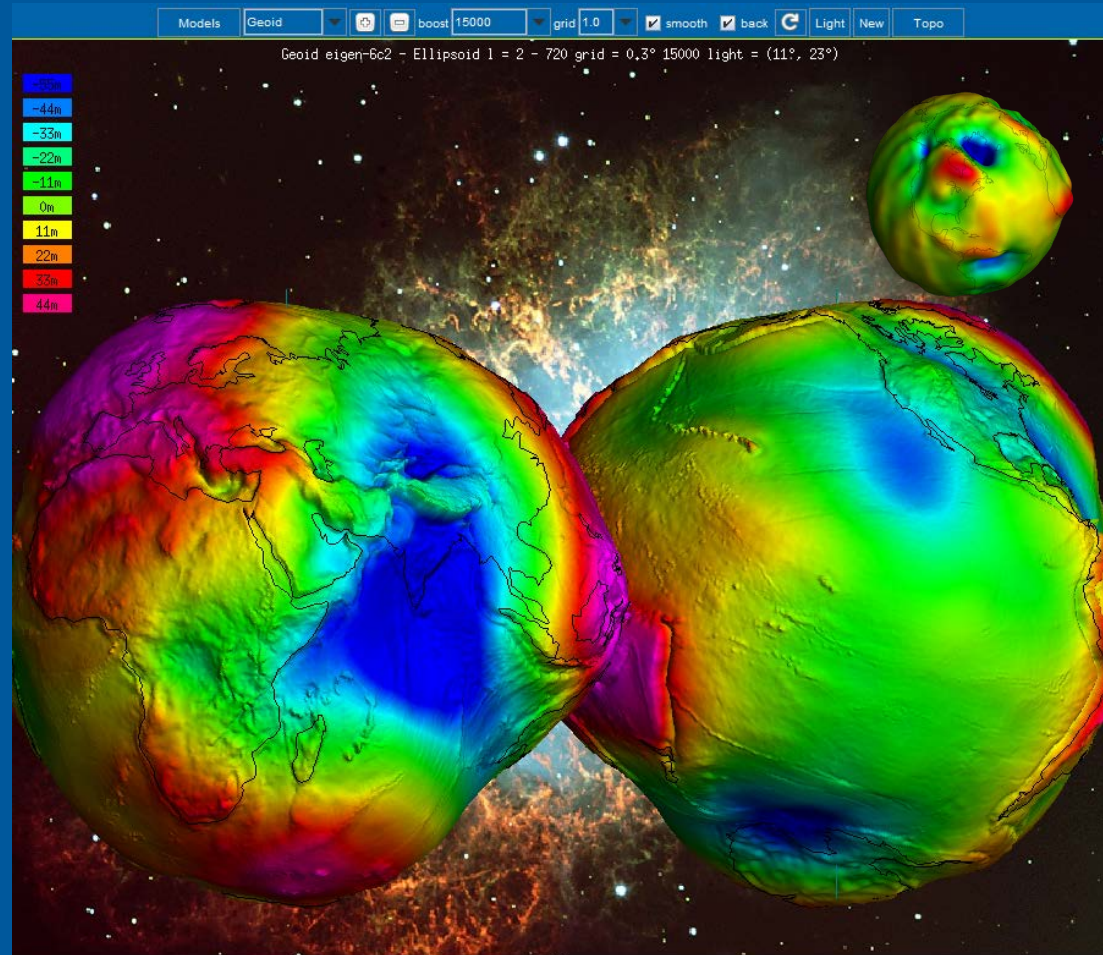


ICGEM

Global Gravity Field Models and the IAG Service ICGEM (International Centre for Global Earth Models)

Franz Barthelmes

GFZ German Research Centre
for Geosciences
Telegrafenberg
14473 Potsdam
Section 1.2

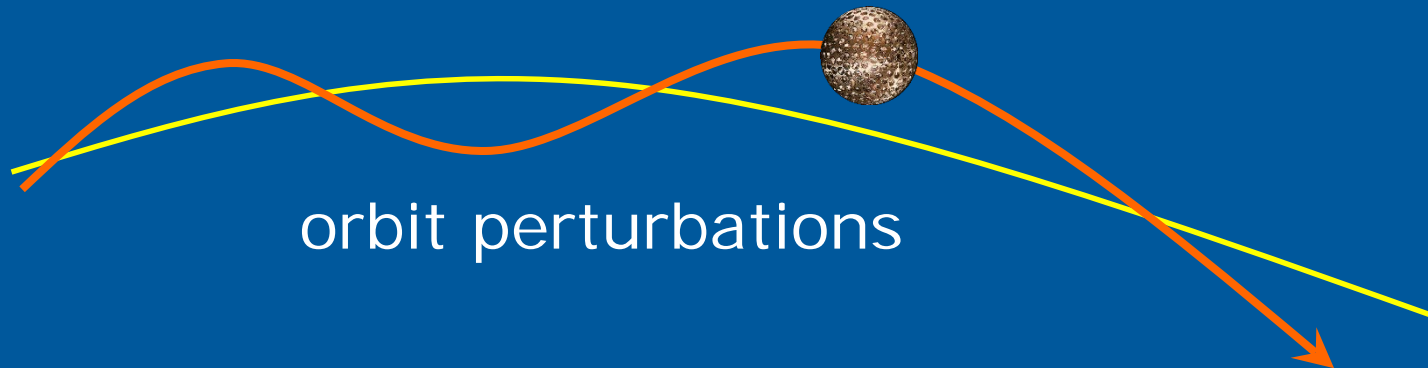


Global Gravity Field Models

Where are they come from?

Satellites + satellite altimetry + terrestrial gravimetry

Satellites → Gravity Field: What can we measure?



Global Gravity Field Models

Where are they come from?

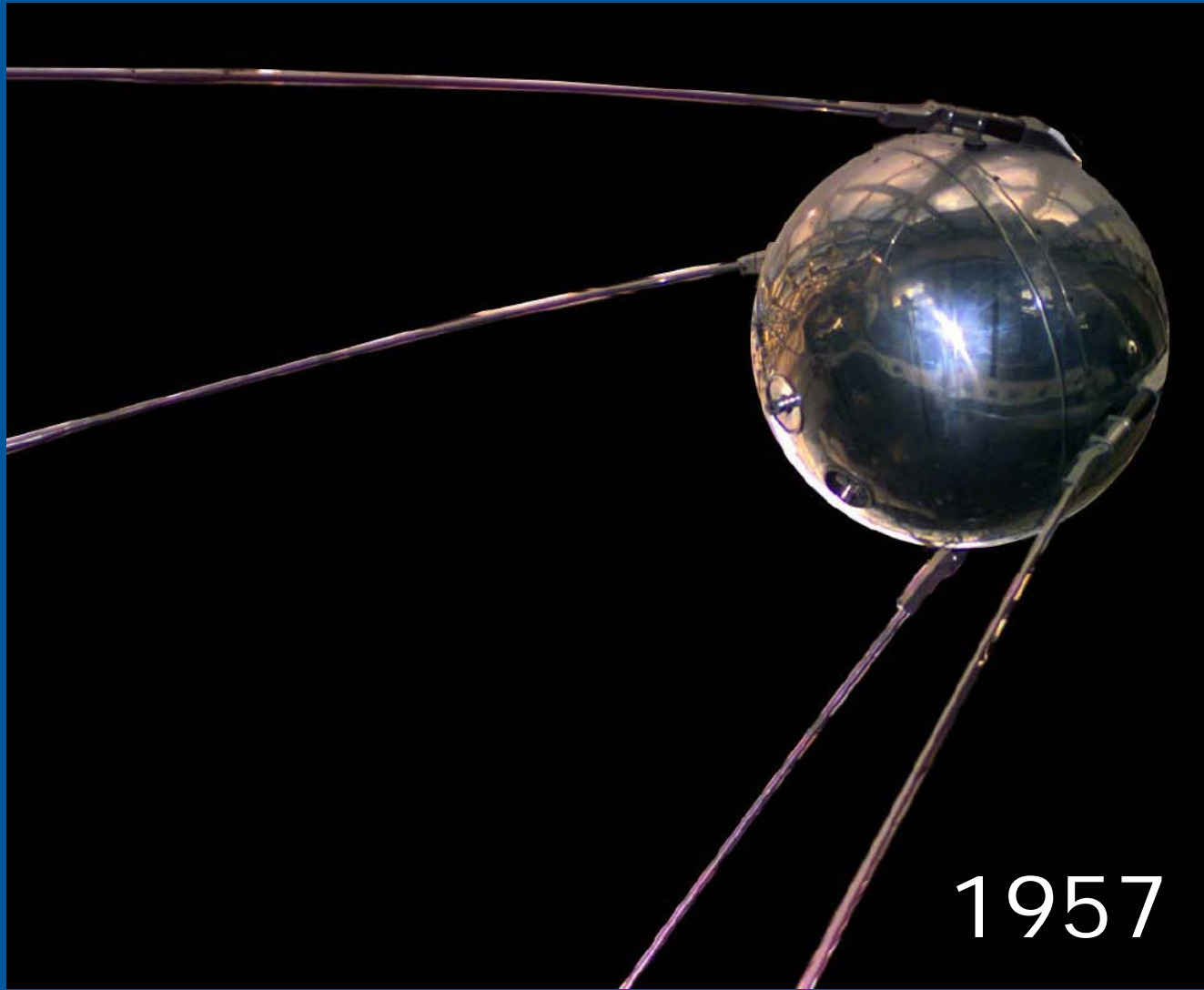
Satellites + satellite altimetry + terrestrial gravimetry

Satellites → Gravity Field: What can we measure?

acceleration differences inside the satellite
→ Gradiometry



The Beginning: Sputnik 1



The first Measurements

optical observation

Sputnik-observations in Potsdam



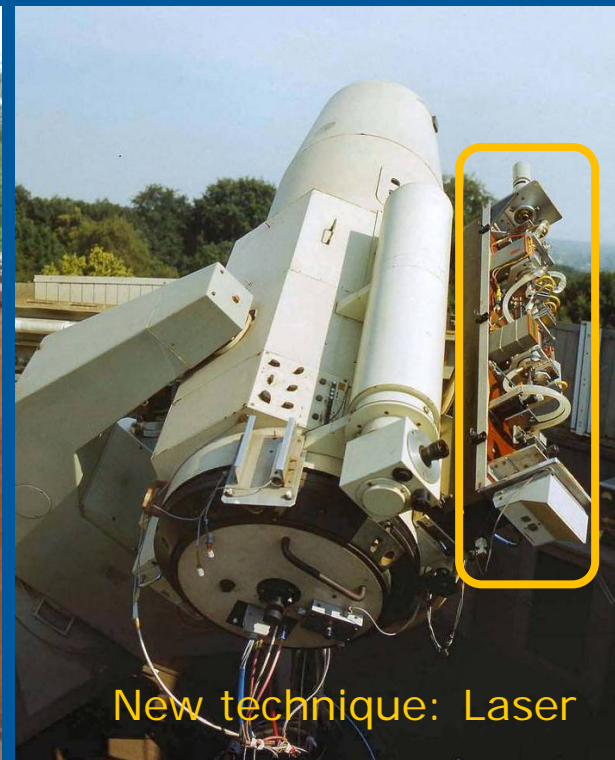
Optical Satellite Tracking



Baker Nunn
(USA 1957)

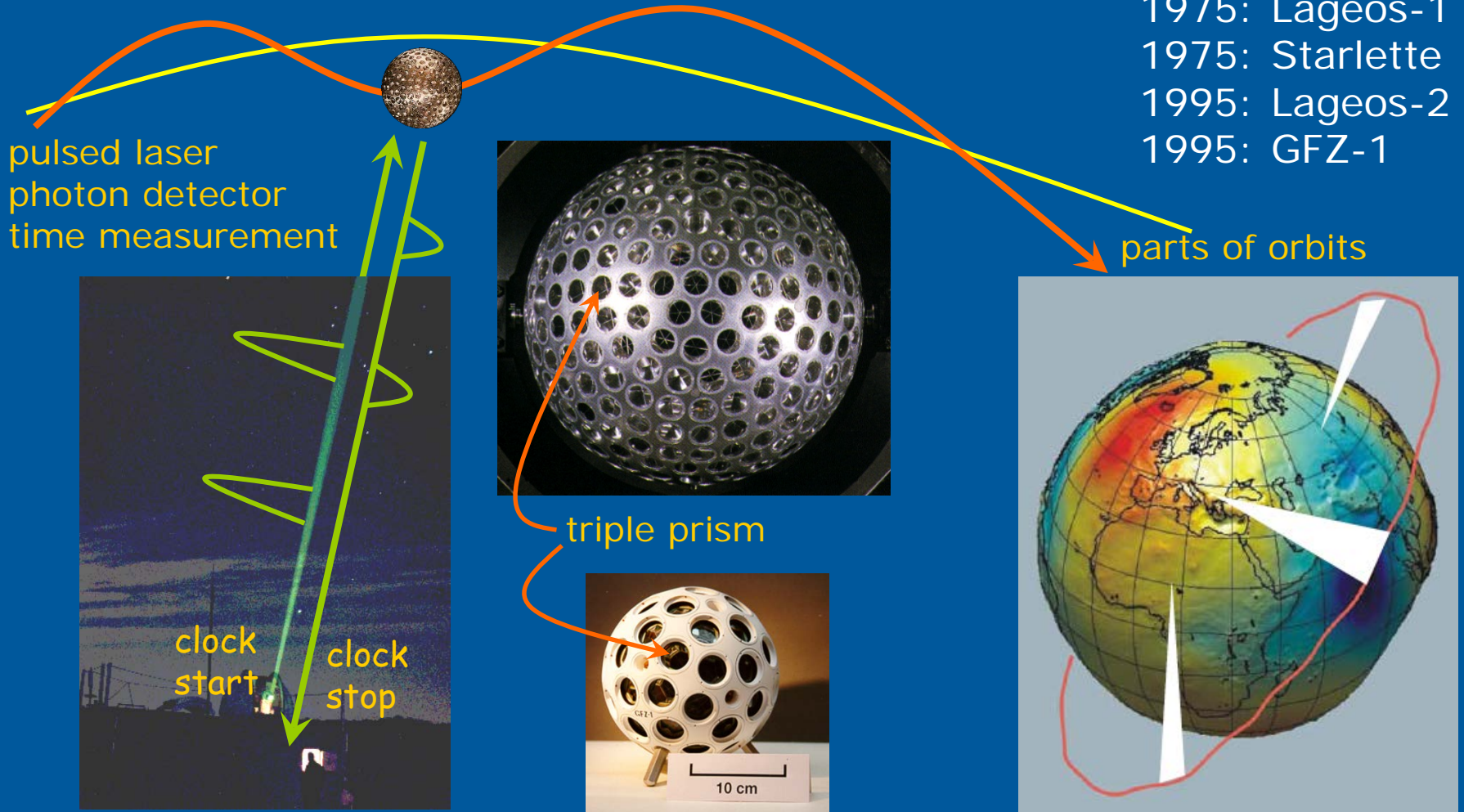


AFU-75
(USSR/Latvia 1967)

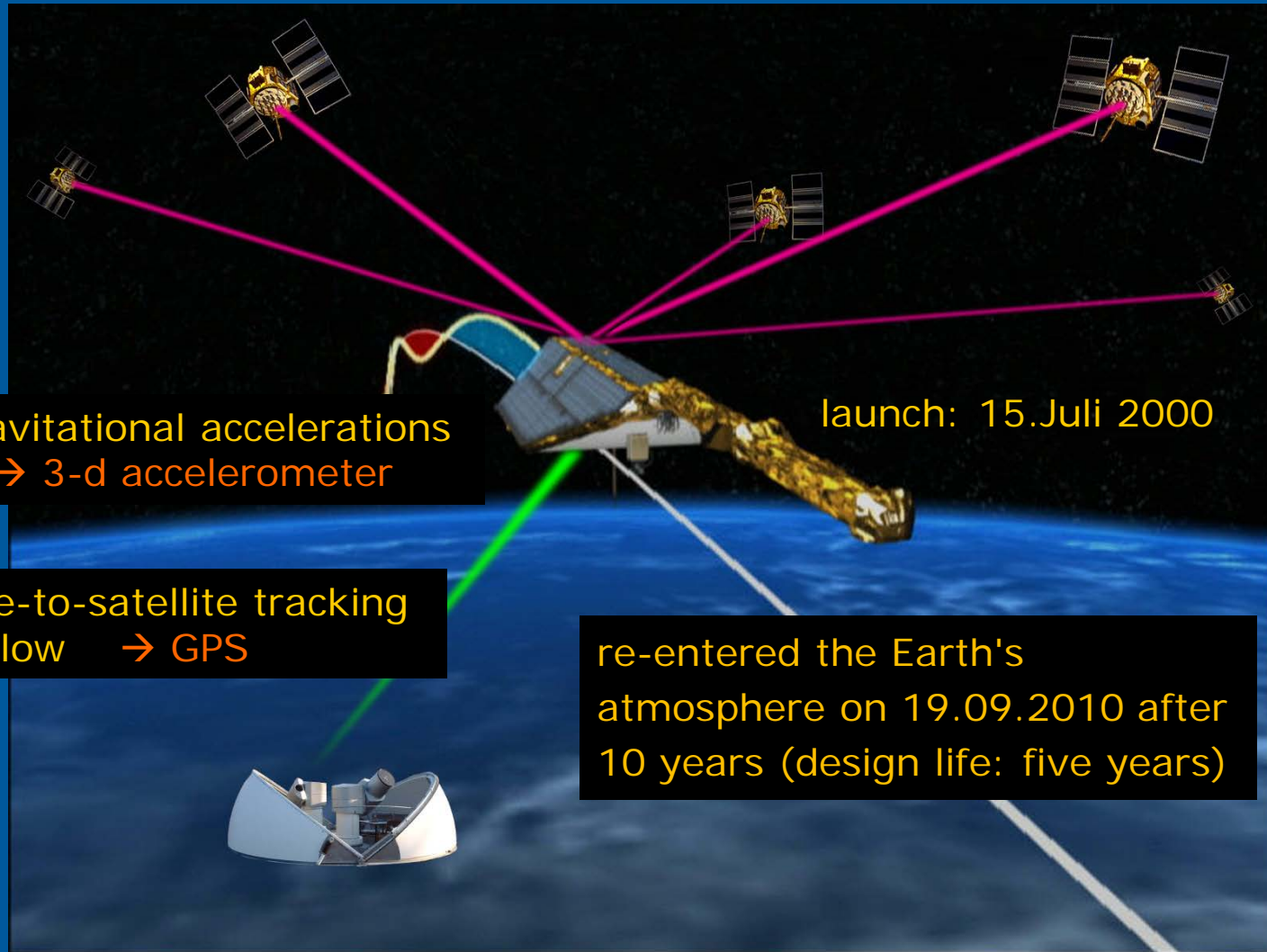


SBG
(Germany/Jena 1966)

