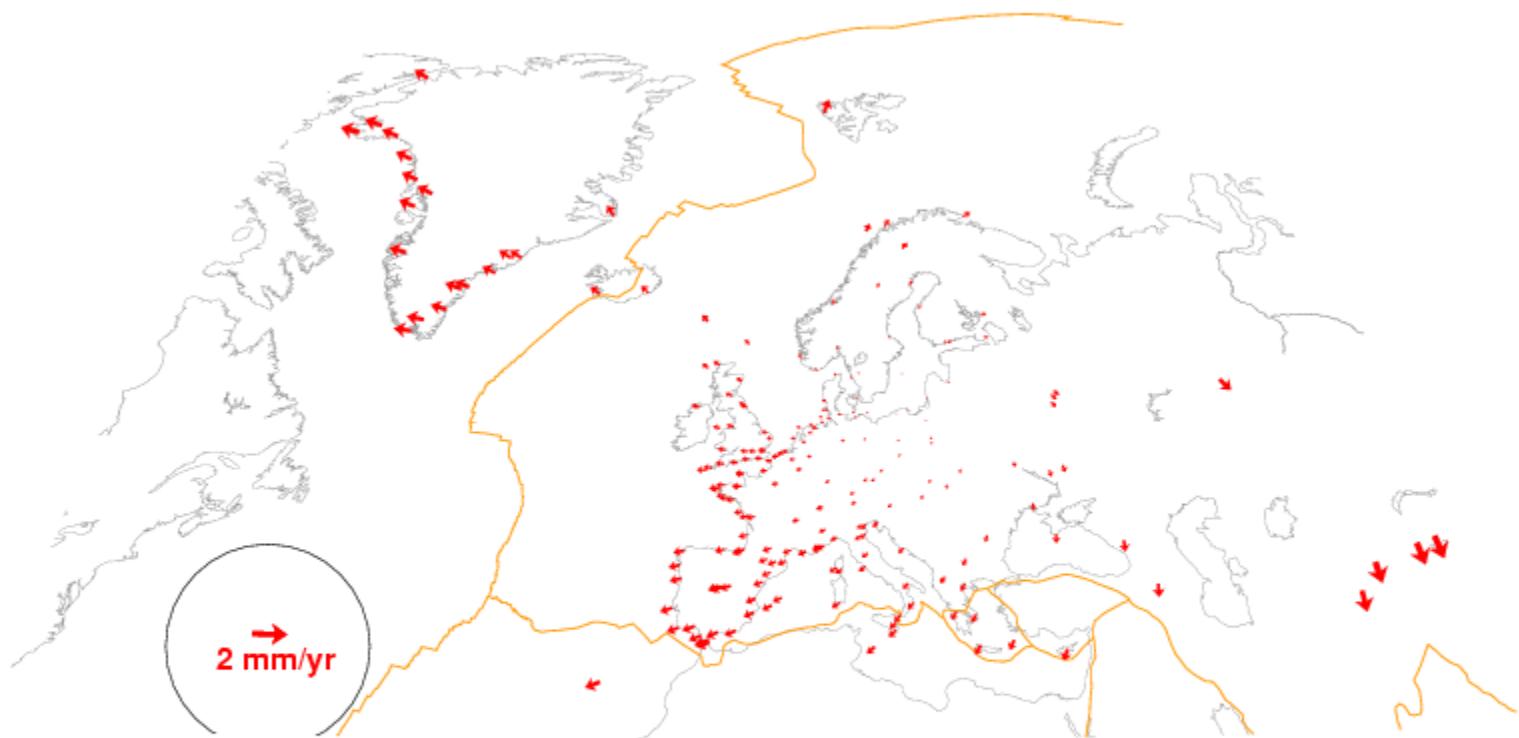


# ITRF2014 → ETRF2014P : Horizontal Velocities

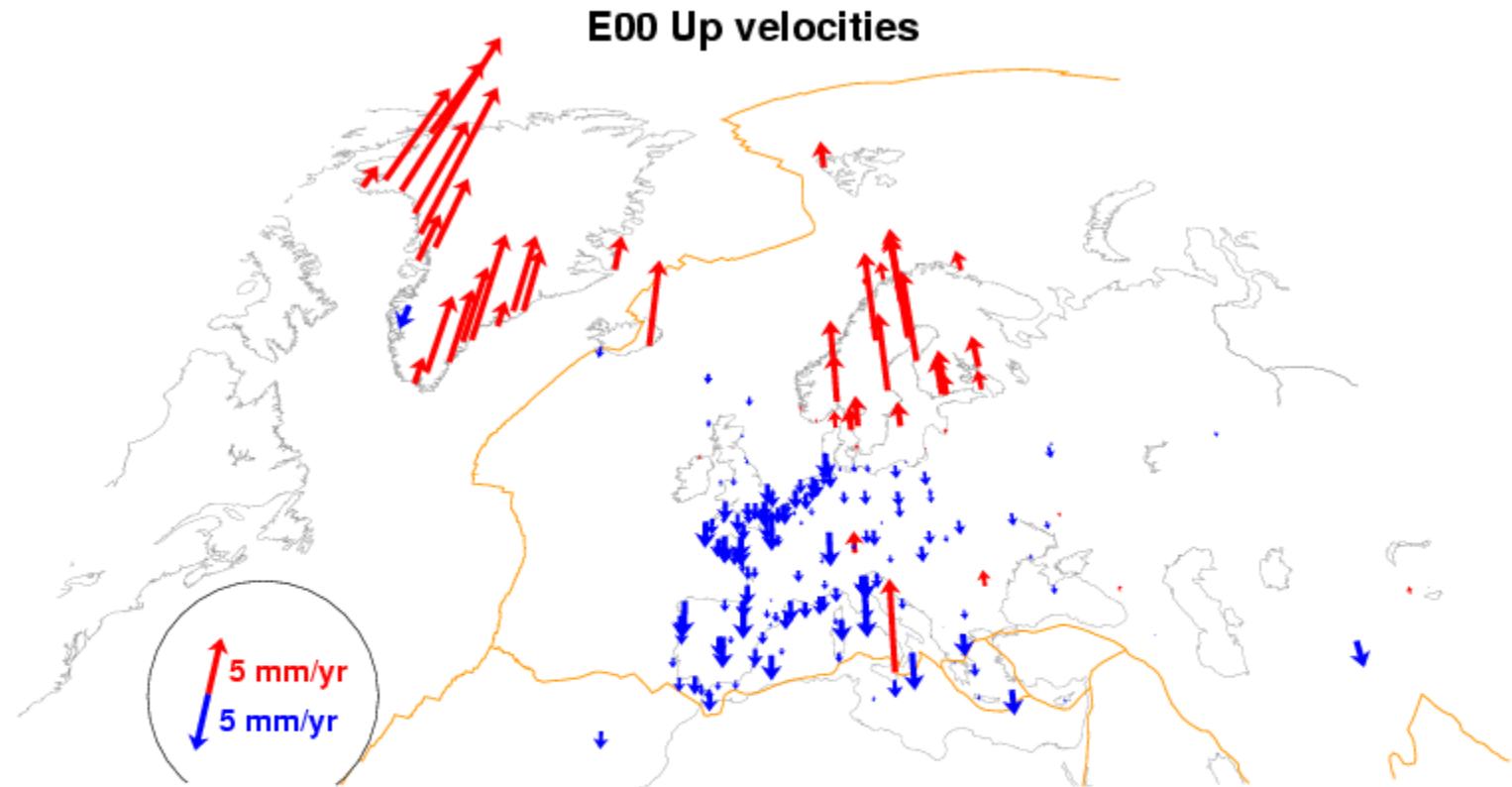


# Horizontal Velocity Diffs ETRF2000 –ETRF2014P

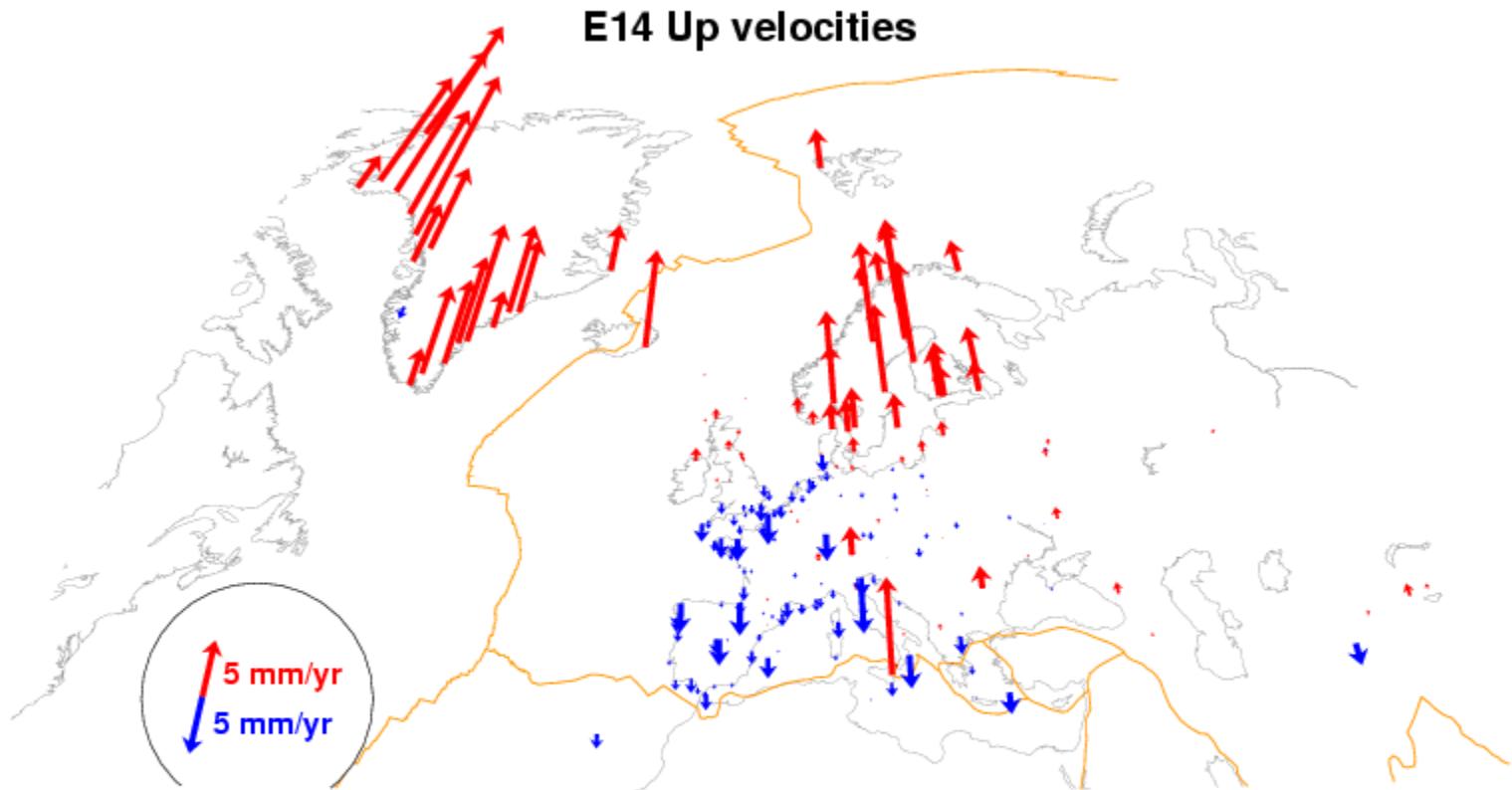