Laser Ranging



High–Low with GPS → CHAMP



non-gravitational accelerations
→ 3-d accelerometer

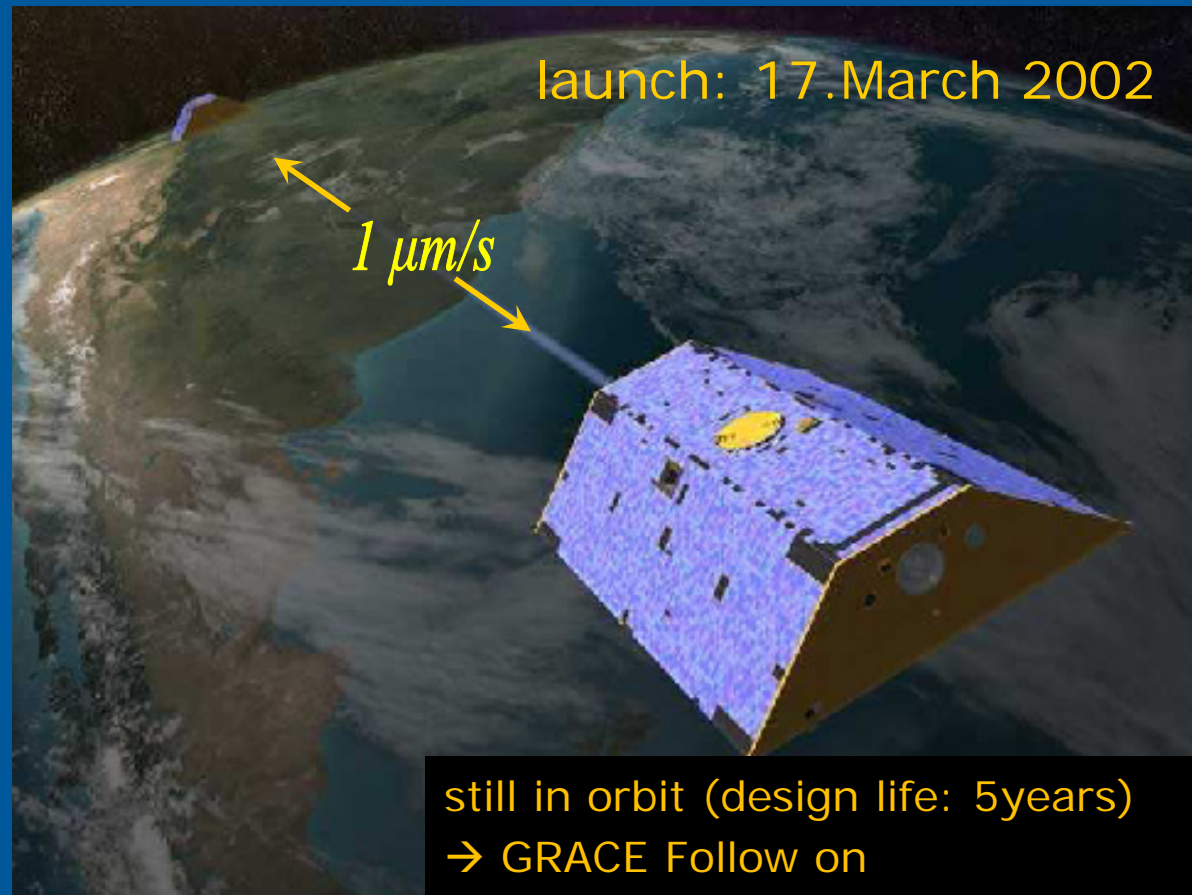
satellite-to-satellite tracking
high – low → GPS

launch: 15.Juli 2000

re-entered the Earth's
atmosphere on 19.09.2010 after
10 years (design life: five years)

Heigh–Low + Low–Low → GRACE

GRACE: Gravity Recovery And Climate Experiment

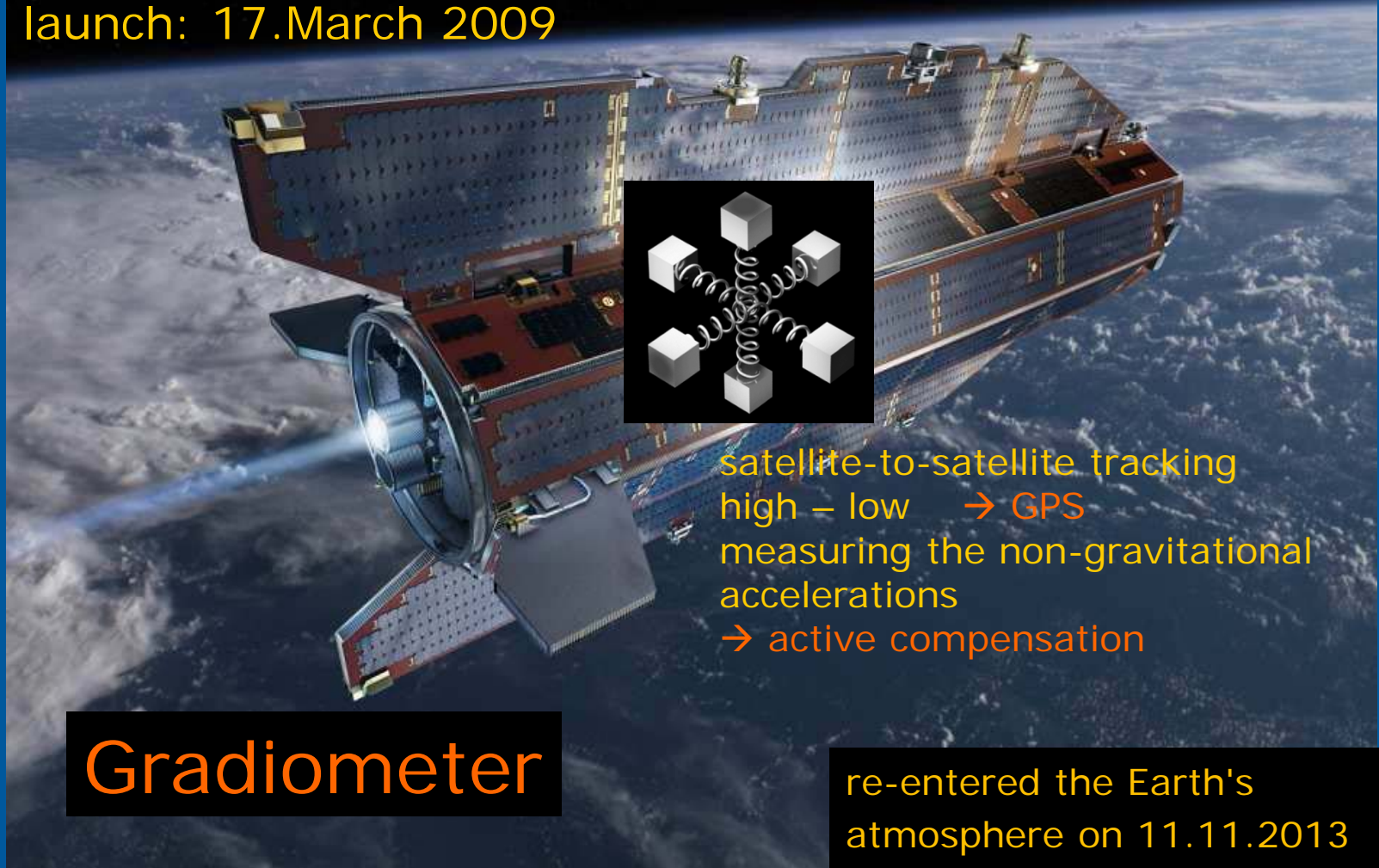


satellite-to-satellite tracking
high – low → GPS
low – low → microwaves
K-band (1.13-1.67cm)

non-gravitational accelerations
→ 3-d accelerometer

GOCE

Gravity Field and Steady State Ocean Circulation Explorer
launch: 17.March 2009



satellite-to-satellite tracking
high – low → GPS
measuring the non-gravitational
accelerations
→ active compensation

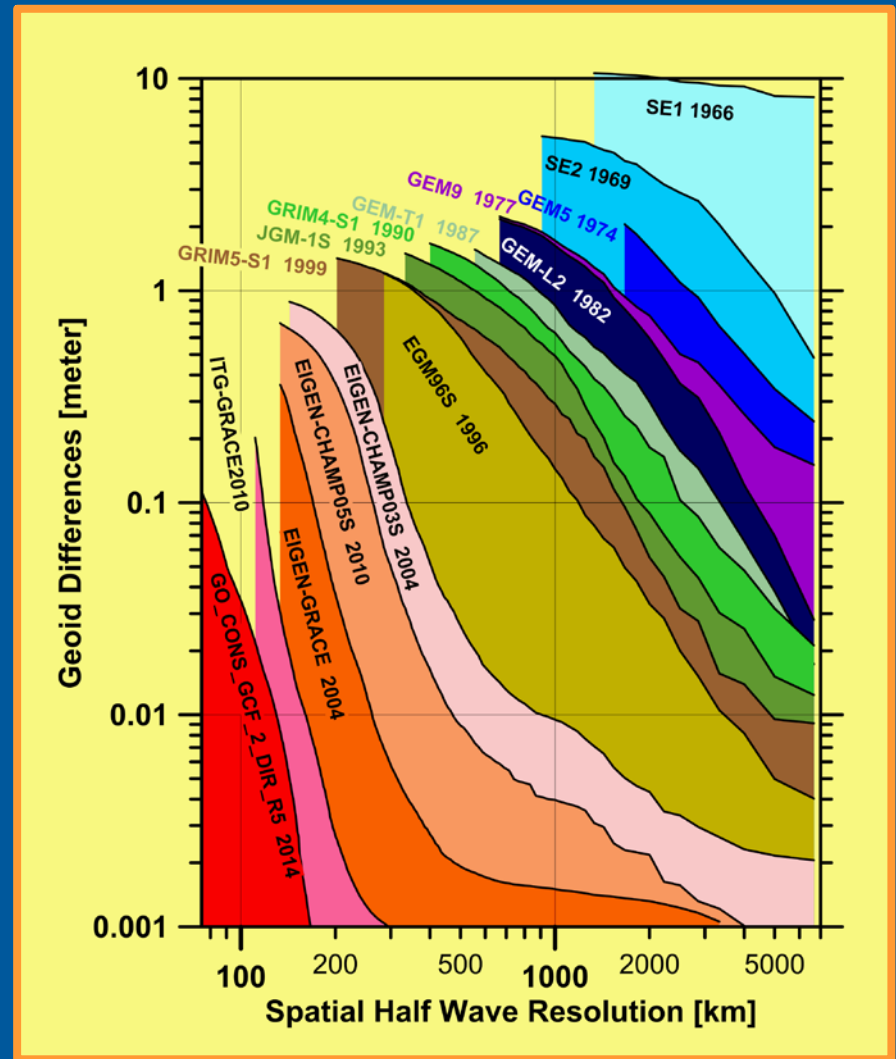
Gradiometer

re-entered the Earth's
atmosphere on 11.11.2013

Global Models – Improvement in History

Geoid differences of satellite-only models of the past to recent (“best”) combination solution as a function of spatial resolution

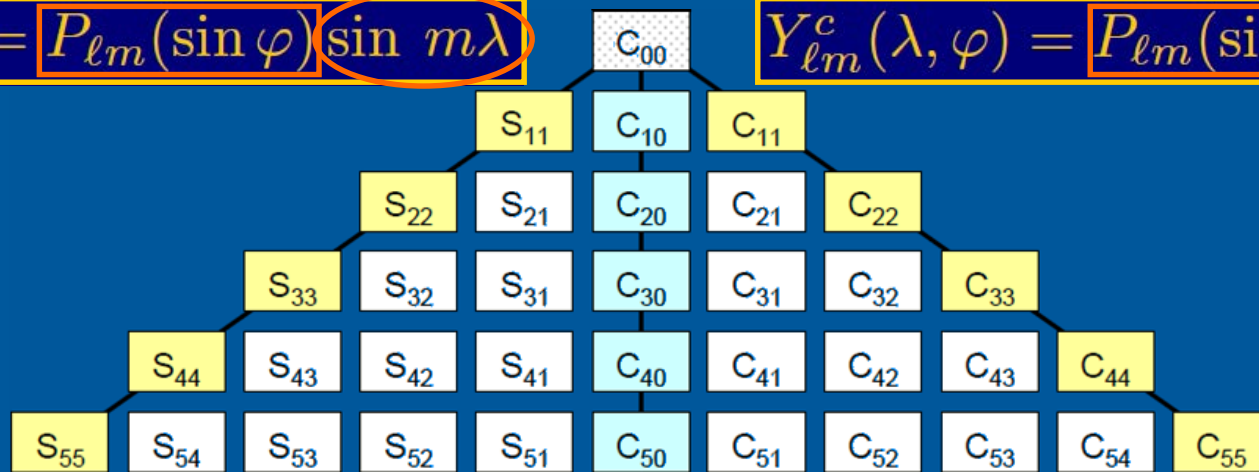
→ differences to
EIGEN-6C4



Mathematical Representation

$$W_a(r, \lambda, \varphi) = \frac{GM}{r} \sum_{\ell=0}^{\infty} \left(\frac{R}{r}\right)^{\ell} \sum_{m=0}^{\ell} [C_{\ell m} Y_{\ell m}^c(\lambda, \varphi) + S_{\ell m} Y_{\ell m}^s(\lambda, \varphi)]$$

$$Y_{\ell m}^s(\lambda, \varphi) = P_{\ell m}(\sin \varphi) \sin m\lambda \quad C_{00} \quad Y_{\ell m}^c(\lambda, \varphi) = P_{\ell m}(\sin \varphi) \cos m\lambda$$



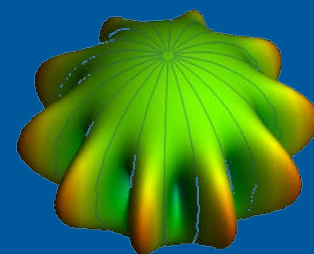
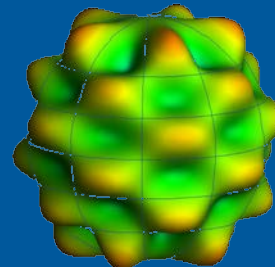
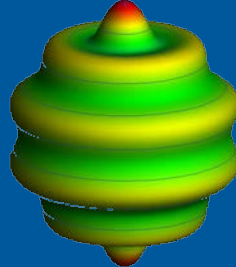
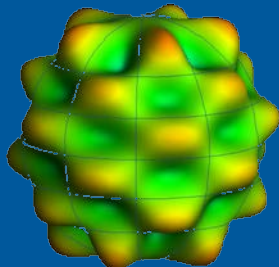
sectorial

tesseral

zonal

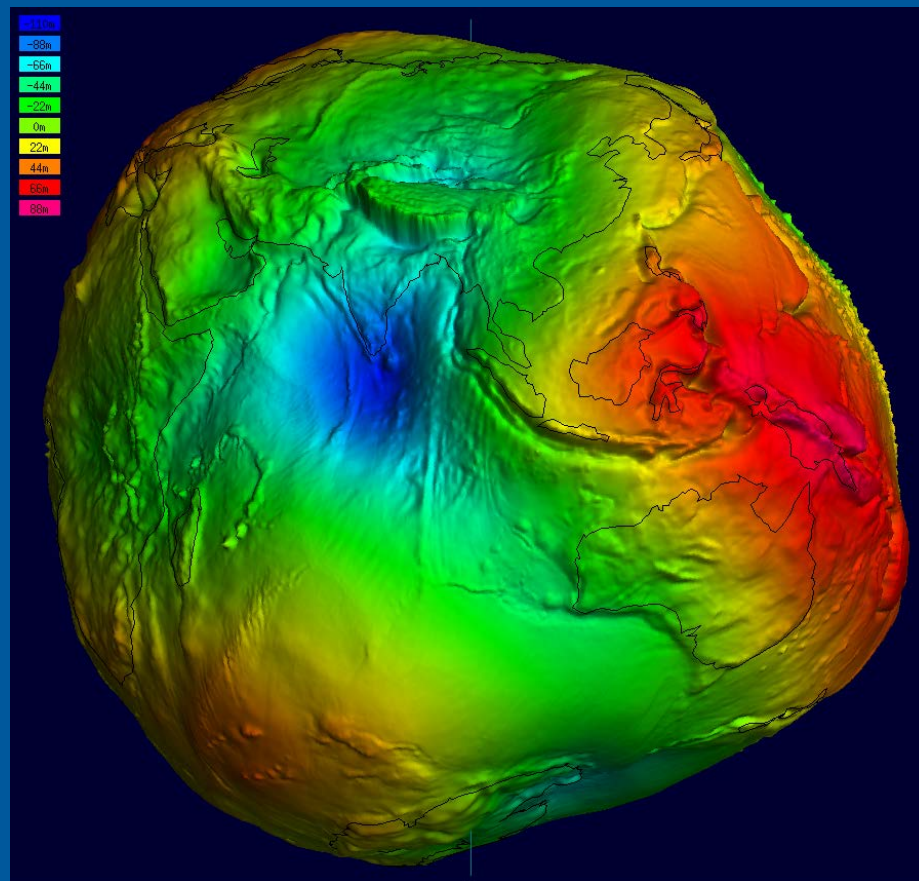
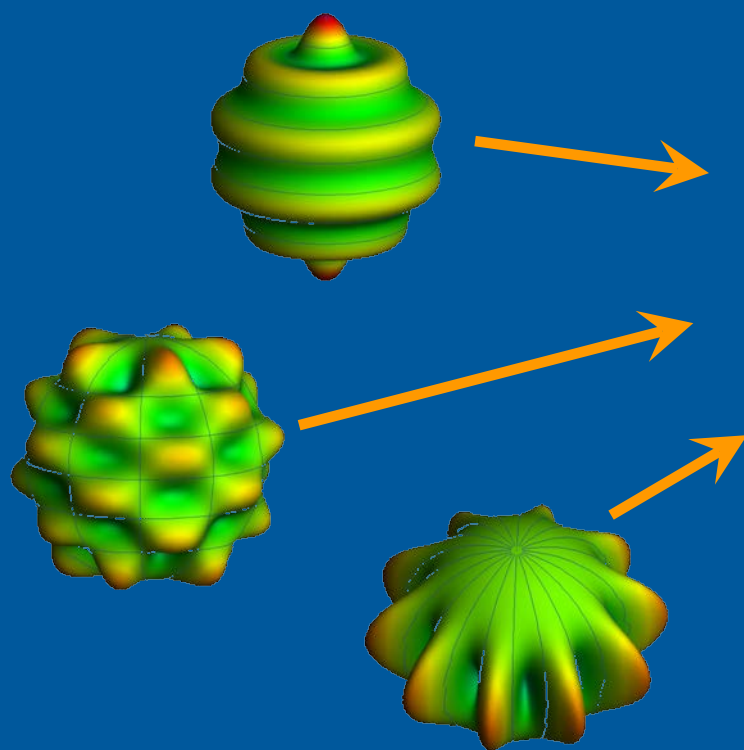
tesseral

sectorial



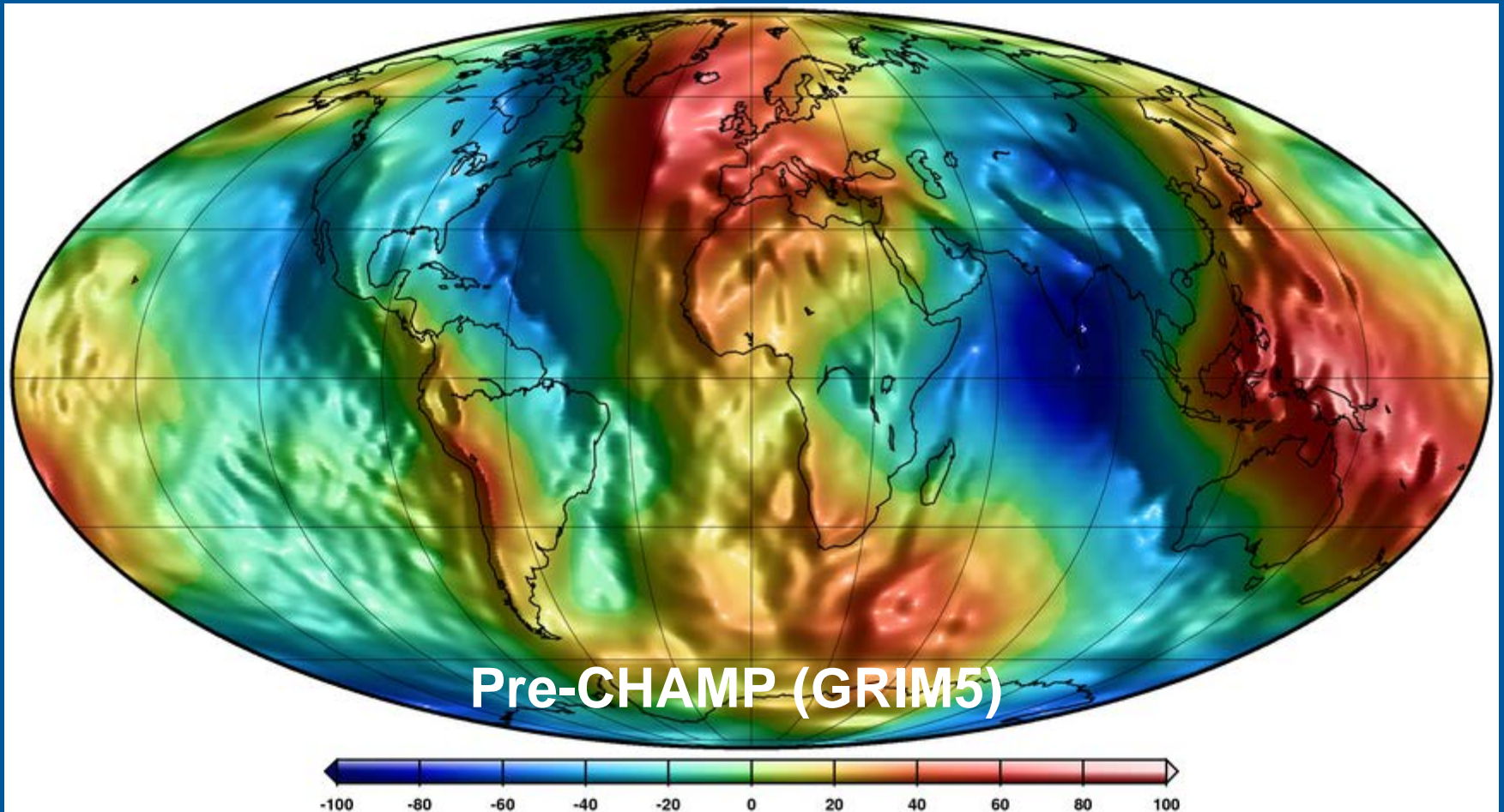
Mathematical Representation

$$W_a(r, \lambda, \varphi) = \frac{GM}{r} \sum_{\ell=0}^{N_{max}} \left(\frac{R}{r}\right)^\ell \sum_{m=0}^{\ell} [C_{\ell m} Y_{\ell m}^c(\lambda, \varphi) + S_{\ell m} Y_{\ell m}^s(\lambda, \varphi)]$$



Improvement of the Global Models

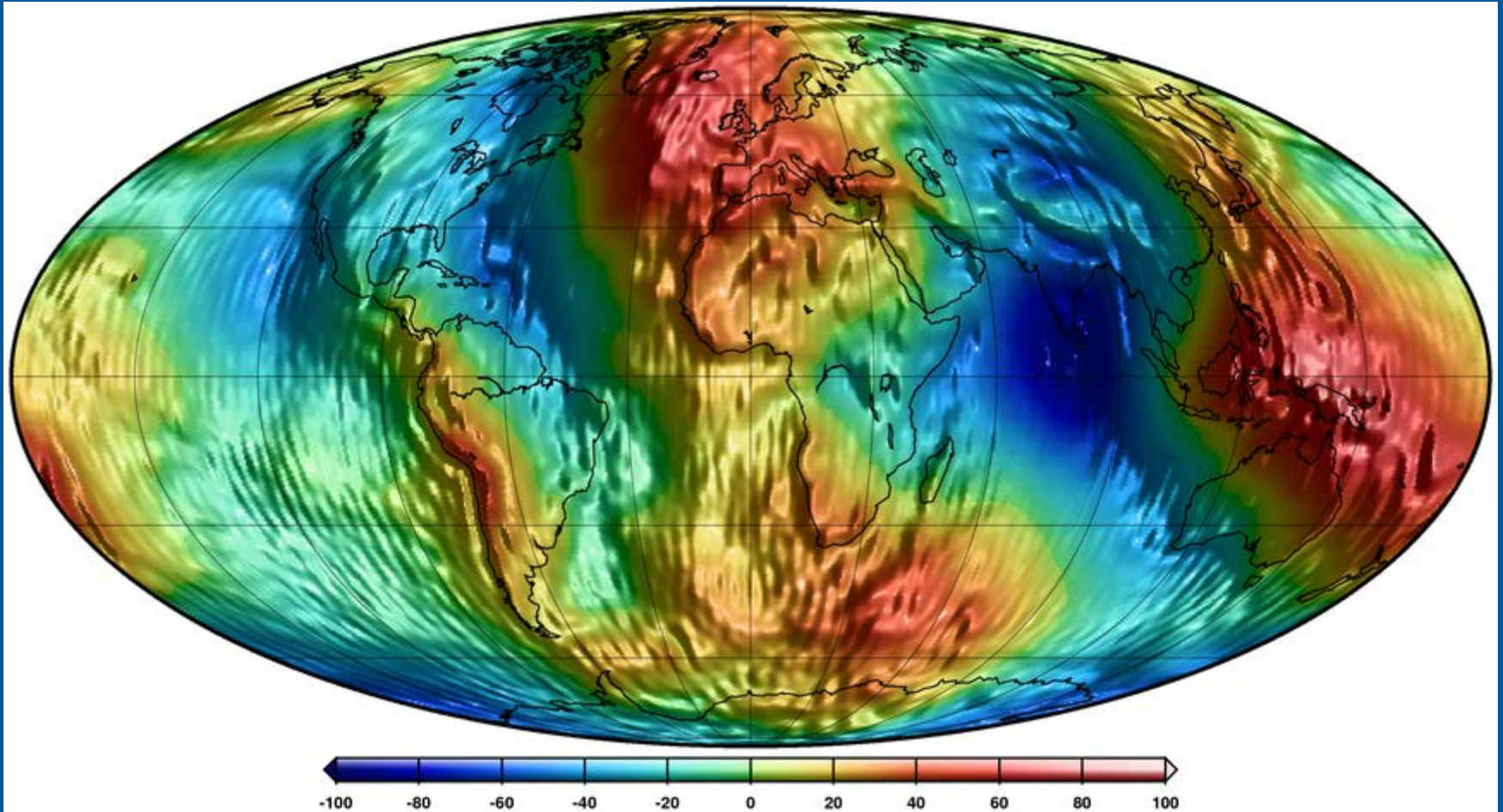
Geoid [m]



Improvement of the Global Models

Geoid [m]

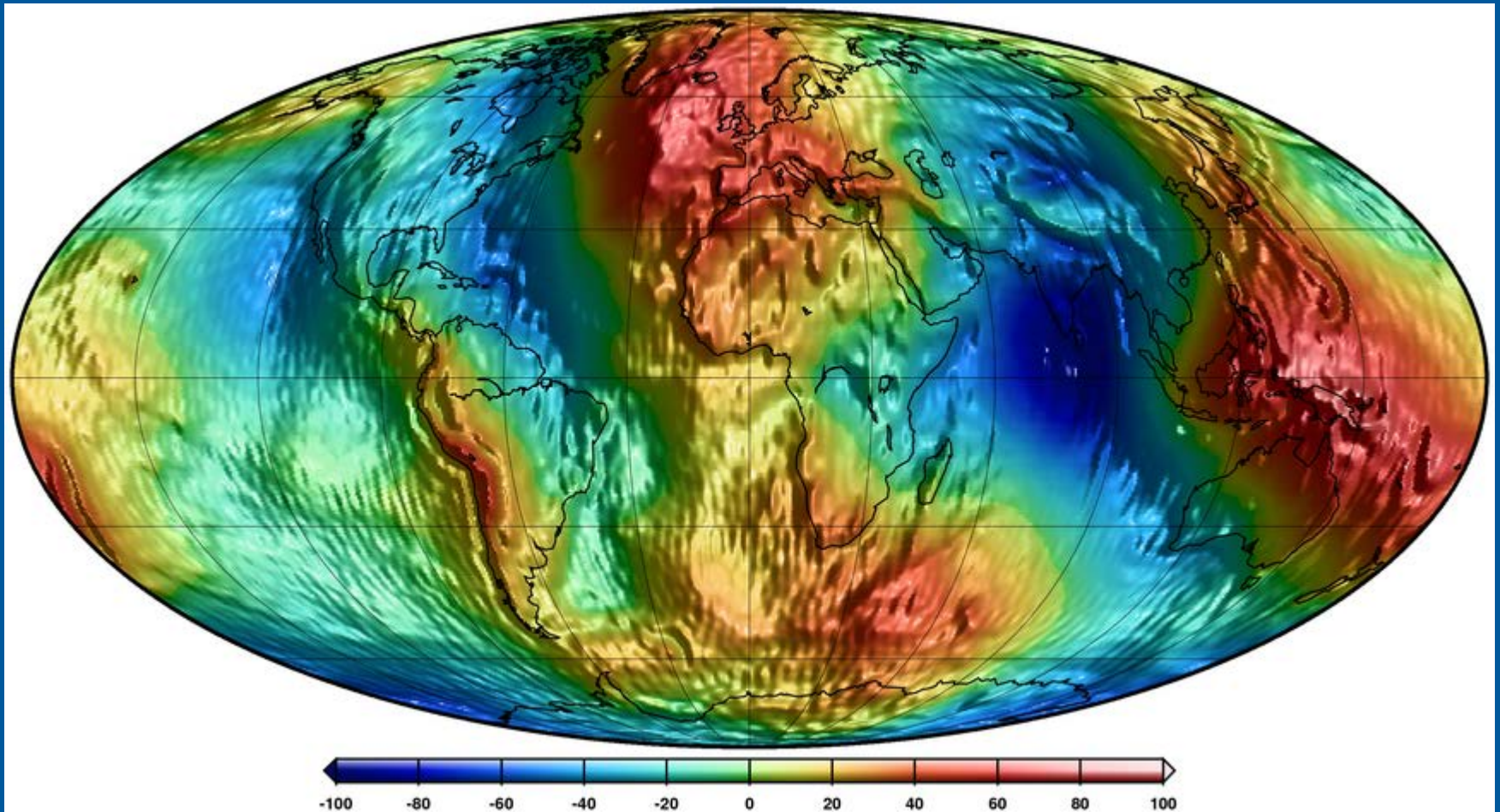
CHAMP 2004



Improvement of the Global Models

Geoid [m]

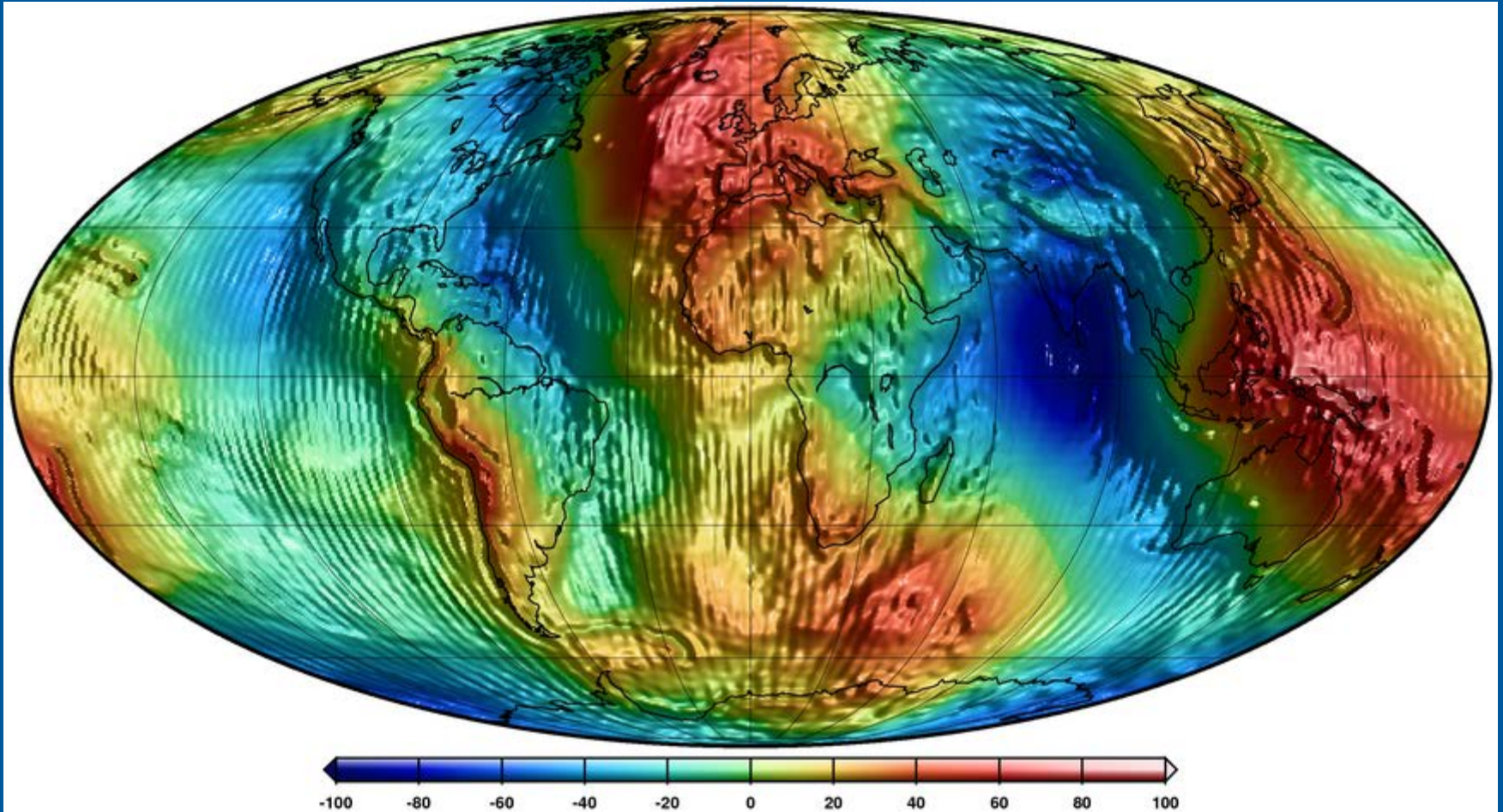
CHAMP 2010



Improvement of the Global Models

Geoid [m]

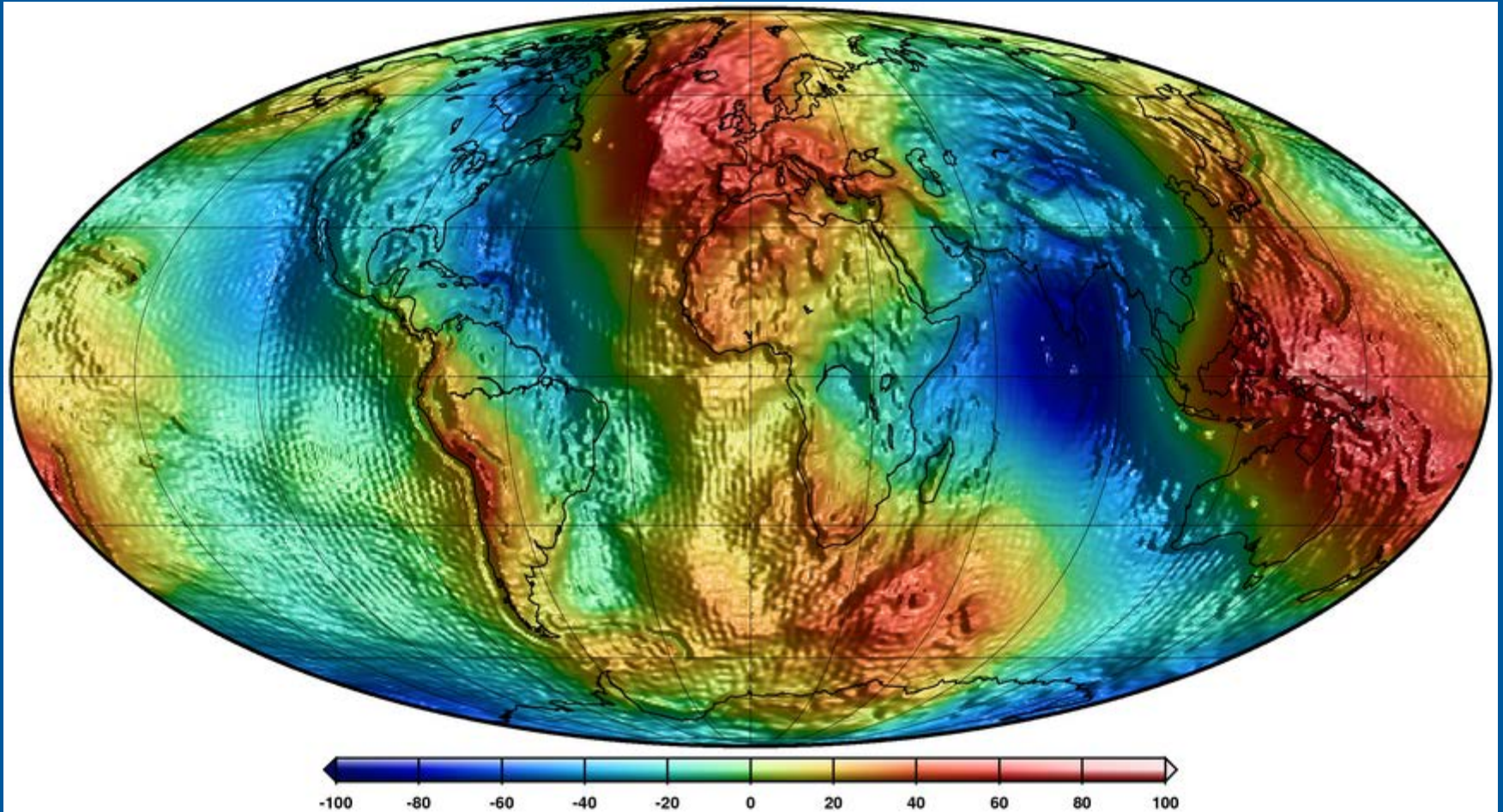
GRACE 2004



Improvement of the Global Models

Geoid [m]