E00 - E14 horizontal velocity diffs



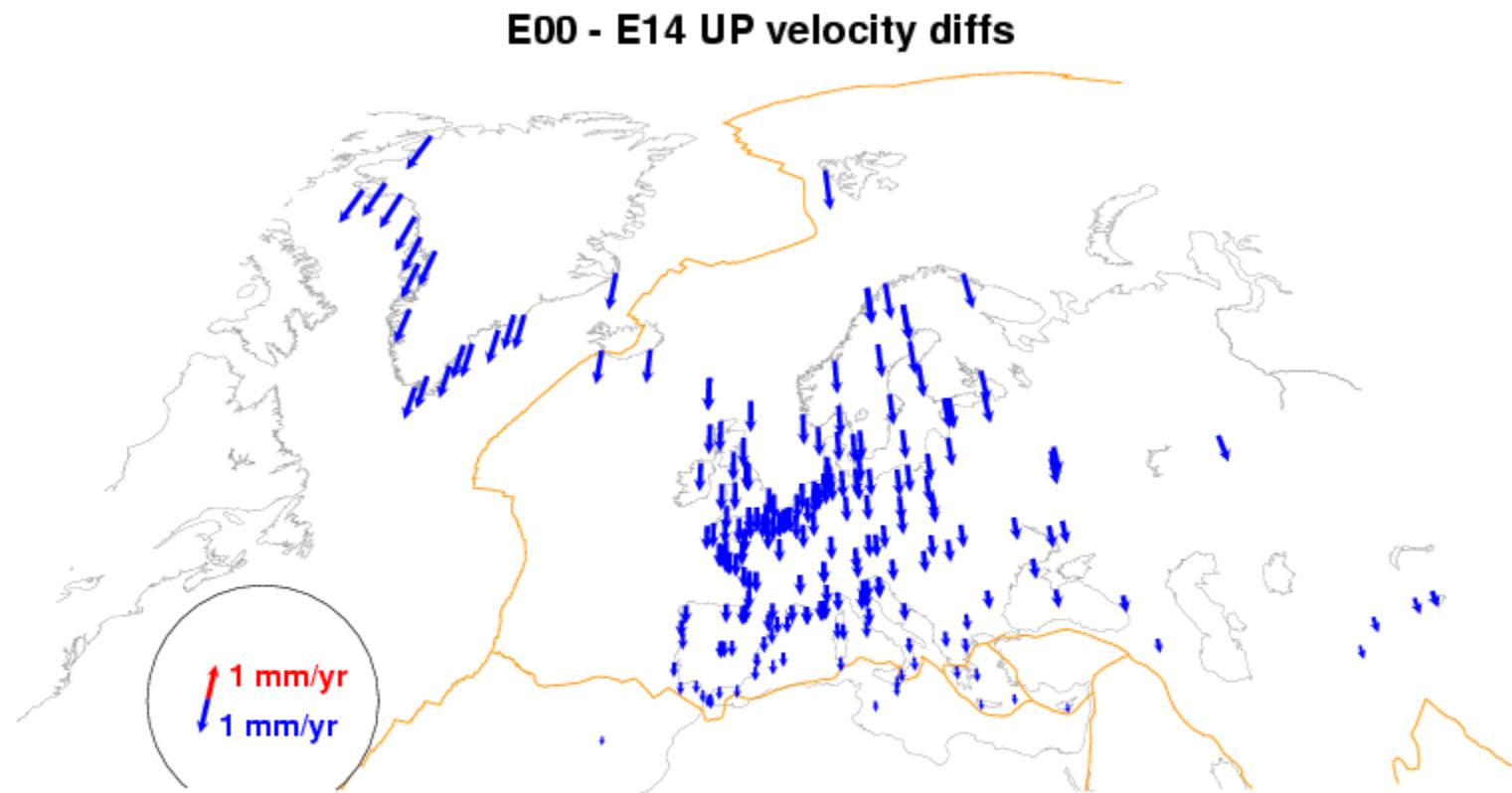
# ITRF2014 → ETRF2000: UP velocities



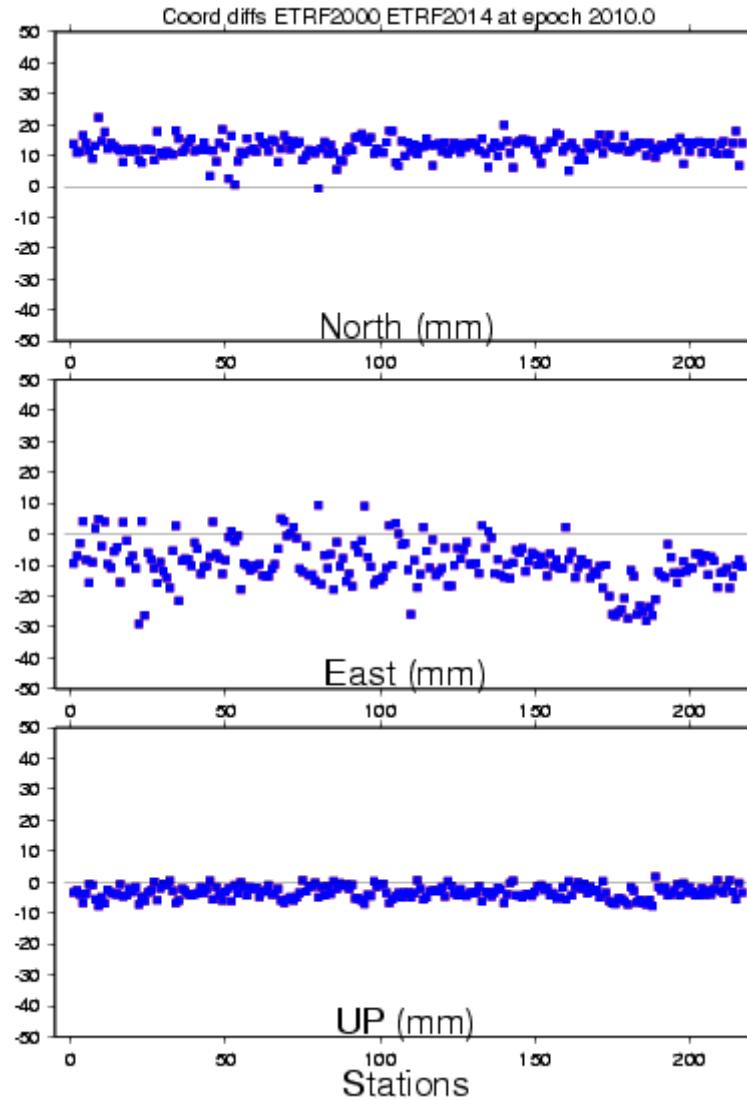
# ITRF2014 → ETRF2014P: UP velocities



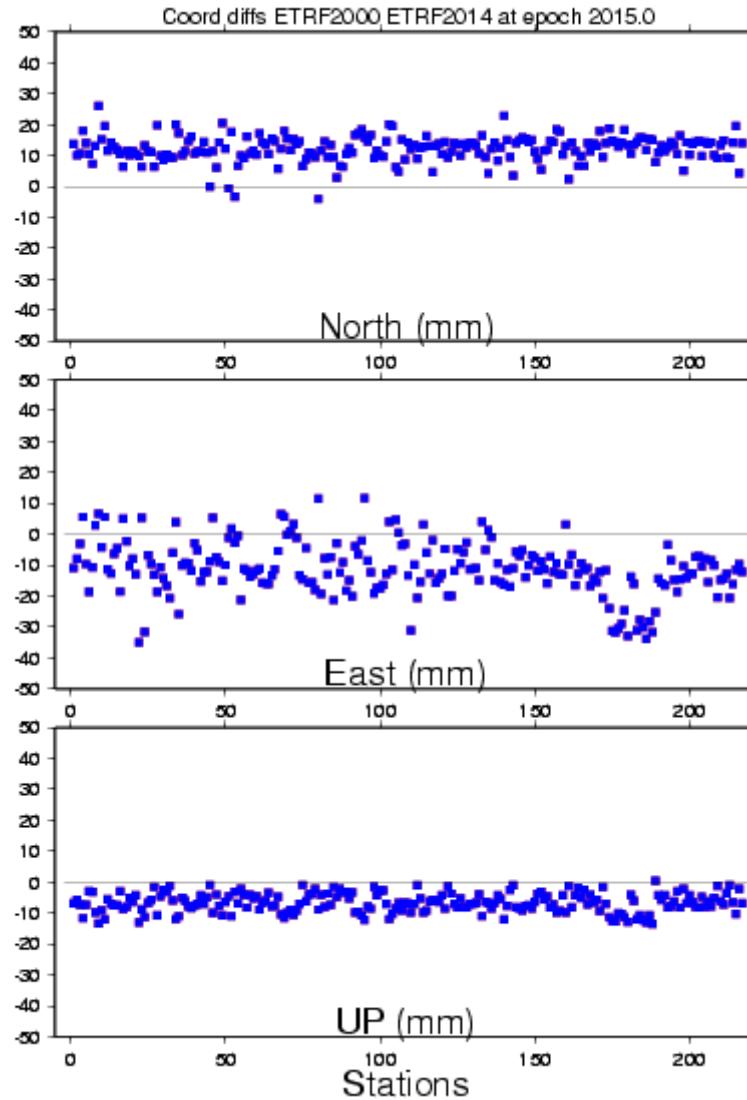
# UP Velocity Diffs ETRF2000 –ETRF2014P



## Coord diffs ETRF2000 – ETRF2014P at epoch 2010.0



## Coord diffs ETRF2000 – ETRF2014P at epoch 2015.0



# Remarks

- Differences btw ETRF2000 and ETRF2014P are small for geo-referencing applications:
  - $\approx 1\text{mm/yr}$  in velocities
  - $< 3 \text{ cm}$  in positions
- ITRF2014 (ETRF2014P) more precise and accurate than ITRF2000 (ETRF2000)
- Origin & Scale btw ITRF2014 & ITRF2008 are small :  
 $< 5 \text{ mm}$   
==> improved ITRF origin and scale accuracy & stability
- If EUREF/TWG adopt an ETRF2014, then
  - Finalize the Eurasia rotation pole values
  - Revise the memo ==> **complete re-write**
  - Adopt ETRF2014 as a new conventional ETRS89 frame