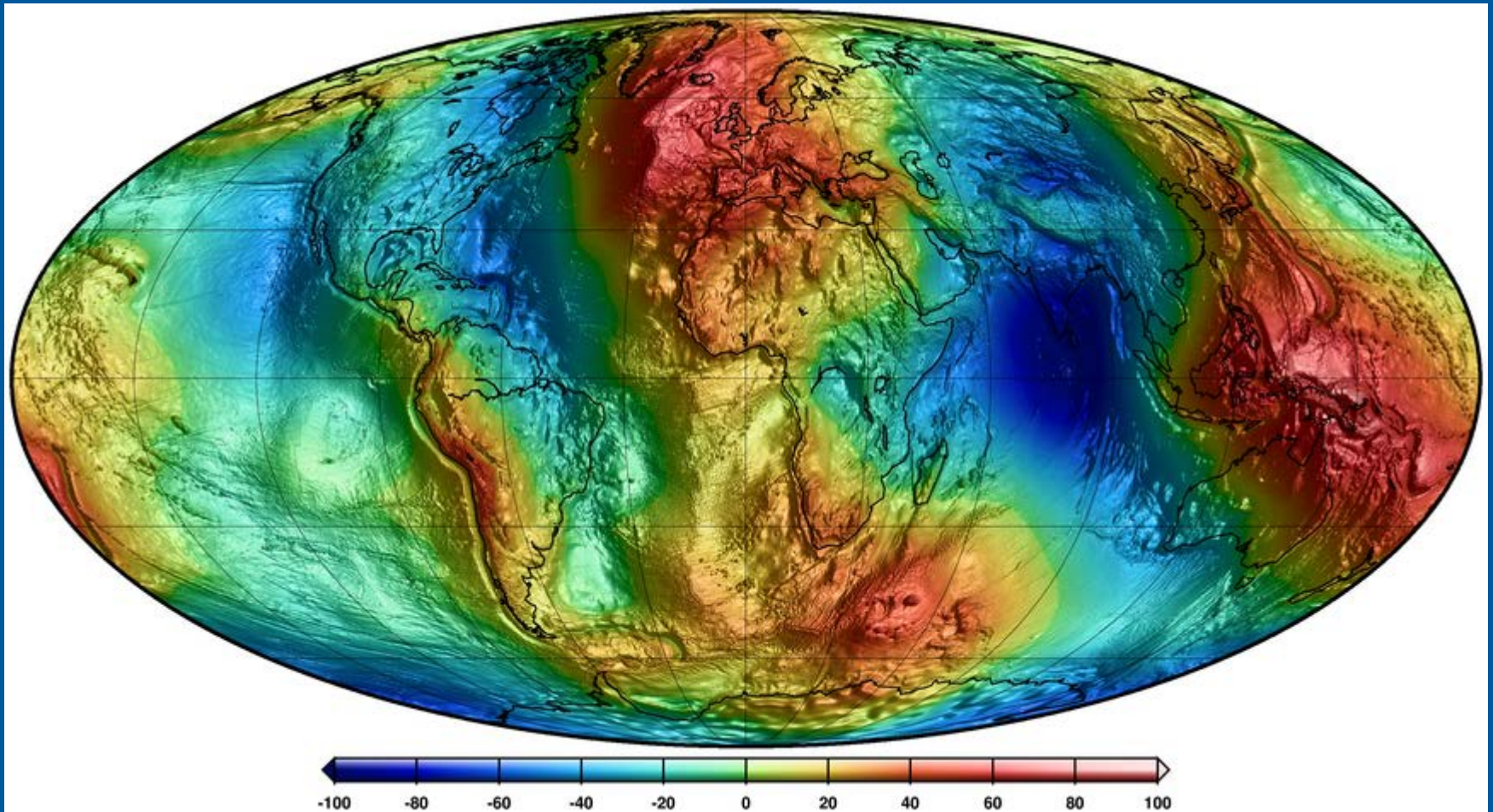
GRACE 2010



Improvement of the Global Models

Geoid [m]

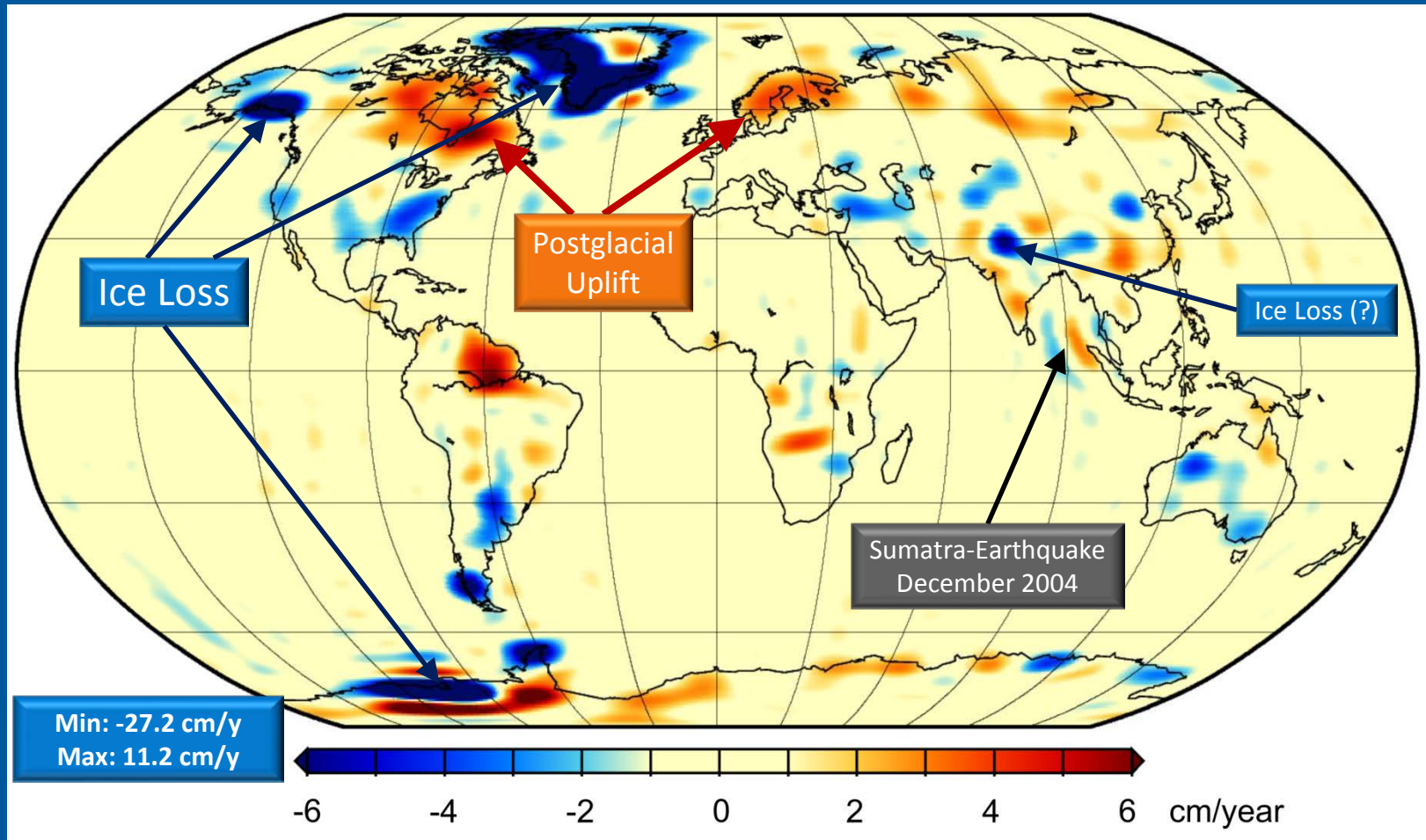
GRACE + GOCE + surface data



Change in Gravity Field from GRACE

Linear Trend from the model EIGEN-6 (time span: 1 Jan 2003 till 30 June 2009)

Geoid \rightarrow Equivalent Water Height (cm/year)



ICGEM – A Service of the IAG



International
Association of
Geodesy

Since 2003

Commission 2 "Gravity Field"

IGFS - International Gravity Field Service

BGI

International
Gravity Bureau
CNES Toulouse

IGeS

International
Geoid Service
Polimi Milano

ICET

International
Centre for
Earth Tides
U.F. Polynesia

ICGEM

International
Centre for
Global
Earth Models

IDEMS

International
DEM Service
DeMontfort UK

IGFS

Technical
Centre
NGA

Objectives / Status of ICGEM

- collecting and archiving of all existing global gravity field models
- making them available on the web
- use of standardised format (self-explanatory) (→ accepted for GOCE / ESA)
- interactive visualisation of the models, their differences, and their time variation
- web-interface to calculate different gravity field functionals from the spherical harmonic models on freely selectable grids (filtering included)
- evaluation of the models (→ differences in the frequency domain, comparison with GPS/levelling)
- answering of questions (online discussion forum / guest book)

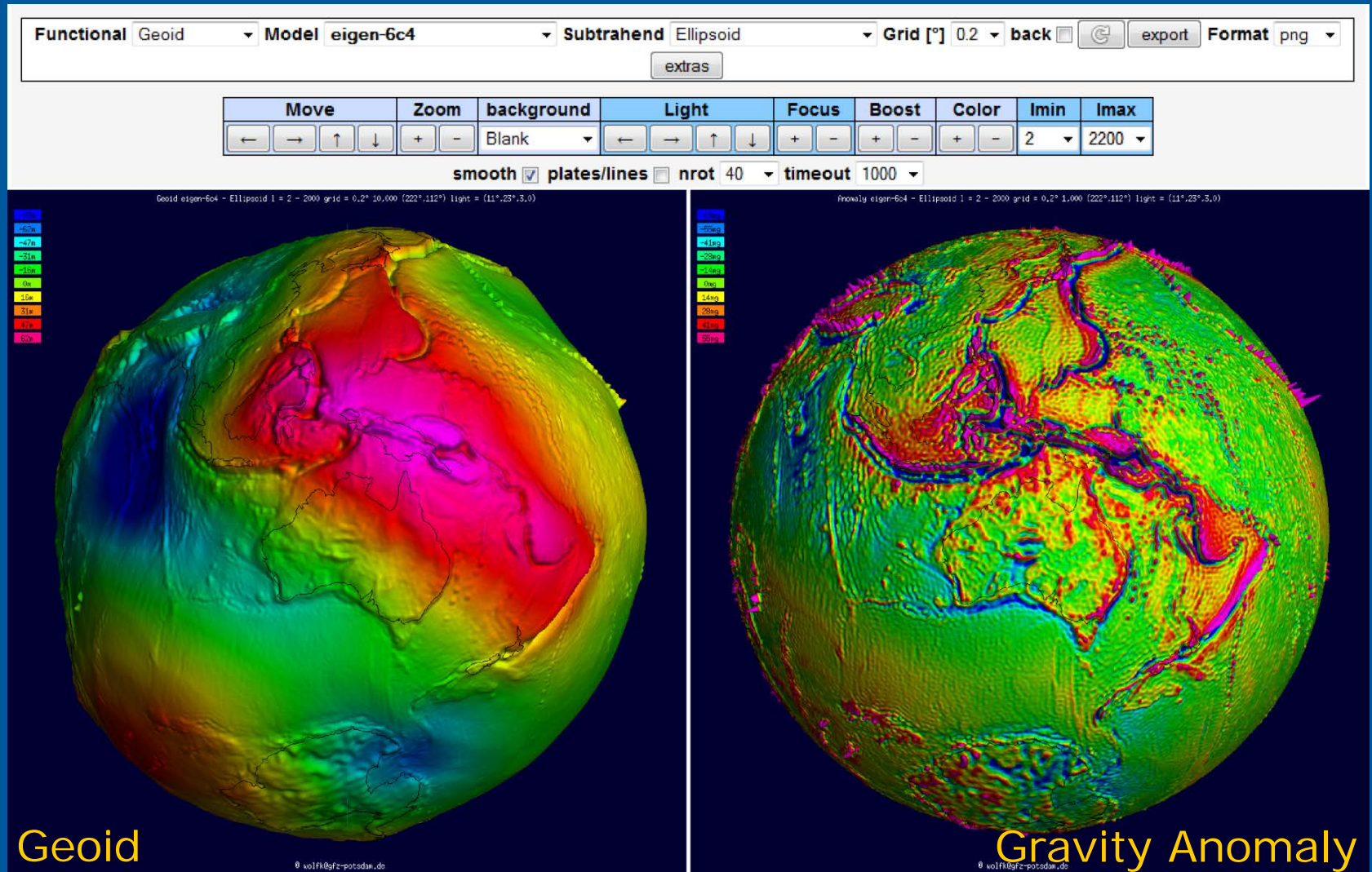
Table of available Models

| Nr ▲ | Model 11 | Year 11 | Degree 11 | Data 11 | Reference 11 | download | calculate | show |
|---------|----------------------|------------|--------------|------------------------------|-------------------------|---|---------------------------|----------------------|
| 150 | GOCO05s | 2015 | 280 | S(see model) | Mayer-Gürr, et al. 2015 | gfc zip | calculate | show |
| 149 | GO_CONS_GCF_2_SPW_R4 | 2014 | 280 | S(Goce) | Gatti et al, 2014 | gfc zip | calculate | show |
| 148 | EIGEN-6C4 | 2014 | 2190 | S(Goce, Grace, Lageos), G, A | Förste et al, 2014 | gfc zip | calculate | show |
| 147 | ITSG-Grace2014s | 2014 | 200 | S(Grace) | Mayer-Gürr et al, 2014 | gfc zip | calculate | show |
| 146 | ITSG-Grace2014k | 2014 | 200 | S(Grace) | Mayer-Gürr et al, 2014 | gfc zip | calculate | show |
| 145 | GO_CONS_GCF_2_TIM_R5 | 2014 | 280 | S(Goce) | Brockmann et al, 2014 | gfc zip | calculate | show |
| 144 | GO_CONS_GCF_2_DIR_R5 | 2014 | 300 | S(Goce, Grace, Lageos) | Bruinsma et al, 2013 | gfc zip | calculate | show |
| 143 | JYY_GOCE04S | 2014 | 230 | S(Goce) | Yi et al, 2013 | gfc zip | calculate | show |
| 142 | GOGRA04S | 2014 | 230 | S(Goce, Grace) | Yi et al, 2013 | gfc zip | calculate | show |
| 141 | EIGEN-6S2 | 2014 | 260 | S(Goce, Grace, Lageos) | Rudenko et al. 2014 | gfc zip | calculate | show |
| 140 | GGM05S | 2014 | 180 | S(Grace) | Tapley et al, 2013 | gfc zip | calculate | show |



| | | | | | | | | |
|---|--------|------|----|------|------------------------------|---------------------|---------------------------|----------------------|
| 8 | GEM2 | 1972 | 16 | S, G | Lerch et al, 1972a | gfc | calculate | show |
| 7 | GEM1 | 1972 | 12 | S | Lerch et al, 1972a | gfc | calculate | show |
| 6 | KOCH71 | 1971 | 11 | S, G | Koch and Witte, 1971 | gfc | calculate | show |
| 5 | KOCH70 | 1970 | 8 | S, G | Koch and Morrison, 1970 | gfc | calculate | show |
| 4 | SE2 | 1969 | 22 | S, G | Gaposchkin and Lambeck, 1970 | gfc | calculate | show |
| 3 | OSU68 | 1968 | 14 | S, G | Rapp, 1968 | gfc | calculate | show |
| 2 | WGS66 | 1966 | 24 | G | WGS Committee, 1966 | gfc | calculate | show |
| 1 | SE1 | 1966 | 15 | S | Lundquist and Veis, 1966 | gfc | calculate | show |

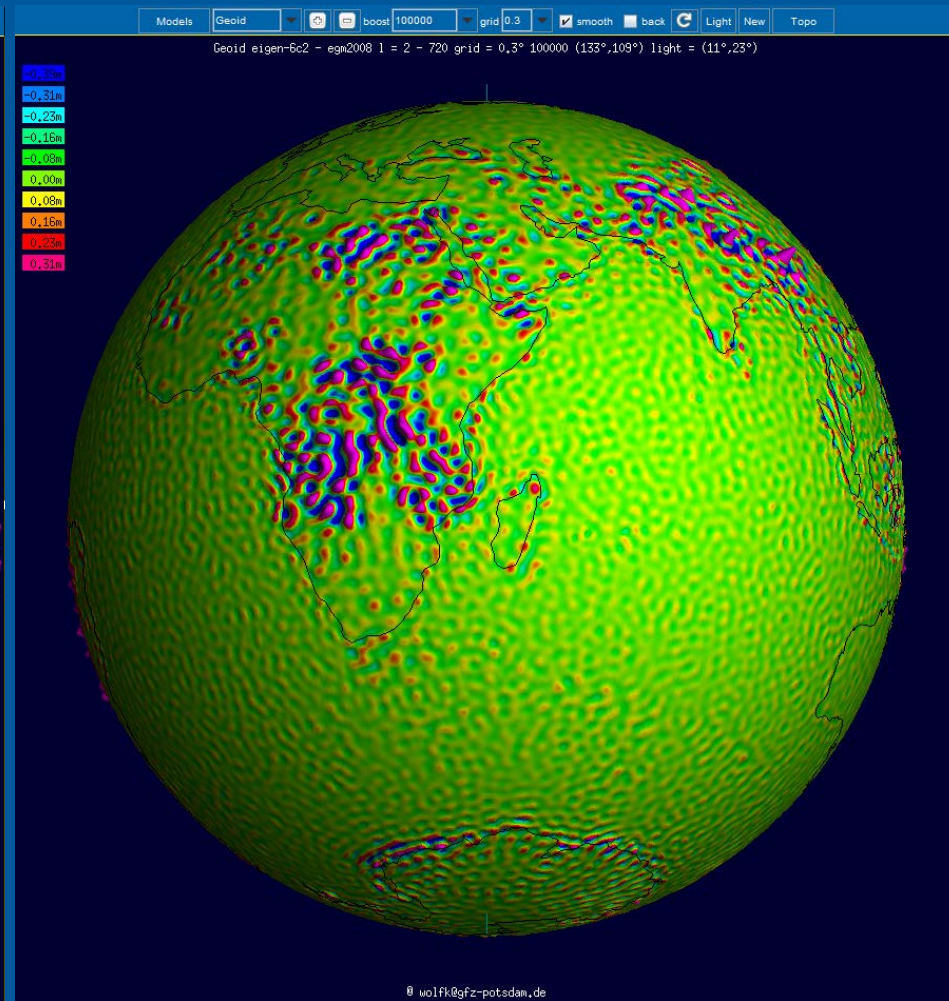
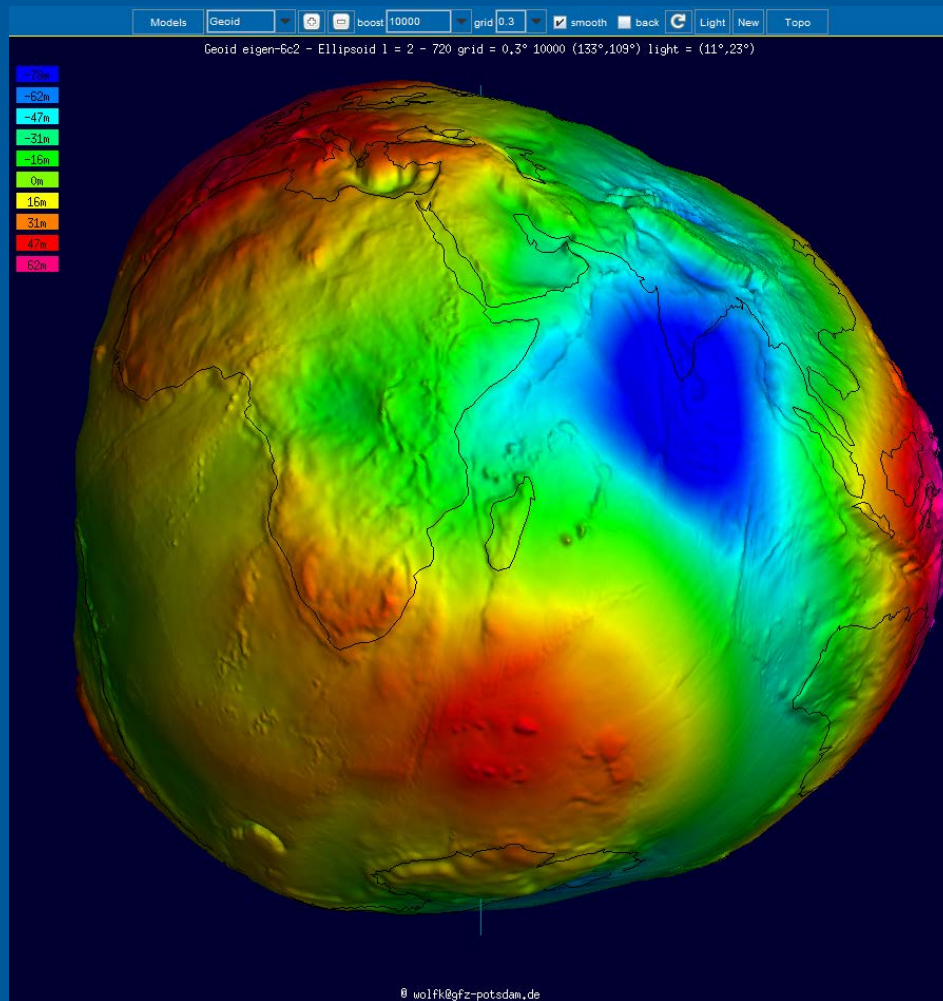
Interactive Visualisation Service



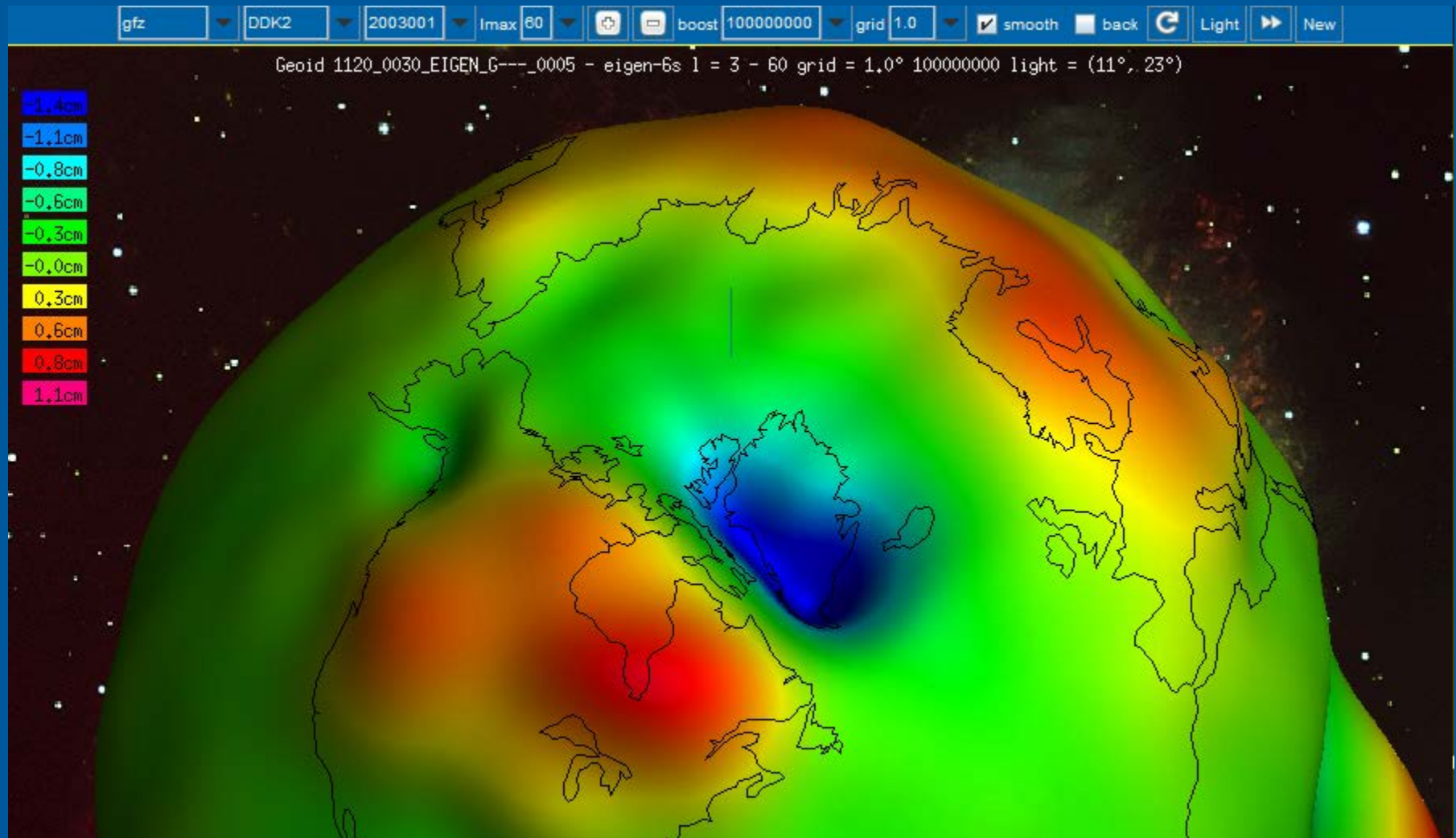
Interactive Visualisation Service

Geoid

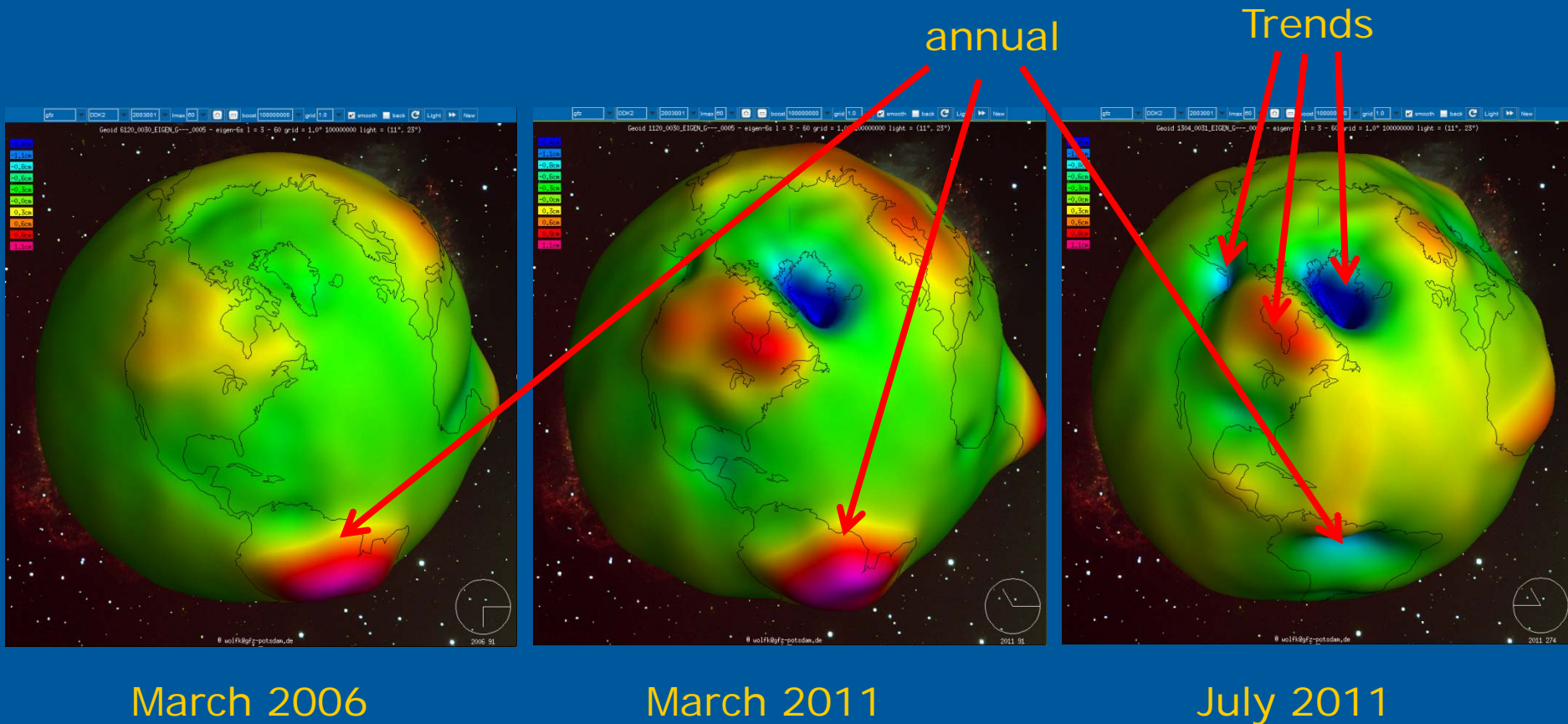
Differences of 2 Models



Visualisation of Monthly Solutions

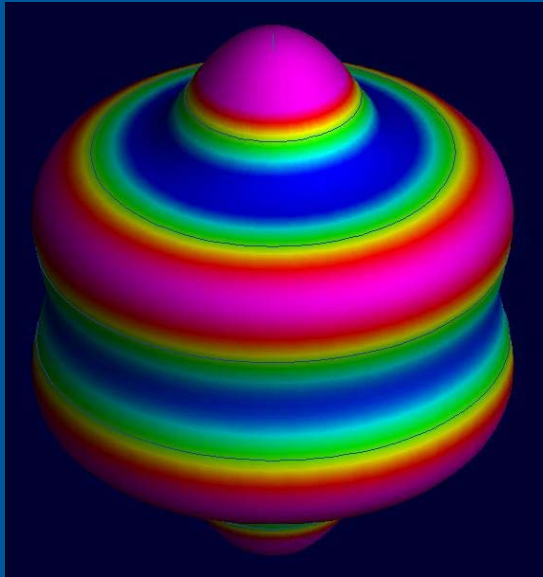


Visualisation of Monthly Solutions

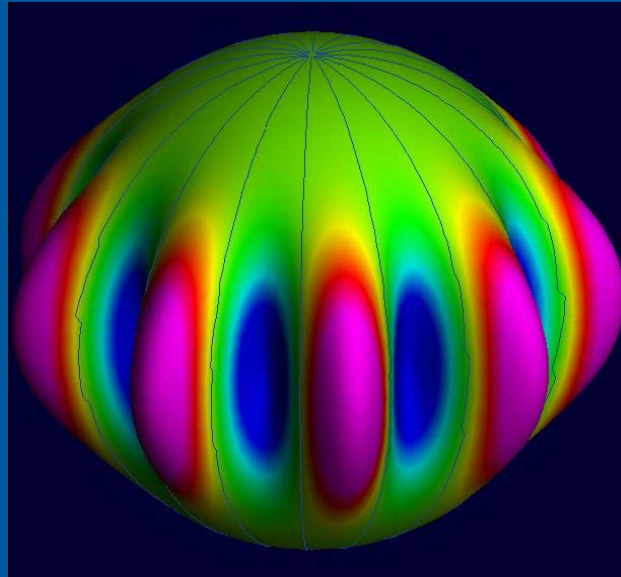


Interactive Visualisation Service

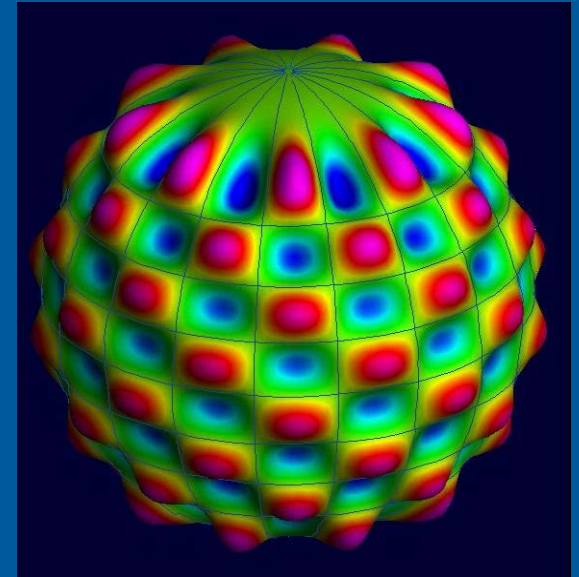
Spherical Harmonics as Tutorial



zonal: $\ell = 6, m = 0$

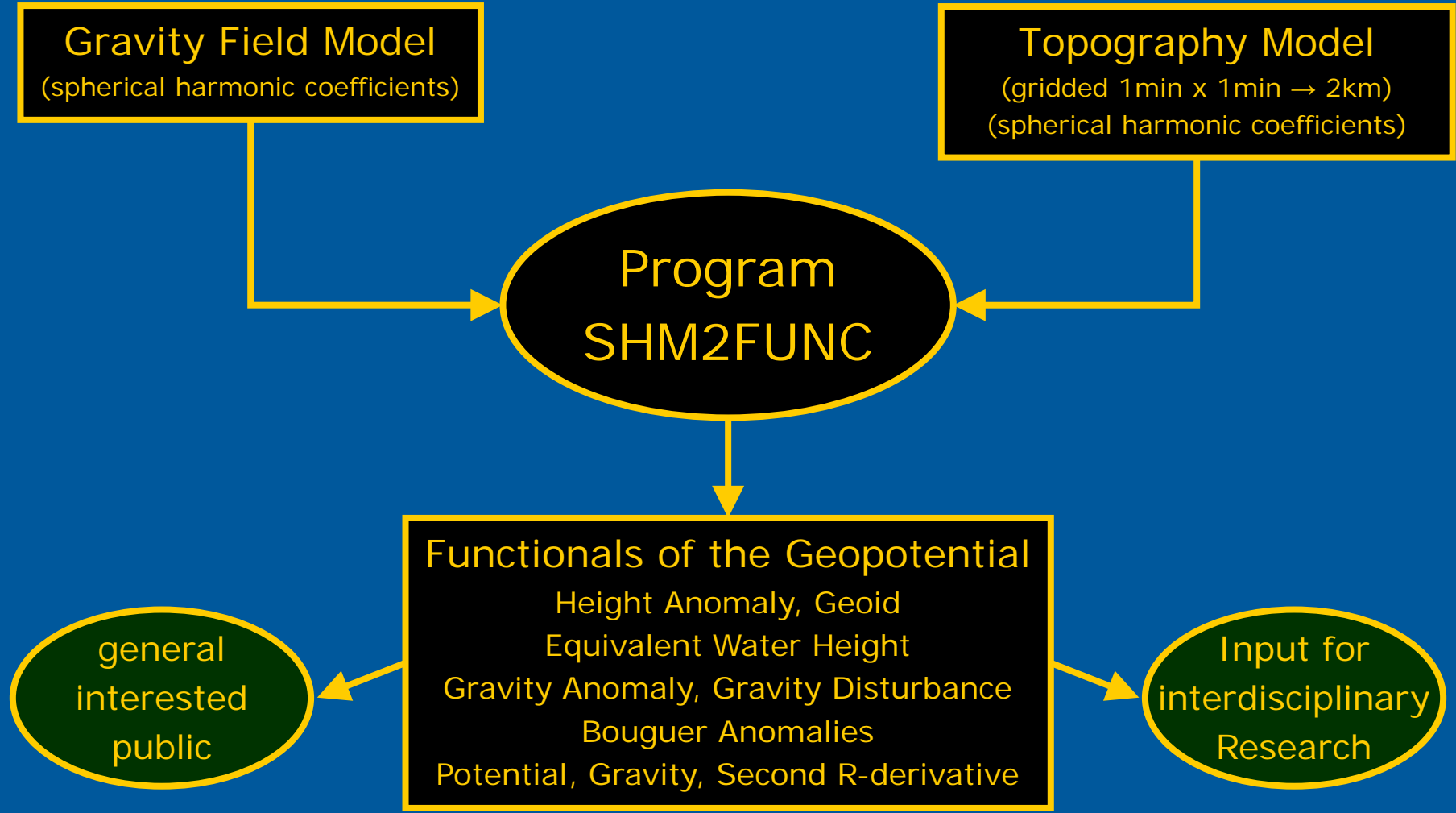


sectorial: $\ell = 9, m = 9$

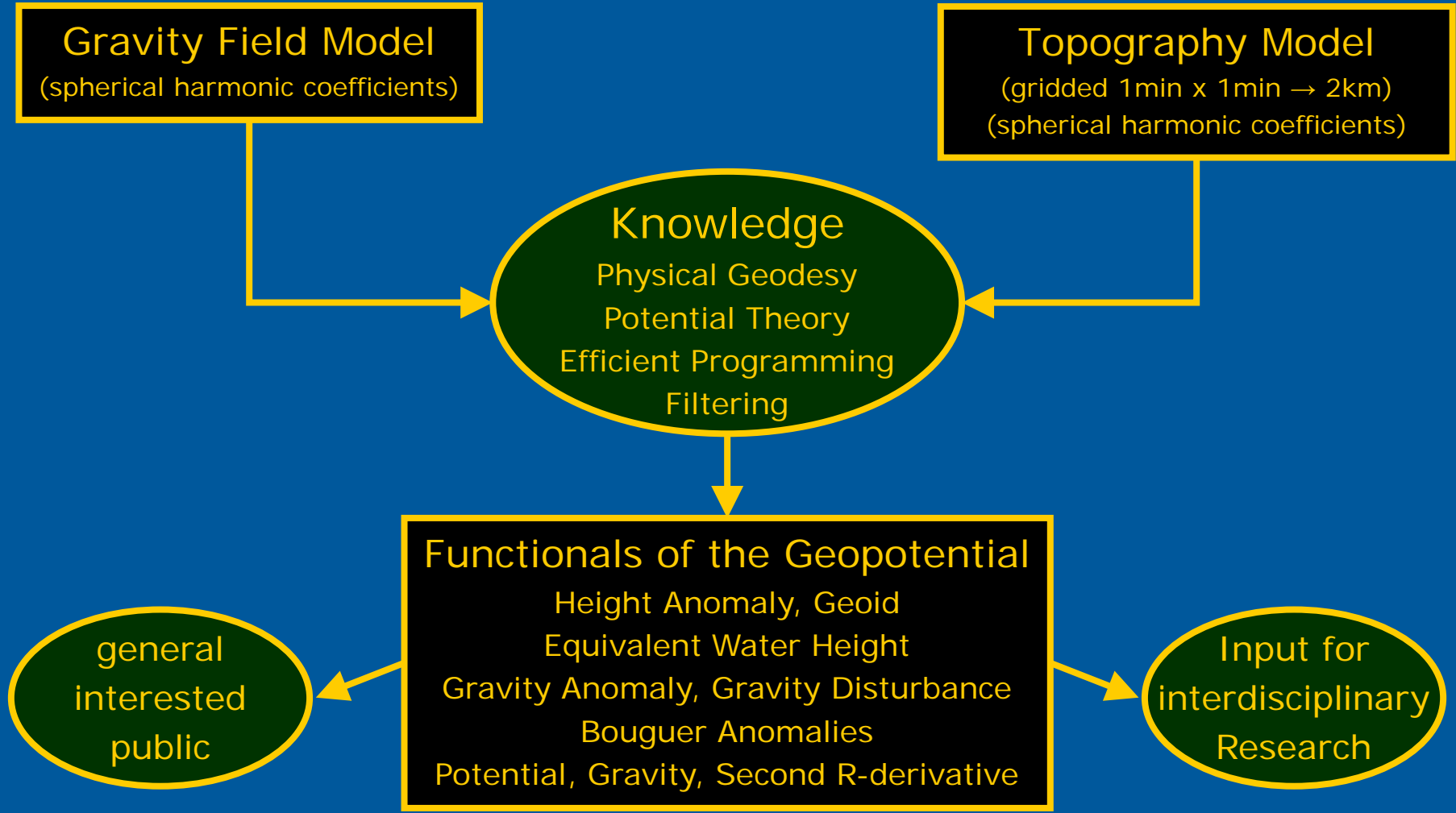


tesseral: $\ell = 16, m = 9$

Calculation Service



Calculation Service



Calculation Service

Web-Interface

| Model and Reference Selection | | Grid Selection | |
|-------------------------------|----------------------|---------------------------|-----|
| Reference System | WGS84 | Grid Step [°] | 0.1 |
| Model Directory | longtime models | Longitude Limit West [°] | 0 |
| Model File | eigen-6c4 | Longitude Limit East [°] | 360 |
| Functional | height_anomaly_ell | Latitude Limit South [°] | -90 |
| Tide System | use unmodified model | Latitude Limit North [°] | 90 |
| Zero Degree Term | yes | Height over Ellipsoid [m] | 0 |

| Truncation | | Gaussian Filtering | |
|------------------|-----------------------|-----------------------------|--------------|
| Maximal Degree | * max degree of model | Filter Type Definition | ** unused ** |
| Start Gentle Cut | ** unused ** | Filter Length in Degree [°] | |
| | | Filter Length in Meter [m] | |

start computation ☒ Image-File ☒ Illumination get grid file get PS file get PNG file input file show directory

functional 'height_anomaly_ell' for 'eigen-6c4' with 6,185,401 grid points (est. comp. time ~ 1611 sec)

Reference System

Model

Functional

Grid Density

Grid Area

Truncation

Filtering

Grids and Plots

Calculation Service

available functionals

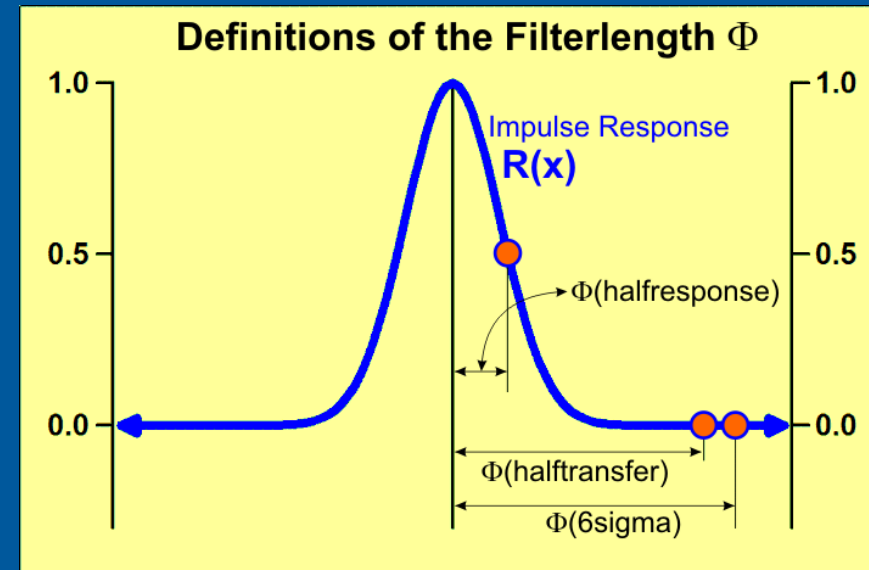
- height anomaly (on the Earth's surface, on the ellipsoid)
- geoid undulation
- gravity anomaly (Molodensky, classical \approx free air, spherical approximation, Bouguer)
- gravity disturbance (on the Earth' surface, spherical approximation)
- gravity (on the Earth' surface, on or above the ellipsoid)
- gravitation (on or above the ellipsoid)
- second radial derivative (on or above the ellipsoid)
- equivalent water height (including elastic deformation)
- potential (on or above the ellipsoid)

Calculation Service

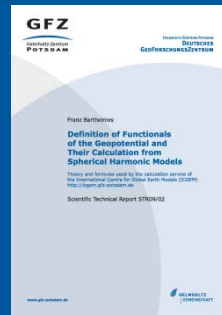
Explanation of the Functionals

| keyword | explanation |
|------------------------|--|
| height_anomaly | The so called "height anomaly" is an approximation of the geoid according to Molodensky's theory. It is equal to the geoid over sea. Here it will be calculated, as defined, on the Earth's surface approximated by Bruns' formula on the ellipsoid plus a first order correction (eqs. 81 and 119 of STR09/02). |
| height_anomaly_ell | The height anomaly can be generalised to a 3-d function, (sometimes called "generalised pseudo-height-anomaly"). Here it can be calculated on ($h=0$) or above ($h>0$) the ellipsoid, approximated by Bruns' formula (eqs. 78 and 118 of STR09/02). |
| geoid | The Geoid is one particular equipotential surface of the gravity potential of the Earth. Among all equipotential surfaces, the geoid is those which is equal to the undisturbed sea surface and its continuation below the continents. Here it will be approximated by the height anomaly plus a topography dependent correction term (eqs. 71 and 117 of STR09/02). |
| gravity_disturbance | The gravity disturbance is defined as the magnitude of the gradient of the potential at a given point minus the magnitude of the gradient of the normal potential at the same point. Here it will be calculated on the Earth's surface (eqs. 87 and 121 – 124 of STR09/02). |
| gravity_disturbance_sa | The gravity disturbance calculated by spherical approximation (eqs. 92 and 125 of STR09/02) on ($h=0$) or above ($h>0$) the ellipsoid. |
| gravity_anomaly | The gravity anomaly (according to Molodensky's theory) is defined as the magnitude of the gradient of the potential on the Earth's surface minus the magnitude of the gradient of the normal potential on the Telluroid (Earth's surface minus height anomaly) (eqs. 101 and 121 – 124 of STR09/02). |
| gravity_anomaly_cl | The classical gravity anomaly is defined as the magnitude of the gradient of the downward continued potential on the geoid minus the magnitude of the gradient |

Explanation of the Filtering



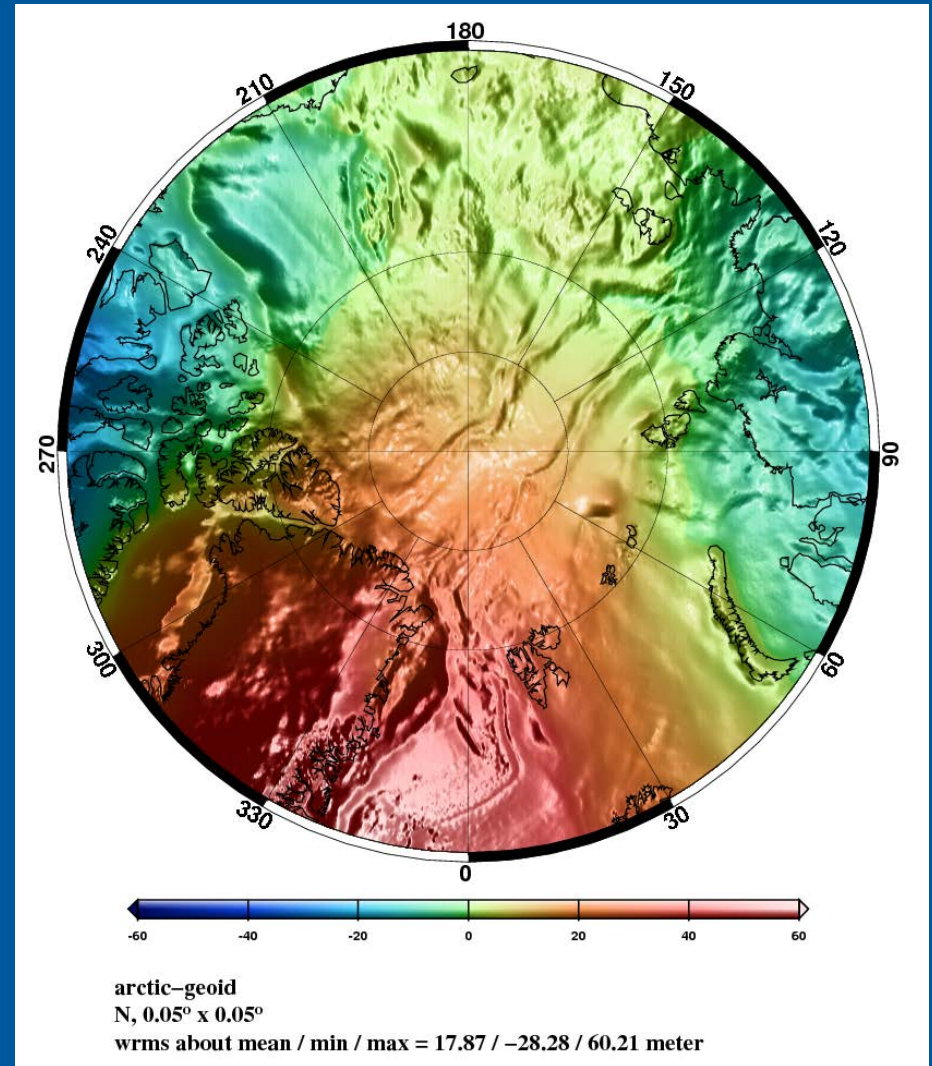
Theory and Formulas
 ➔ Link to: Report STR09/02



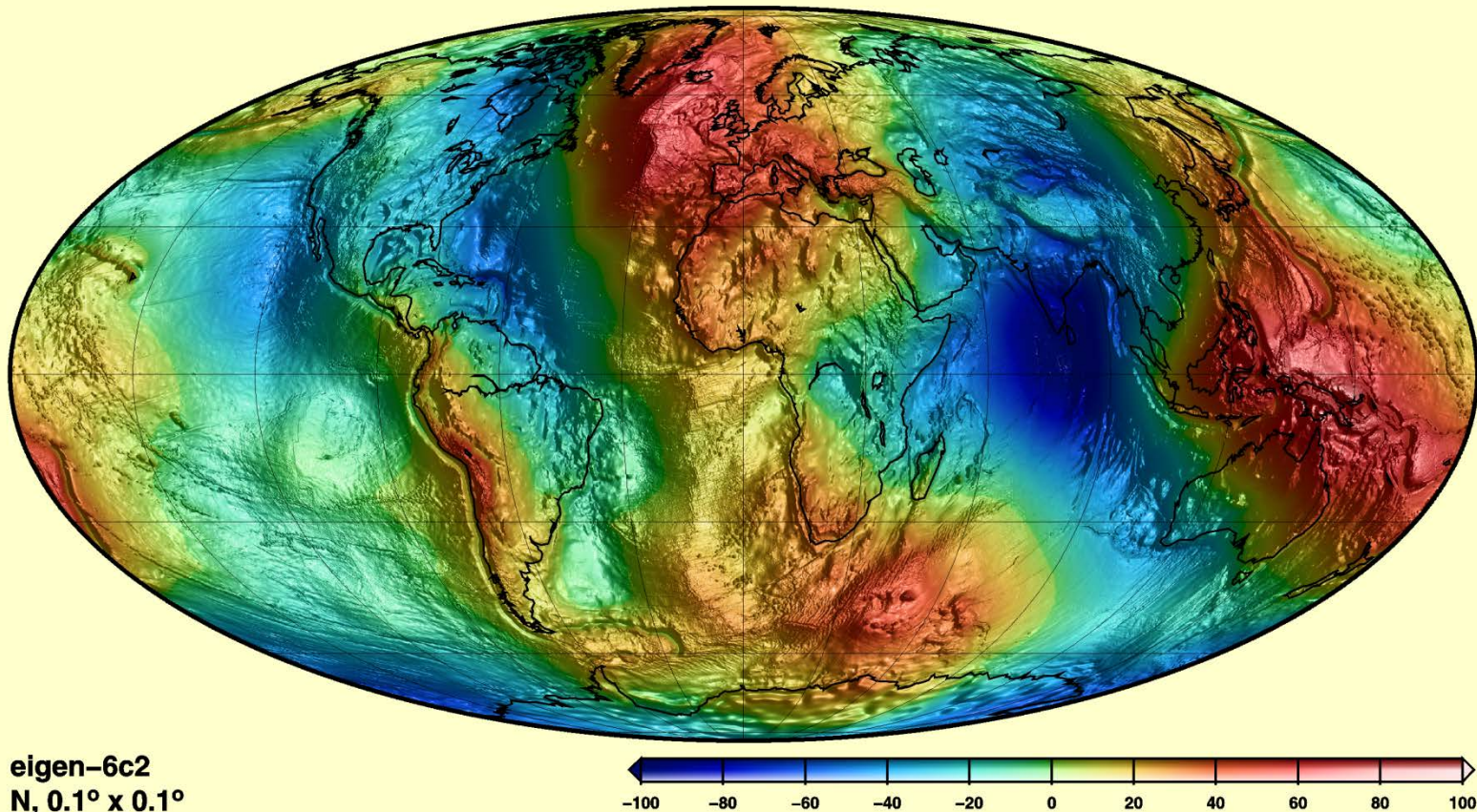
Calculation Service

Calculation of downloadable Grids

- freely selectable grid areas
- automatic generation of plots



Calculation Service



eigen-6c2

N, $0.1^\circ \times 0.1^\circ$

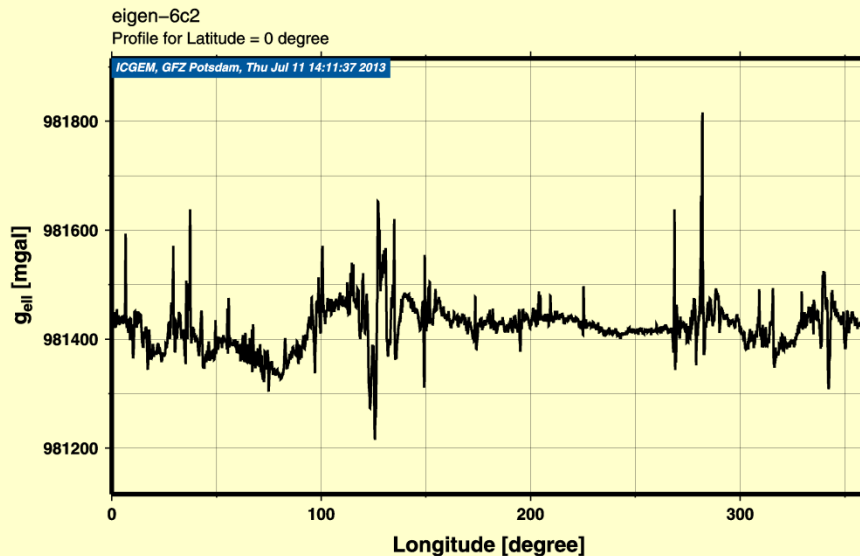
wrms about mean / min / max = 30.59 / -106.5 / 86.38 meter

ICGEM, GFZ Potsdam, Thu Jul 11 09:23:59 2013

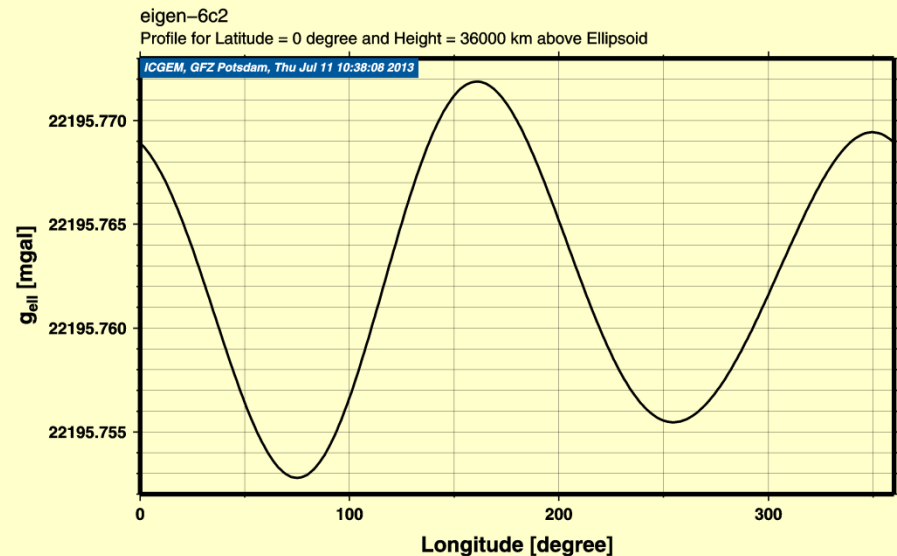
Calculation Service

Cross Sections (here: gravitation on and above the ellipsoid)

Cross Section along Latitude



Cross Section along Latitude



Evaluation of the Models

Comparisons in the
spectral domain

→ plot for each model

GO_CONS_GCF_2_DIR_R4 spectral comparison with the model EIGEN-6C2

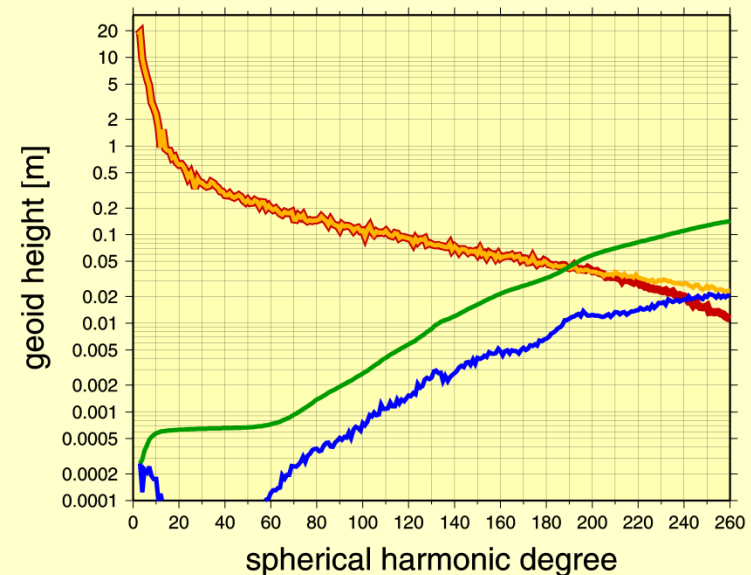
The graphs show:

Signal amplitudes per degree of GO_CONS_GCF_2_DIR_R4

Signal amplitudes per degree of EIGEN-6C2

Difference amplitudes per degree of
GO_CONS_GCF_2_DIR_R4 vs. EIGEN-6C2

Difference amplitudes as a function of maximum degree of
GO_CONS_GCF_2_DIR_R4 vs. EIGEN-6C2



Evaluation of the Models

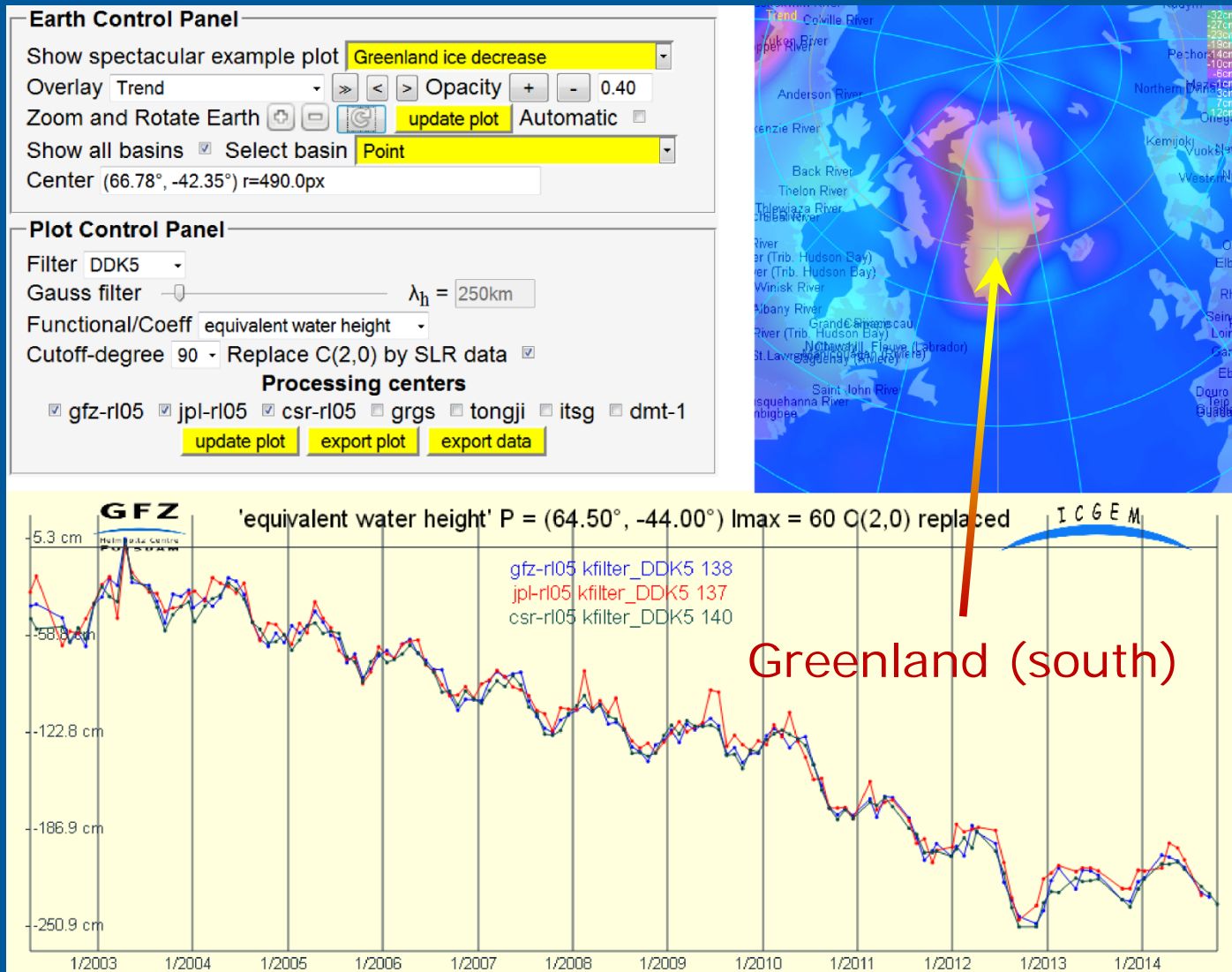
Comparisons with GPS-levelling data

The table is interactively re-sortable for all columns by clicking in the header cells.

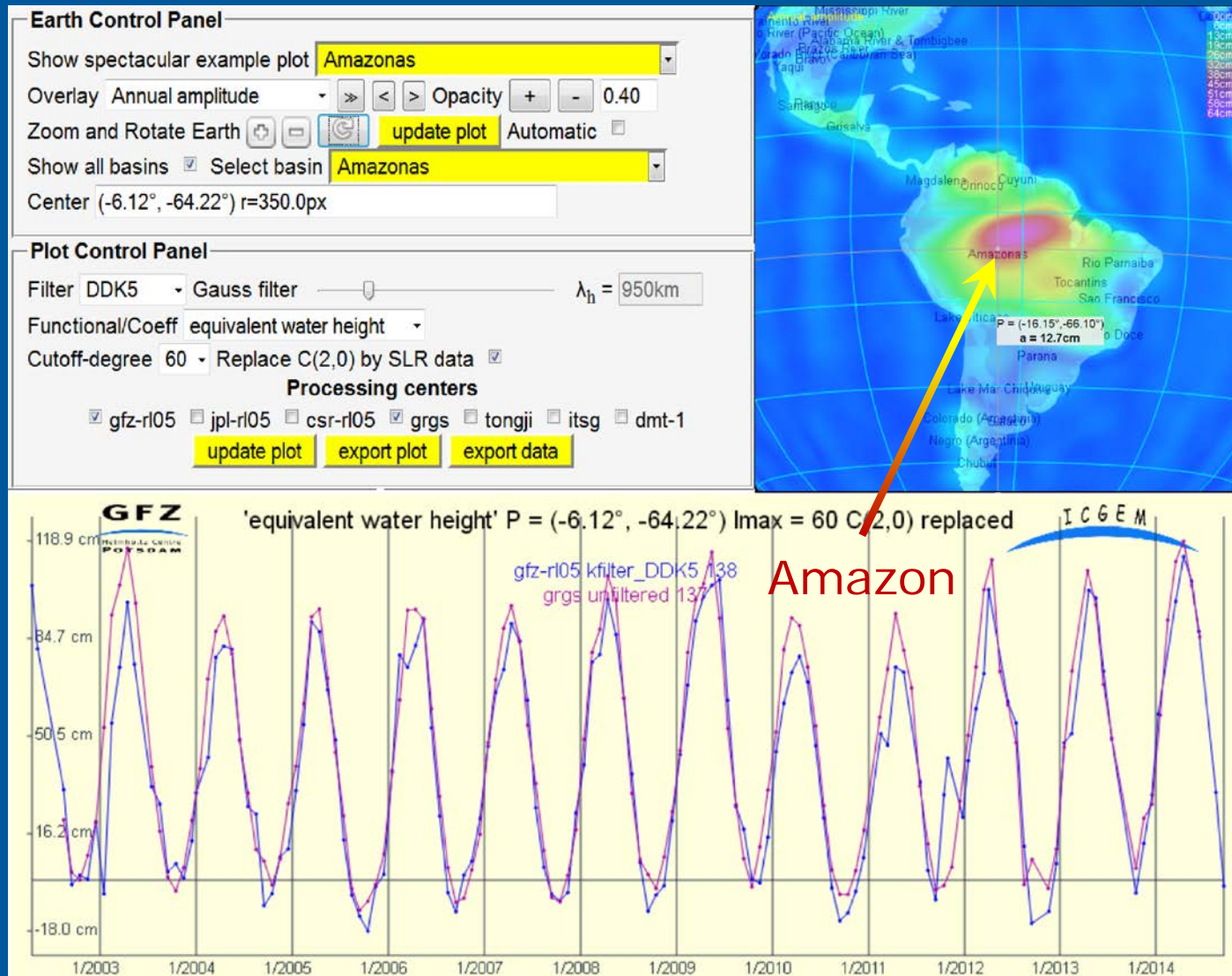
| Nr▲ | Model 11 | Nmax 11 | USA 11 6169 points | Canada 11 2691 points | Europe 11 1235 points | Australia 11 201 points | Japan 11 816 points | Brazil 11 1112 points | All 11 12224 points |
|-----|----------------------|---------|--------------------------|-----------------------------|-----------------------------|----------------------------|---------------------------|-----------------------------|---------------------------|
| 136 | GOCO05S | 280 | 0.399 m | 0.308 m | 0.372 m | 0.335 m | 0.450 m | 0.505 m | 0.3921 m |
| 135 | GO CONS GCF 2 SPW R4 | 280 | 0.406 m | 0.330 m | 0.394 m | 0.322 m | 0.473 m | 0.508 m | 0.4037 m |
| 134 | EIGEN-6C4 | 2190 | 0.247 m | 0.126 m | 0.210 m | 0.212 m | 0.079 m | 0.446 m | 0.2408 m |
| 133 | ITSG-GRACE2014S | 200 | 1.095 m | 0.871 m | 1.015 m | 1.175 m | 0.932 m | 1.273 m | 1.0508 m |
| 132 | ITSG-GRACE2014K | 200 | 0.542 m | 0.419 m | 0.580 m | 0.433 m | 0.651 m | 0.611 m | 0.5350 m |
| 131 | GO CONS GCF 2 TIM R5 | 280 | 0.398 m | 0.310 m | 0.371 m | 0.336 m | 0.450 m | 0.505 m | 0.3919 m |
| 130 | GO CONS GCF 2 DIR R5 | 300 | 0.405 m | 0.299 m | 0.373 m | 0.327 m | 0.447 m | 0.507 m | 0.3937 m |
| 129 | JYY_GOCO04S | 230 | 0.422 m | 0.359 m | 0.416 m | 0.342 m | 0.506 m | 0.511 m | 0.4225 m |
| 128 | GOGRA04S | 230 | 0.421 m | 0.359 m | 0.415 m | 0.342 m | 0.507 m | 0.511 m | 0.4220 m |
| 127 | EIGEN-6S2 | 260 | 0.405 m | 0.322 m | 0.393 m | 0.337 m | 0.476 m | 0.512 m | 0.4025 m |
| 126 | GGM05S-UPTO150 | 150 | 0.640 m | 0.606 m | 0.699 m | 0.478 m | 0.876 m | 0.668 m | 0.6576 m |
| 125 | EIGEN-6C3STAT | 1949 | 0.247 m | 0.129 m | 0.212 m | 0.213 m | 0.078 m | 0.447 m | 0.2415 m |
| 124 | TONGJI-GRACE01 | 160 | 0.596 m | 0.595 m | 0.694 m | 0.495 m | 0.835 m | 0.682 m | 0.6314 m |
| 123 | JYY_GOCO02S | 230 | 0.422 m | 0.386 m | 0.423 m | 0.344 m | 0.516 m | 0.522 m | 0.4304 m |

| | | | | | | | | | |
|----|--------|----|----------|----------|----------|----------|---------|----------|-----------|
| 11 | WGS72 | 28 | 2.971 m | 2.248 m | 3.529 m | 2.984 m | 7.610 m | 3.721 m | 3.4777 m |
| 10 | GEM4 | 16 | 3.467 m | 3.145 m | 2.880 m | 3.314 m | 5.647 m | 3.058 m | 3.4987 m |
| 9 | GEM3 | 12 | 5.225 m | 4.954 m | 3.336 m | 3.954 m | 4.322 m | 4.655 m | 4.8767 m |
| 8 | GEM2 | 22 | 2.910 m | 3.359 m | 3.720 m | 3.003 m | 4.080 m | 3.677 m | 3.2625 m |
| 7 | GEM1 | 22 | 4.180 m | 5.075 m | 3.164 m | 3.449 m | 4.847 m | 2.713 m | 4.2348 m |
| 6 | KOCH71 | 11 | 17.179 m | 10.880 m | 12.101 m | 11.823 m | 6.075 m | 21.583 m | 15.3930 m |
| 5 | KOCH70 | 8 | 15.783 m | 12.300 m | 10.683 m | 13.334 m | 2.854 m | 10.538 m | 13.5699 m |
| 4 | SE2 | 22 | 3.897 m | 4.777 m | 4.434 m | 3.325 m | 4.924 m | 3.719 m | 4.2110 m |
| 3 | OSU68 | 14 | 4.261 m | 8.921 m | 3.654 m | 5.097 m | 4.013 m | 3.690 m | 5.5474 m |
| 2 | WGS66 | 24 | 3.206 m | 5.307 m | 3.360 m | 3.982 m | 5.853 m | 4.680 m | 4.1311 m |
| 1 | SE1 | 15 | 3.895 m | 5.071 m | 8.339 m | 3.826 m | 5.003 m | 6.003 m | 5.0527 m |

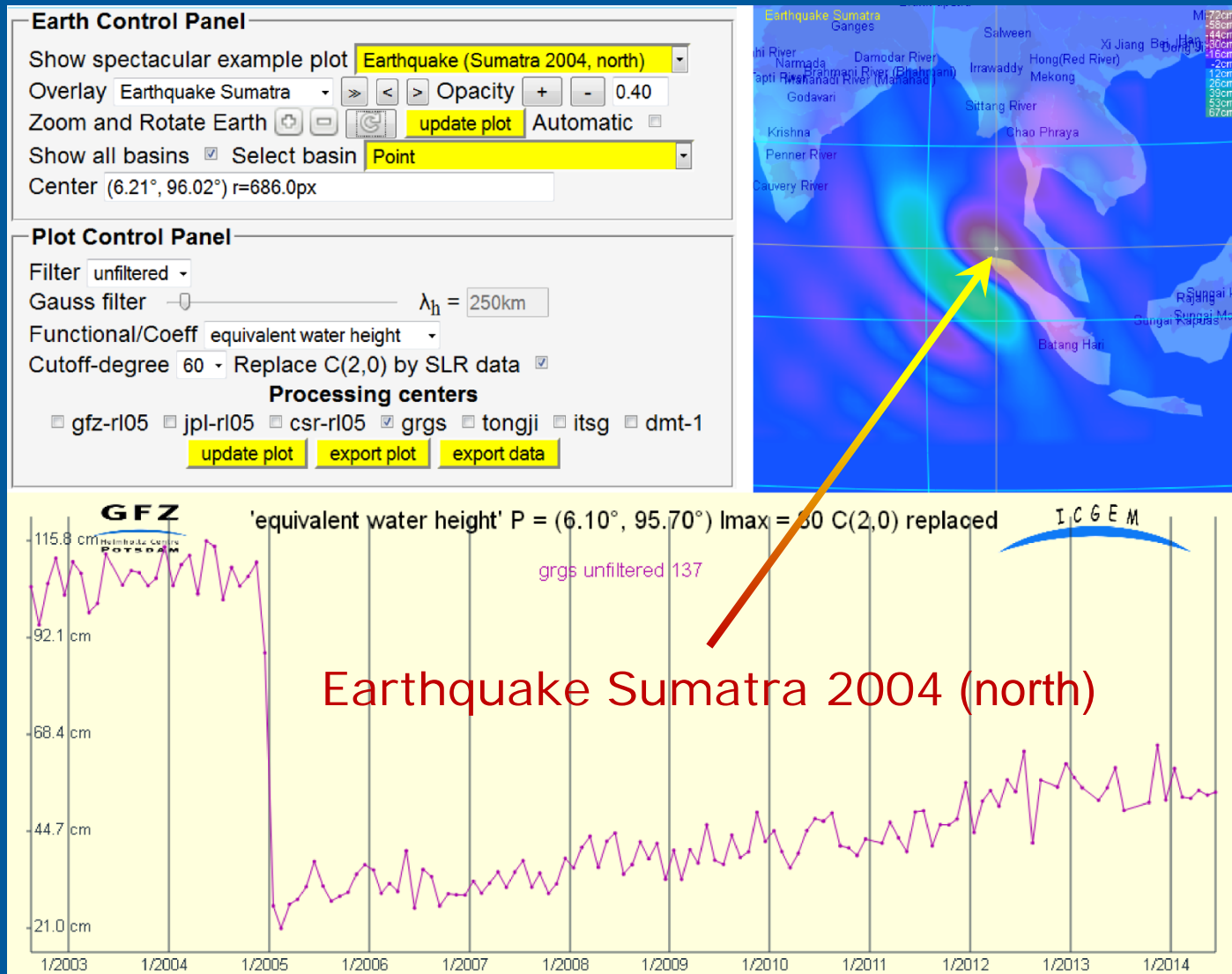
The G³-Browser (GFZ Grace Gravity Browser)



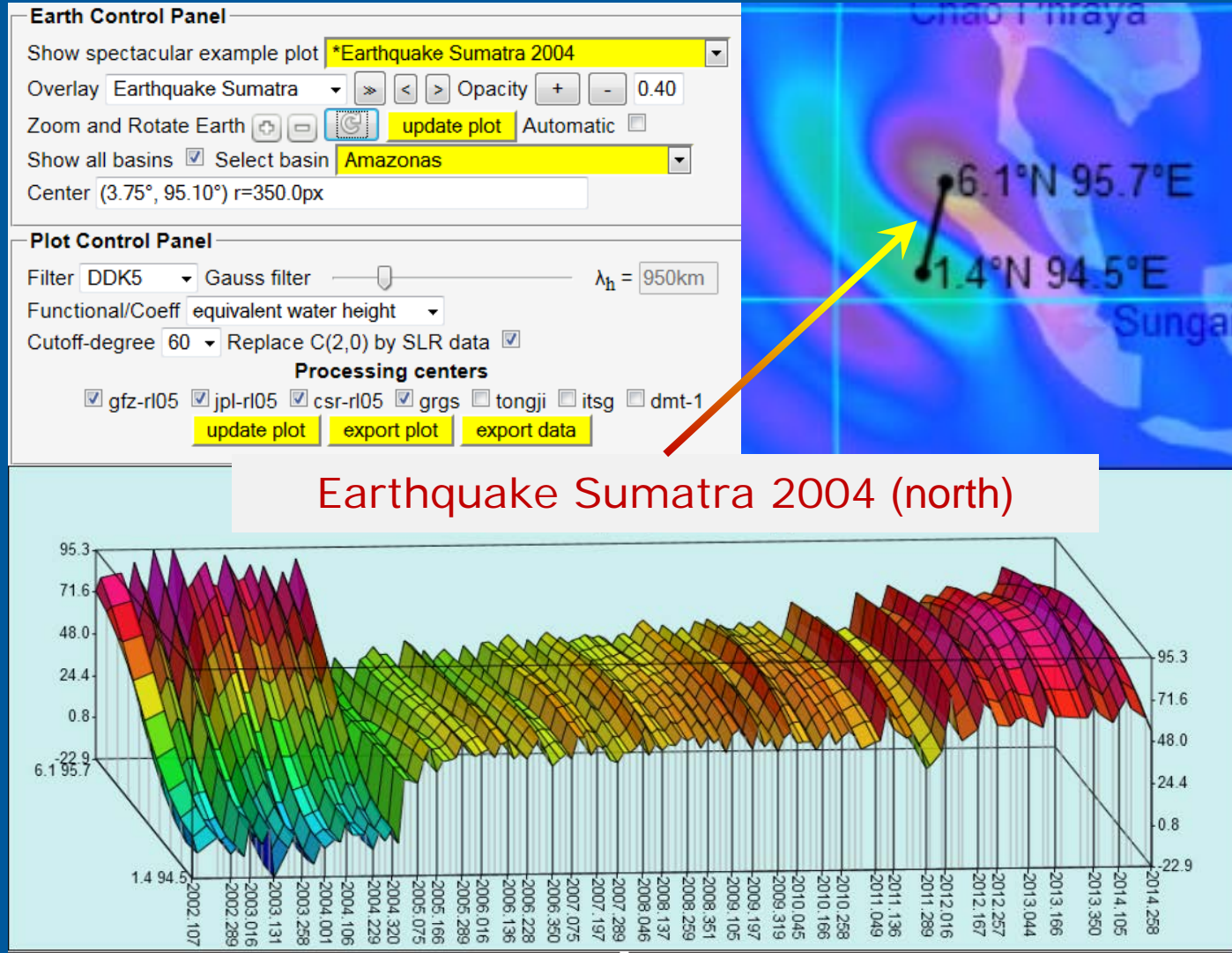
The G³-Browser (GFZ Grace Gravity Browser)



The G³-Browser (GFZ Grace Gravity Browser)



The G³-Browser (GFZ Grace Gravity Browser)

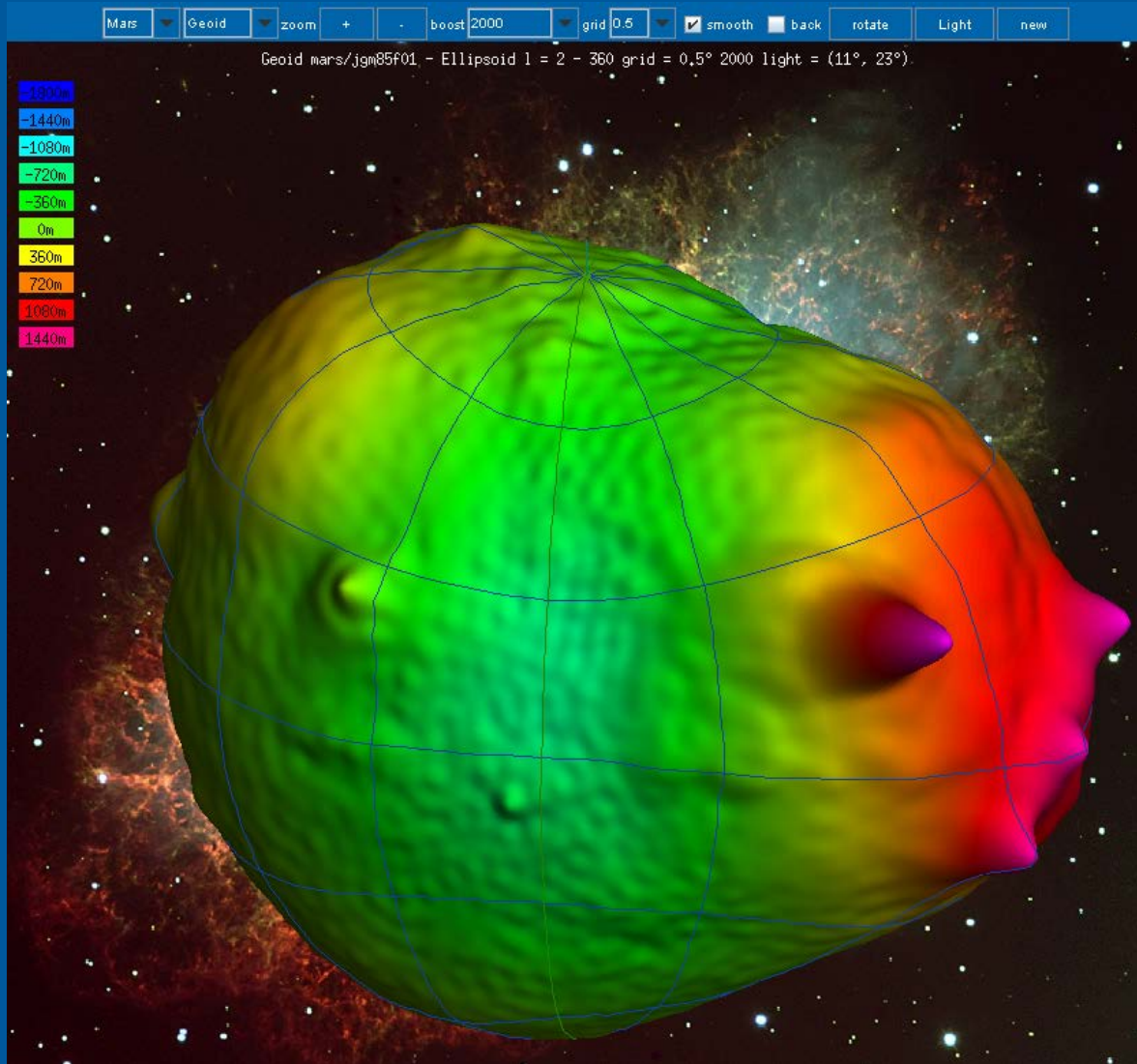


Latest Changes (and history)

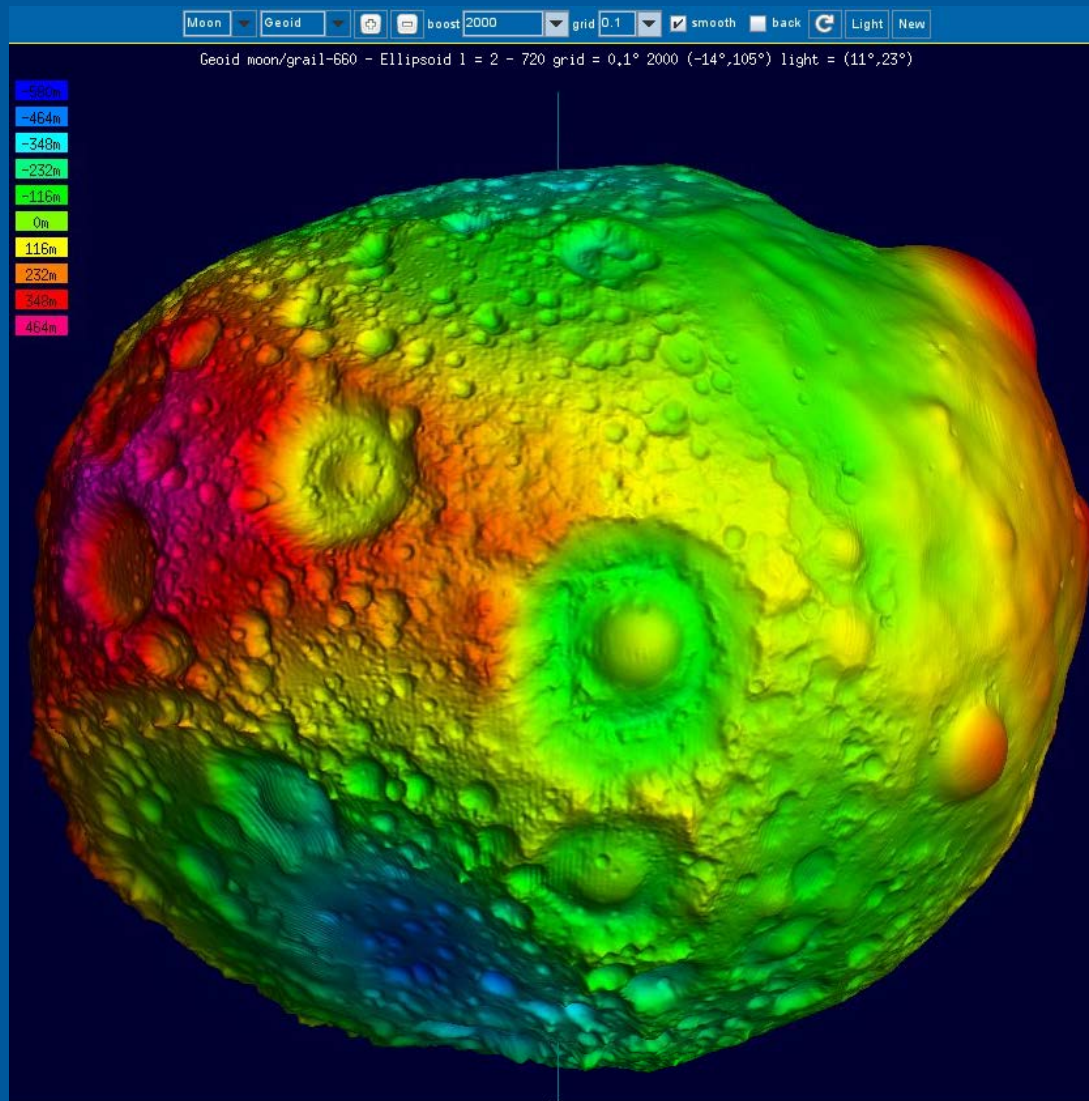
- **15. May 2015:**
Bugfix for the Visualizations Services: The computed grids for very small values of l_{max} ($l_{max} \leq 5$) contained extremely large numbers. Unfortunately, this error could have quite drastic consequences for the user: Since the Java-server-thread did not finish rendering, the limitation of access numbers could inhibit further connections for this client.
- **27. April 2015:**
The "G³ Browser" has the new feature to display 3D-grid-plots for cross-sections (a line defined by two end-points). Example plots for the two major Earthquakes and polar regions have been added.
- **16. April 2015:**
For the Visualization Services now also the functional Water column can be displayed (for static fields and monthly models of the Earth).
- **31. March 2015:**
New model GOCO05s included.
- **27. March 2015:**
The last two pages that contained Java applets ("Visualization of Monthly Models", "Calculation Service for Celestial Bodies") have been replaced with JavaScript versions. Our ICGEM-service is from now completely free of Java Applets!
- **25. March 2015:**
The server-program for visualizations ("potato-server.C") now enables computations for higher orders ($l_{max} > 360$) by an improved routine for Legendre polynoms.
- **9. March 2015:**
The Visualization Services (Potato.html, Tutorial.html, PotatoBodies.html) are now implemented completely in JavaScript (no Java Applets) to avoid Oracle's restrictions. It should now work for all operating systems and browsers. The ICGEM-service is now nearly Java-free (on the client-side). Additionally, users have now the option to download generated images as files, and in the page "Table of Models" the visualization of gravity models is now possible with a simple mouse click on the button 'show' (analogous to 'calculate').
- **30. January 2015:**
The table of models on the page Evaluation of Models is now also interactively sortable, allowing a direct ranking of the models for different regions (and complete GPS/levelling data set).
- **26. January 2015:**
 - The Calculation Service is now implemented completely in JavaScript (without Java Applets) to avoid the access restrictions introduced by Oracle. It should now work for all operating systems and browsers without trouble. Additionally, users have now the option to download generated images as PNG file.
 - The Table of Models is now sortable (for 'Model', 'Year', 'Degree', 'Data' and 'References'). The buttons calculate in the last column of the table now offer a direct link to the Calculation Service for the selected model.

Byproducts: Models of Moon, Mars and Venus

Mars

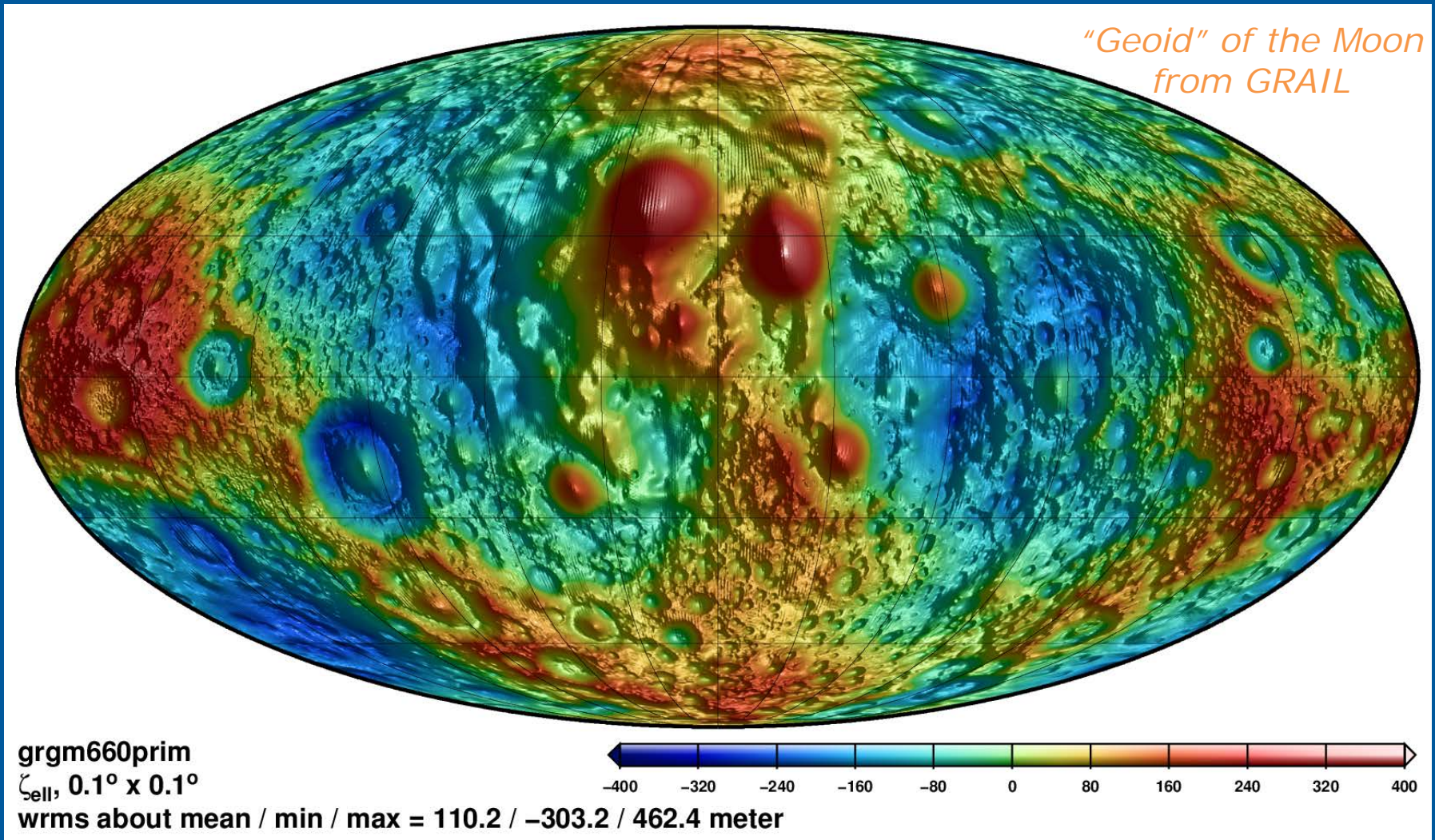


Byproducts: Models of Moon, Mars and Venus



Moon
(GRAIL-mission)

Byproducts: Models of Moon, Mars and Venus

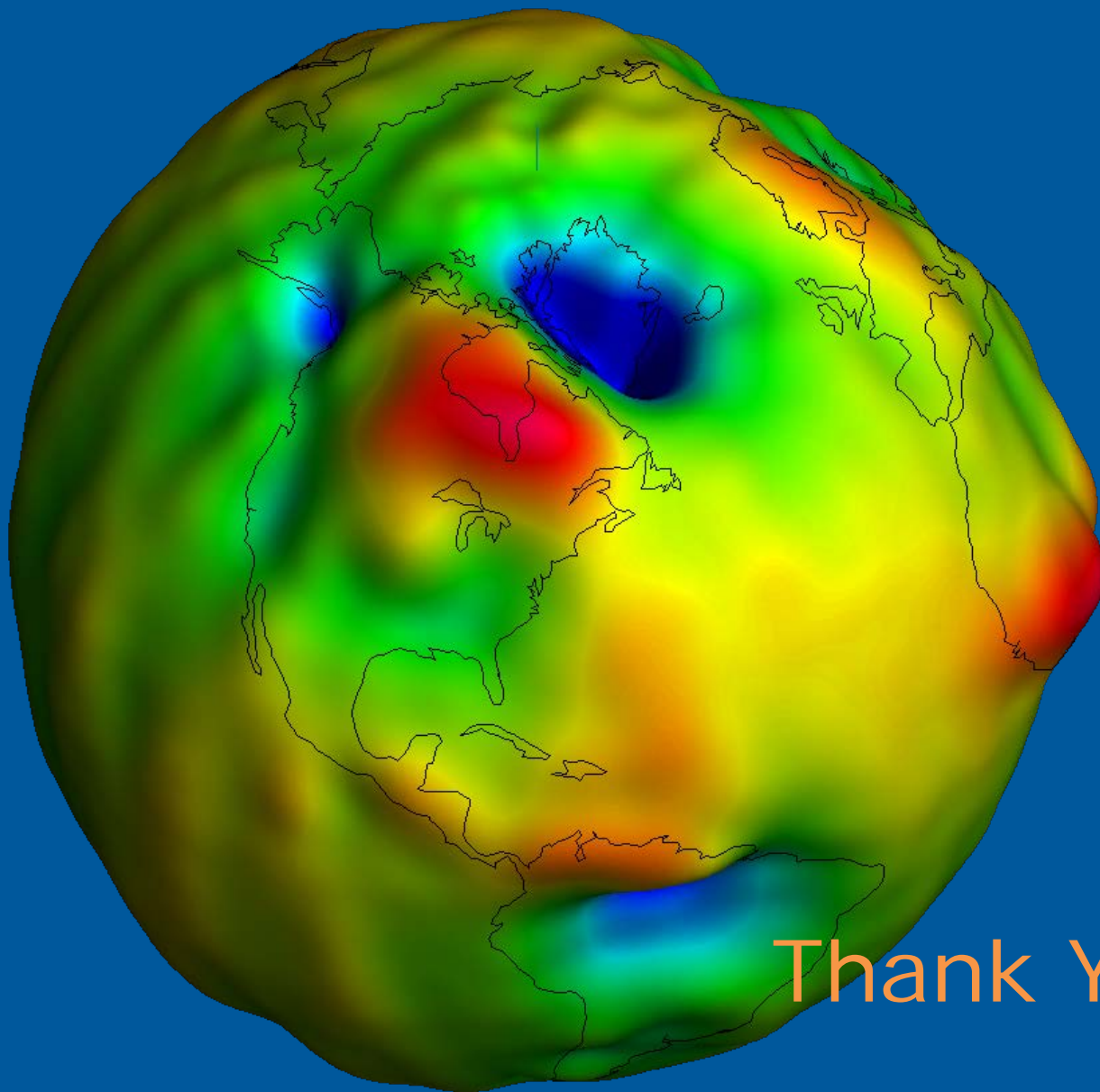


Conclusion

ICGEM do **NOT** offer:
research at the push of a button

But (hopefully) ICGEM:

- is useful for educational purposes
- helps to overcome obstacles in using the global gravity field models
- enables and stimulates research



Thank You